1 2	Negative Differential Resistance, Instability, and Critical Transition in Lightning Leader	
3	Xueqiang Gou <sup>1</sup> †, Chao Xin <sup>1</sup> Liwen Xu <sup>1</sup> Ping Yuan <sup>1</sup> Yijun Zhang <sup>2</sup> Mingli <u>Chen<sup>3</sup></u>	删除了: Cheng <sup>3</sup>
4	<sup>1</sup> College of Physics and Electronic Engineering, Northwest Normal University, Lanzhou 730070, China	
6 7	<sup>2</sup> Department of Atmospheric and Oceanic Sciences & Institute of Atmospheric Sciences, Fudan University, Shanghai, 200438, China	
8 9	<sup>3</sup> Department of Building Environment and Energy Engineering, The Hong Kong Polytechnic University Hong Kong, SAR, China	
10	<sup>†</sup> Corresponding to: Xueqiang Gou (1491168405@qq.com)	
11 12 13	Abstract. The phenomena of leader extinction and restrike during lightning events, such as multiple strokes in ground flashes or recoil leaders in cloud flashes, present significant challenges. A key aspect of this issue involves the	
14	discussion of the channel's negative differential resistance and its instability. From the perspective of bifurcation	删除了: channel's
15	theory in nonlinear dynamics, this paper suggests an inherent consistency among the channel's negative differential	删除了: posits
16	resistance, channel instability, and the critical transition from insulation to conduction. This study examines the	删除了: channel's
17	differential resistance characteristics of the leader-streamer system in lightning development. We correlate the	
18	differential resistance characteristics of the leader-streamer channel with the channel's state and instability transitions,	<b>删除了:</b> channel's
19	investigating the critical current and potential difference conditions required for the stable transition of the leader-	
20	streamer channel.	
21	Key words: negative differential resistance; instability; critical transition; lightning	
22	1 Introduction	
23	Natural lightning exhibits distinct intermittent characteristics that differentiate it from	删除了: an intermittent nature
24	long-gap discharges observed in laboratory settings (Gou et al., 2010; Gou et al., 2018a; Iudin et	<b>删除了:</b> 2018
25	al., 2022). This intermittency is <u>intrinsically linked</u> to the fractal structure and critical dynamics	删除了: closely related
26	of the lightning process (Bulatov et al., 2020; Gou et al., 2018b, Sterpka et al., 2021; Iudin &	删除了: characteristics
27	Syssoev, 2022; Syssoev et al., 2022). Additionally, the <u>inherent polarity</u> asymmetry <u>in</u>	删除了: between positive and negative polarities
28	bidirectional leader development introduces instability in the discharge process, leading to	<b>删除了:</b> inherent
29	destabilization and re-excitation phenomena in various lightning events (Van der Velde &	删除了: of
30	Montanya, 2013; Williams, 2006; Williams & Heckman, 2012; Iudin, 2021; da Silva et al., 2023;	删除了: 2016
31	Scholten et al., 2023).	

