#### **Negative Differential Resistance, Instability, and Critical** 1 **Transition in Lightning Leader** 2 Xueqiang Gou<sup>1</sup><sup>+</sup>, Chao Xin<sup>1</sup>, Liwen Xu<sup>1</sup>, Ping Yuan<sup>1</sup>, Yijun Zhang<sup>2</sup>, Mingli Chen<sup>3</sup> 3 <sup>1</sup> College of Physics and Electronic Engineering, Northwest Normal University, Lanzhou 4 730070, China 5 <sup>2</sup> Department of Atmospheric and Oceanic Sciences & Institute of Atmospheric Sciences, Fudan 6 7 University, Shanghai, 200438, China <sup>3</sup> Department of Building Environment and Energy Engineering, The Hong Kong Polytechnic 8 University Hong Kong, SAR, China 9 <sup>†</sup>Corresponding to: Xueqiang Gou (1491168405@qq.com) 10 11 12 Abstract. The phenomena of leader extinction and restrike during lightning events, such as multiple strokes in ground 13 flashes or recoil leaders in cloud flashes, present significant challenges. A key aspect of this issue involves the 14 discussion of the channel's negative differential resistance and its instability. From the perspective of bifurcation 15 theory in nonlinear dynamics, this paper suggests an inherent consistency among the channel's negative differential 16 resistance, channel instability, and the critical transition from insulation to conduction. This study examines the 17 differential resistance characteristics of the leader-streamer system in lightning development. We correlate the 18 differential resistance characteristics of the leader-streamer channel with the channel's state and instability transitions, 19 investigating the critical current and potential difference conditions required for the stable transition of the leader-20 streamer channel. 21 Key words: negative differential resistance; instability; critical transition; lightning

## 22 1 Introduction

Natural lightning exhibits distinct intermittent characteristics that differentiate it from 23 24 long-gap discharges observed in laboratory settings (Gou et al., 2010; Gou et al., 2018a; Iudin et al., 2022). This intermittency is intrinsically linked to the fractal structure and critical dynamics 25 of the lightning process (Bulatov et al., 2020; Gou et al., 2018b, Sterpka et al., 2021; Iudin & 26 Syssoev, 2022; Syssoev et al., 2022). Additionally, the inherent polarity asymmetry in 27 bidirectional leader development introduces instability in the discharge process, leading to 28 29 destabilization and re-excitation phenomena in various lightning events (Van der Velde & 30 Montanya, 2013; Williams, 2006; Williams & Heckman, 2012; Iudin, 2021; da Silva et al., 2023; Scholten et al., 2023). 31

The intermittent nature of lightning is particularly evident in ground flashes, where 32 negative ground flash discharges are characteristically separated by extended periods of dim 33 luminosity. These periods are marked by a distinctive sequence: when the downward negative 34 channel decays and eventually terminates, the still-active intracloud positive component 35 intermittently creates conditions that facilitate the formation of dart or dart-stepped leaders (Van 36 der Velde & Montanya, 2013; Stock et al., 2014; Stock et al., 2023; Lapierre et al., 2017; Jensen 37 et al., 2023). A similar intermittent behavior is observed in cloud flashes, where the active 38 39 positive leader exhibits marked temporal asymmetry compared to the negative leader, resulting in K-processes or recoil leaders within the cloud. These transient phenomena are generally 40 attributed to channel instability, which manifests primarily through negative differential 41 resistance characteristics of the channel (Williams & Heckman, 2012; Mazur, 2016b). 42

43 In gas discharge physics, negative differential resistance is fundamentally associated with 44 bistability, hysteresis, and critical transitions (Bosch & Merlino, 1986; Lozneanu et al., 2002; Agop et al., 2012; Raizer & Mokrov, 2013). In lightning discharges, the leader and streamer 45 form a strongly coupled system with complex interactions: streamers supply the energy and 46 current essential for leader development, while the highly conductive leader channel maintains 47 the electric field and potential required for continuous streamer propagation. Given this intricate 48 coupling, this study expands the investigation of negative differential resistance properties to 49 encompass the entire leader-streamer system, rather than focusing solely on the leader channel. 50 Our analysis specifically examines the stability characteristics during lightning development and 51 identifies the critical conditions—in terms of current and potential difference—that govern 52 channel stability. 53

#### 54 2 Method

## 55 2.1 Negative differential resistance in lightning

Lightning, as a natural large-scale arc discharge, exhibits negative differential resistance characteristics in its channel (Heckman, 1992; da Silva et al., 2019). This behavior manifests when channel temperature and conductivity increase with current, leading to a decrease in the internal electric field needed to maintain the current, thus reducing the voltage across the channel (dV/dI < 0). This characteristic was identified by Krehbiel et al. (1979) as a potential mechanism for channel attenuation.