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45	The intermittent nature of lightning is particularly evident in ground flashes, where		<b>H</b> IB
46	negative ground flash discharges are characteristically separated by extended periods of dim	$\square$	删除
47	Juminosity. These periods are marked by a distinctive sequence: when the downward negative		删除
48	channel decays and eventually <u>terminates</u> , the <u>still-active intracloud positive component</u>		删除
49	intermittently <u>creates</u> conditions that facilitate the formation of dart or dart-stepped leaders (Van		删除
50	der Velde & Montanya, 2013; Stock et al., 2014; Stock et al., 2023; Lapierre et al., 2017; Jensen		删除
51	et al., 2023). <u>A similar intermittent behavior is observed in cloud flashes, where the active</u>		删除
52	positive leader exhibits marked temporal asymmetry compared to the negative leader, resulting		制限
53	in K-processes or recoil leaders within the cloud. These transient phenomena are generally		删除
54	attributed to channel instability, which manifests primarily through negative differential		删除
55	resistance characteristics of the channel (Williams & Heckman, 2012; Mazur, 2016b).		删版 Stoc
56	In gas discharge physics, negative differential resistance is <u>fundamentally</u> associated with		删除
57	bistability, hysteresis, and <u>critical</u> transitions (Bosch & Merlino, 1986; Lozneanu et al., 2002;		inte
58	Agop et al., 2012; Raizer & Mokrov, 2013). In lightning discharges, the leader and streamer		inst
59	form a strongly coupled system with complex interactions: streamers supply the energy and		201 the
60	current essential for leader development, while the highly conductive leader channel maintains		char
61	the electric field and potential required for continuous streamer propagation. Given this intricate		删除
62	coupling, this study expands the investigation of negative differential resistance properties to		删除
63	encompass the entire leader-streamer system, rather than focusing solely on the leader channel.	$\langle  $	stre:
64	Our analysis specifically examines the stability characteristics during lightning development and		删除
65	identifies the critical conditions—in terms of current and potential difference—that govern		删除
66	channel stability.		删除
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67	2, Method		删除
68	2.1 Negative differential resistance in lightning		删除
60	Lightning as a natural large scale are discharge, exhibits negative differential resistance		删除
09	Lighting, as a natural jarge-scale are discharge, exhibits negative differential resistance	/	删版
70	<u>characteristics</u> in its channel (Heckman, 1992; da Silva et al., 2019). This <u>behavior manifests</u>	//	删除
71	when channel temperature and conductivity increase with current, leading to a decrease in the		删除
72	internal electric field <u>needed</u> to maintain the current <u>thus reducing</u> the voltage across the channel	$\langle$	删除
73	(dV/dI < 0). This characteristic was identified by Krehbiel et al. (1979) as a potential mechanism		加加

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删除了: ground flashes (Van der Velde & Montanya, 2013; Stock et al., 2014; Lapierre et al., 2017

删除了: Recoil leaders are generally believed to arise from instability in the bidirectional leader channel due to current interruption (Williams & Heckman, 2012; Mazur, 2016). Stepped leaders are thought to emerge from various instabilities within the streamer channel at the leader's end and their critical transitions (Malagón-Romero & Luque, 2019; Hare et al., 2021). These instabilities often manifest as the negative differential resistance characteristics of the channel.

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for channel attenuation.