Heckman (1992) and Williams & Heckman (2012) investigated how negative differential resistance relates to the multiplicity of negative ground flashes. They proposed that while a channel with negative differential resistance connected to an extended streamer source is inherently unstable, parallel channel resistance and capacitance could provide stabilization. Specifically, channel stability occurs when the electrical response time constant (RC) exceeds the thermal attenuation constant  $\tau$ , with a critical stability current of approximately 100 A (Heckman, 1992; Williams, 2006; Williams & Heckman, 2012).

However, Mazur & Ruhnke (2014) and Mazur (2016a, b) challenged the appropriateness of modeling the leader channel as a parallel RC circuit. They argued that channel stability depends primarily on the minimum potential difference in the streamer zone at the channel tip, rather than negative differential resistance characteristics (Bazelyan & Raizer, 2000; Mazur, 2016a). Given that leader development is guided by numerous streamers at the front, we suggest that differential resistance analysis should consider both the leader channel and its associated streamers.

#### 76 **2.2 Negative differential resistance and bistability**

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To understand how negative differential resistance leads to bistability in lightning channels, we use a normalized relationship between current J and voltage  $\varphi$  that captures the essential nonlinear dynamics of the discharge process. This relationship emerges from the fundamental physics of plasma channel formation and maintenance (Agop et al., 2012):

$$\varphi = J\left(1 + \frac{a}{1 + J^2}\right) \tag{1}$$

82 where *a* is a dimensionless control parameter that governs the system's nonlinear 83 characteristics

As illustrated in Figure 1, for parameter a = 18, the  $J - \varphi$  characteristic curve exhibits three distinct regions. There are two stable regions where  $\varphi'(J) > 0$ : a low-conductivity state (segment AB) and a high-conductivity state (segment CD), both characterized by a monotonically increasing current with voltage. These stable regions are separated by an unstable region where  $\varphi'(J) < 0$ , demonstrating negative differential resistance. The system displays bistability, with critical transitions occurring between the two stable states: at point B, the system

- 90 abruptly transitions from the low-conductivity state to the high-conductivity state, while at point
- 91 D, it reverts to the low-conductivity state. This results in hysteretic behavior, where the system
- follows different paths during voltage increase  $(A \rightarrow B \rightarrow C)$  and decrease  $(C \rightarrow D \rightarrow A)$ .



$$\partial f / \partial J = -1 - a \frac{1 - J^2}{(1 + J^2)^2}$$
 (3)

104 From equation (1), at equilibrium we have 
$$\varphi = J(1 + \frac{a}{1 + J^2})$$
, and  $\partial f / \partial J = -\varphi'(J)$ .

105 The stability condition  $\partial f/\partial J > 0$  is equivalent to  $\varphi'(J) < 0$ , which corresponds to negative 106 differential resistance. This mathematical analysis provides insight into how the sign of channel 107 differential resistance determines the stability of lightning channel states and their transitions Similar bistability, hysteresis, and critical transitions are widely observed in biological,
atmospheric, ecological, and other systems, and they can be described by similar dynamical
systems (Scheffer & Carpenter, 2003; Scheffer, 2009). The generation of instability and
bistability can be illustrated by the rolling ball model shown in Figure 2, where the peaks and
valleys represent unstable and stable points, respectively. Instability triggered by strong
nonlinearities (positive feedback) is an important factor causing the bistability (polymorphism)
of the system and the critical transition.



## 116

117Fig. 2. Schematic representation of the locus of stability as a function of external conditions (adapted from118Scheffer & Carpenter, 2003, reprinted with permission from Springer Nature)

## 119 **2.3** The relationship between Lightning channel electric field and current.

The differential resistance characteristics of a gas discharge gap at a centimeter scale were measured first by King (1961). However, due to the effect of electrode vaporization, as pointed out by Mazur & Ruhnke (2014), King's results are only applicable to currents less than 10A with short gaps. In larger-scale lightning channels, the relationship between current and electric field is generally expressed in a power-law form. For example, Bazelyan et al. (2008) assumed that the leader channel current is inversely proportional to the electric field, ,  $E = 3400I^{-1}$ , meanwhile, Larsson et al. (2005) proposed that the relationship between channel current and
electric field can be described as:

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$$E = 1600I^{-0.18} \tag{4}$$

129 This is consistent with the observations of Tanaka et al. (2003) and aligns with the

suggestions of da Silva et al. (2019), who suggested that the power law varies for different

131 segments within the range of  $10^2$  to  $10^4$  A.

To develop a comprehensive description of the channel's electrical characteristics across
 different current regimes, we combined two complementary datasets:

134 1. King et al. (1961) data for I < 10 A, characterizing the initial breakdown phase where</li>
135 electrode effects dominate.

2. Larsson et al. (2005) measurements for I > 10 A, representing the fully developed
leader channel. The combined dataset was then fitted using a double power-law model that
captures both regimes

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 $E = aI^b + cI^d \tag{5}$ 

140 Where a = 4278, b = -0.9788, c = 1799, d = -0.2006, The minimum current used for

141 fitting was approximately 0.1 A.

Figure 3 shows the relationship between the electric field and current, with squares represent King's observations, circles representing Tanaka's (2003) experiments, and the solid green line representing the fitted curve.



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Fig. 3. Electric field versus current in arc channel

## 150 **2.4 Differential resistance of the leader-streamer channel**

151 The resistance of a streamer channel is determined by the potential difference  $\Delta U_{T}$  across 152 the streamer zone of the leader head and the channel current I, which can be expressed as 153 (Bazelyan & Raizer, 2000):

$$I = q_c V_L = 2\pi \varepsilon_0 V_L \Delta U_T \tag{6}$$

where  $q_c$  represents the channel charge line density, and  $V_L$  is the channel development speed. The relationship between  $V_L$  and l follows a power-law form (Bazelyan & Raizer, 2000; Popov, 2009):

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$$V_{I} = kI^{\alpha} \tag{7}$$

Since the power exponent  $\alpha$  varies significantly in different studies, such as  $\alpha \approx 1/3$ (Hutzler & Hutzler, 1982; Bazelyan et al., 2007) and  $\alpha \approx 0.66$  (Kekez & Savic, 1983), this study adopts  $k = 1.88 \times 10^4$ ,  $\alpha = 0.67$  based on more recent works (Andreev et al., 2008; Popov, 2009; Bazelyan et al., 2009). From Equations (6) and (7), we derive the voltage drop across the streamer zone at the leader head:

$$\Delta U_{T} = \frac{I}{2\pi\varepsilon_{0}kI^{\alpha}} = \frac{I^{1-\alpha}}{2\pi\varepsilon_{0}k}$$
(8)

166 Considering the leader channel potential drop  $U_C = LE$ , where *L* is the leader channel 167 length and *E* is the electric field of the channel as shown in Equation (4), and the streamer 168 channel potential drop  $\Delta U_T$  from Equation (8), the total potential drop *U* of the leader-169 streamer system is:

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$$U = L(aIb + cId) + \frac{I^{1-\alpha}}{2\pi\varepsilon_0 k}$$
(9)

Differentiating both sides with respect to I, we obtain the total differential resistance:

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$$\frac{dU}{dI} = L(abI^{b-1} + cdI^{d-1}) + (1 - \alpha)\frac{I^{-\alpha}}{2\pi\varepsilon_0 k}$$
(10)

#### 174 3 Analysis results

Figure 4 illustrates how the differential resistance varies with channel current for different leader channel lengths, where the horizontal line represents zero differential resistance. The point at which the curve intersects the horizontal line marks a change in the sign of the differential resistance, with the corresponding current at this intersection representing the critical current.



Fig. 4. Dependence of total differential resistance of channel on current with varying channel lengths (km).
 The horizontal line represents zero resistance

Figure 5 shows that both the critical currents and the critical potential differences in the streamer zone at the leader head increase with the channel length, which is consistent with theoretical predictions. This trend aligns with Heckman's 1992 study on critical currents, and supports the threshold condition for the critical potential difference proposed by Bazelyan & Raizer (2000) and Mazur (2016a).

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# Fig. 5. Critical channel current and potential difference of the streamer channel at the leader tip vary with channel length.

As the leader channel length increases, the ambient (stabilized) electric field decreases. Between 0.1 km and 12 km, the stabilized leader-streamer field drops from 15.5 kV/m to 1.1 kV/m. This trend is consistent with the findings of Lalande et al. (2002) and Becerra & Vernon (2006) who reported that the leader channel's ambient electric field decreases with channel height. Similarly, the internal electric field of the leader channel decreases (Figure 6). At a length of 0.1 km, the electric field is approximately 4.9 kV/m, while at 12 km, it drops to 0.65 kV/m. Syssoev & Shcherbakov (2001) found that stable thermal leader channels with long electric

198 fields (30–50 m) had electric fields around 3–10 kV/m, which is consistent with our results.



200Fig. 6. variations of ambient electric field of the leader-streamer system and electric field of the leader201channels with length

## 202 4 Discussion and conclusion

This paper extends the discussion on lightning discharge channel stability and differential 203 204 resistance from the leader channel to the leader-streamer system. Using bifurcation theory and critical transition theory from nonlinear dynamics, we studied the extinction, re-excitation, and 205 critical transition of intermittent events (such as recoil leaders) in the lightning process. By 206 analyzing the sign changes in the differential resistance of the leader-streamer system, we 207 208 determined the critical current and the critical potential difference at the channel end. Our results show that as the channel length increases, both the critical current and the critical potential 209 difference at the channel end increase. Meanwhile, the average ambient electric field and the 210 electric field required for stable transmission gradually decrease after an initial sharp drop. These 211 findings are consistent with existing research. 212

The exact mechanism behind the sudden change in channel conductivity remains unclear, but it is likely related to instability caused by positive feedback within the channel. The reexcitation of a decayed leader channel is typically due to the uneven distribution of current and electric field, which becomes more pronounced with increasing channel length. This asymmetry is particularly evident in the channel structure: the leader head maintains higher charge concentration and conductivity, remaining active and often merging with adjacent channels,

while the rear part exhibits lower conductivity and greater susceptibility to disconnection andsplitting

In the case of negative ground flashes, the electric field in the upper channel becomes 221 non-uniform due to the low current in the positive leader section, which is insufficient to 222 maintain conductivity in the lower channel. Recent observations show that the low current in the 223 positive leader and poor conductivity in the rear section lead to negative charge deposition in the 224 center of the rear channel. This creates negatively polarized needle structures that trigger 225 226 nonlinear instability (Williams & Montanya, 2019; Hare et al., 2019; Pu & Cummer, 2019; Hare et al., 2021). The current in the rear positive leader decreases, leading to disconnection from the 227 negative leader. The increased potential difference at the paused negative leader causes re-228 breakdown and reconnection, resulting in multiple strokes. In contrast, positive ground flashes 229 230 feature stronger current at the negative leader head, making the channel less prone to splitting, which typically results in a single stroke. 231

232 The transition from a semiconductor to a conductive state in the leader channel may be driven by ionization-thermal instability caused by positive feedback. As shown in previous 233 234 studies (Bazelyan & Raizer, 2000; Popov, 2009; da Silva et al., 2019), the pulsed mechanism of the stepped leader is related to electric field inhomogeneity among the streamers at the leader 235 236 head (Syssoev & Iudin, 2023). This instability may exacerbate the electrical inhomogeneity in the streamer zone, which is thought to be triggered by attachment instability (Douglas-Hamilton 237 238 & Mani, 1974; Sigmond, 1984; Luque et al., 2016; Malagón-Romero & Luque, 2019). If the mechanism in positive stepped leaders is similar to that of negative stepped leaders, the 239 excitation of the leader should occur in the streamer zone at the leader head (Tran & Rakov, 240 2016; Kostinskiy et al., 2018; Huang et al., 2020; Wang et al., 2020). 241

Furthermore, the inhomogeneities, instabilities, and critical transitions observed in the leader channel and streamer zone, whether during initiation or transmission, as well as the emergence of pulse events of various scales and the interactions between leader channels, streamers, and other streamers, all exhibit collective, fractal, and critical properties. These phenomena may require more unified explanations based on fractal analysis and critical dynamics.

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# 267 Code/Data Availability

The data and code used in this study are available from the corresponding author on reasonable request.

## 270 Author Contribution

- Xueqiang Gou: Conceptualization, Methodology, Software, Validation,
   Formal analysis, Investigation, Writing Original Draft, Review &
   Editing, Visualization, Supervision, Project administration.
- **Chao Xin**: Software, Formal analysis,
- Liwen Xu: Visualization.
- Ping Yuan, Yijun Zhang, Mingli Chen: Review & Editing Supervision
- 277 Competing Interests

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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