123	Heckman (1992) and Williams & Heckman (2012) investigated how negative differential	删除了:
124	resistance <u>relates to</u> the multiplicity of negative ground flashes. They <u>proposed</u> that while a	between 删除了:
125	channel with negative differential resistance connected to an extended streamer source is	删除了:
126	inherently unstable, parallel channel resistance and capacitance could provide stabilization.	删除了:
127	Specifically, channel stability occurs when the electrical response time constant (RC) exceeds	删除了:
128	the thermal attenuation constant $\tau_{a}$ with a critical stability current of approximately <u>100 A</u>	删除了:
129	(Heckman, 1992; Williams, 2006; Williams & Heckman, 2012).	删除了:
130	However, Mazur & Ruhnke (2014) and Mazur (2016a, b) challenged the appropriateness	删除了:
131	of modeling the leader channel as a parallel RC circuit. They argued that channel stability	删除∫:
132	depends primarily on the minimum potential difference in the streamer zone at the channel tip,	删除了:
133	rather than negative differential resistance characteristics (Bazelyan & Raizer, 2000; Mazur,	unstable.
134	2016a). Given that leader development is guided by numerous streamers at the front, we suggest	删除了:
135	that differential resistance analysis should consider both the leader channel and its associated	删除了:
136	streamers.	删除了:
137	2.2 Negative differential resistance and bistability	be appro channel i currents,
138	<u>To understand how</u> negative differential resistance, <u>leads to</u> bistability in <u>lightning</u>	determin
138 139	<u>To understand how</u> negative differential resistance, leads to bistability in lightning channels, we use a normalized relationship between current $J$ and voltage $\varphi$ that captures the	negative determin <b>删除了:</b>
138 139 140	<u>To understand how negative differential resistance leads to bistability in lightning</u> <u>channels, we use</u> a normalized relationship between current $J$ and voltage $\varphi$ that captures the <u>essential nonlinear dynamics of the discharge process. This relationship emerges from the</u>	negative determin 删除了: 删除了: 删除了:
<ol> <li>138</li> <li>139</li> <li>140</li> <li>141</li> </ol>	<u>To understand how negative differential resistance leads to bistability in lightning</u> <u>channels, we use</u> a normalized relationship between current $J$ and voltage $\varphi$ <u>that captures the</u> <u>essential nonlinear dynamics of</u> the discharge process. This relationship emerges from the <u>fundamental physics of plasma</u> channel <u>formation and maintenance</u> (Agop et al., 2012):	negative determin 删除了: 删除了: 删除了: 删除了:
<ol> <li>138</li> <li>139</li> <li>140</li> <li>141</li> <li>142</li> </ol>	To understand how negative differential resistance leads to bistability in lightning channels, we use a normalized relationship between current $J$ and voltage $\varphi$ that captures the essential nonlinear dynamics of the discharge process. This relationship emerges from the fundamental physics of plasma channel formation and maintenance (Agop et al., 2012): $\varphi = J \left( 1 + \frac{a}{1+J^2} \right) $ (1)	negative determin 删除了: 删除了: 删除了: 删除了: 删除了: 们除了: 们除了:
<ol> <li>138</li> <li>139</li> <li>140</li> <li>141</li> <li>142</li> <li>143</li> </ol>	To understand how negative differential resistance, leads to bistability in lightning channels, we use a normalized relationship between current $J$ and voltage $\varphi$ that captures the essential nonlinear dynamics of the discharge process. This relationship emerges from the fundamental physics of plasma channel formation and maintenance (Agop et al., 2012): $\varphi = J\left(1 + \frac{a}{1+J^2}\right)$ (1) where $a$ is a dimensionless control parameter that governs the system's nonlinear	negative determin 删除了: 删除了: 删除了: 删除了: 删除了: 删除了: 而the cham resistance be detern the
<ol> <li>138</li> <li>139</li> <li>140</li> <li>141</li> <li>142</li> <li>143</li> <li>144</li> </ol>	<u>To understand how negative differential resistance leads to bistability in lightning</u> <u>channels, we use</u> a normalized relationship between current $J$ and voltage $\varphi$ <u>that captures the</u> <u>essential nonlinear dynamics of the discharge process. This relationship emerges from the</u> <u>fundamental physics of plasma</u> channel formation and maintenance (Agop et al., 2012): $\varphi = J\left(1 + \frac{a}{1+J^2}\right)$ (1) <u>where a is a dimensionless control parameter that governs the system's nonlinear</u> <u>characteristics</u>	negative determin 删除了: 删除了: 删除了: 删除了: 删除了: 们除了: 机除了: 则除了: 则除了:
<ol> <li>138</li> <li>139</li> <li>140</li> <li>141</li> <li>142</li> <li>143</li> <li>144</li> <li>145</li> </ol>	To understand how negative differential resistance, leads to bistability in lightning channels, we use a normalized relationship between current $J$ and voltage $\varphi$ that captures the essential nonlinear dynamics of the discharge process. This relationship emerges from the fundamental physics of plasma channel formation and maintenance (Agop et al., 2012): $\varphi = J\left(1 + \frac{a}{1+J^2}\right)$ (1) where $a$ is a dimensionless control parameter that governs the system's nonlinear characteristics As illustrated in Figure 1, for parameter $a = 18$ , the $J - \varphi$ characteristic curve exhibits	negative determin 删除了: 删除了: 删除了: 删除了: 删除了: 删除了: 删除了: 删除了:
<ol> <li>138</li> <li>139</li> <li>140</li> <li>141</li> <li>142</li> <li>143</li> <li>144</li> <li>145</li> <li>146</li> </ol>	To understand how negative differential resistance leads to bistability in lightning channels, we use a normalized relationship between current $J$ and voltage $\varphi$ that captures the essential nonlinear dynamics of the discharge process. This relationship emerges from the fundamental physics of plasma channel formation and maintenance (Agop et al., 2012): $\varphi = J\left(1 + \frac{a}{1+J^2}\right)$ (1) where $a$ is a dimensionless control parameter that governs the system's nonlinear characteristics As illustrated in Figure 1, for parameter $a = 18$ , the $J - \varphi$ characteristic curve exhibits three distinct regions. There are two stable regions where $\varphi'(J) > 0$ : a low-conductivity state	negative determin 删除了:
<ol> <li>138</li> <li>139</li> <li>140</li> <li>141</li> <li>142</li> <li>143</li> <li>144</li> <li>145</li> <li>146</li> <li>147</li> </ol>	To understand how negative differential resistance, leads to bistability in lightning channels, we use a normalized relationship between current $J$ and voltage $\varphi$ that captures the essential nonlinear dynamics of the discharge process. This relationship emerges from the fundamental physics of plasma channel formation and maintenance (Agop et al., 2012): $\varphi = J\left(1 + \frac{a}{1+J^2}\right)$ (1) where $a$ is a dimensionless control parameter that governs the system's nonlinear characteristics As illustrated in Figure 1, for parameter $a = 18$ , the $J - \varphi$ characteristic curve exhibits three distinct regions. There are two stable regions where $\varphi'(J) > 0$ : a low-conductivity state (segment AB) and a high-conductivity state (segment CD), both characterized by a	negative determin 删除了: 删除了: 删除了: 删除了: 删除了: 删除了: 删除了: 删除了:
<ol> <li>138</li> <li>139</li> <li>140</li> <li>141</li> <li>142</li> <li>143</li> <li>144</li> <li>145</li> <li>146</li> <li>147</li> <li>148</li> </ol>	To understand how negative differential resistance, leads to bistability in lightning channels, we use a normalized relationship between current $J$ and voltage $\varphi$ that captures the essential nonlinear dynamics of the discharge process. This relationship emerges from the fundamental physics of plasma channel formation and maintenance (Agop et al., 2012): $\varphi = J\left(1 + \frac{a}{1+J^2}\right)$ (1) where $a$ is a dimensionless control parameter that governs the system's nonlinear characteristics As illustrated in Figure 1, for parameter $a = 18$ , the $J - \varphi$ characteristic curve exhibits three distinct regions. There are two stable regions where $\varphi'(J) > 0$ : a low-conductivity state (segment AB) and a high-conductivity state (segment CD), both characterized by a monotonically increasing current with voltage. These stable regions are separated by an unstable	negative determin 删除了:
<ol> <li>138</li> <li>139</li> <li>140</li> <li>141</li> <li>142</li> <li>143</li> <li>144</li> <li>145</li> <li>146</li> <li>147</li> <li>148</li> <li>149</li> </ol>	To understand how negative differential resistance leads to bistability in lightning channels, we use a normalized relationship between current $J$ and voltage $\varphi$ , that captures the essential nonlinear dynamics of the discharge process. This relationship emerges from the fundamental physics of plasma channel formation and maintenance (Agop et al., 2012): $\varphi = J\left(1 + \frac{a}{1+J^2}\right)$ (1) where $a$ is a dimensionless control parameter that governs the system's nonlinear characteristics As illustrated in Figure 1, for parameter $a = 18$ , the $J - \varphi$ characteristic curve exhibits three distinct regions. There are two stable regions where $\varphi'(J) > 0$ : a low-conductivity state (segment AB) and a high-conductivity state (segment CD), both characterized by a monotonically increasing current with voltage. These stable regions are separated by an unstable region where $\varphi'(J) < 0$ , demonstrating negative differential resistance. The system displays	negative         determin         删除了:

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Ň	删除了: for the channel resistance is greater than
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V)	<b>删除了:</b> to
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	删除了: of the channel is
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	删除了: a large number of streamers originating from the front, the high resistance of the streamer zone is important for the channel's stability. We suggest that the differential resistance properties of the lightning channel should not only be determined by the leader channel but should also include the
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删除了: Figure 1 shows the theoretical dependence of the normalized current on the normalized voltage. It can be seen that as the parameter *a* increases, the system changes from stable to unstable. For example, when the parameter a = 6, ....



Then

$$\partial f / \partial J = -1 - a \frac{1 - J^2}{(1 + J^2)^2}$$
 (3)

E31 From equation (1), at equilibrium we have 
$$\varphi = J(1 + \frac{a}{1 + J^2})$$
, and  $\partial f/\partial J = -\varphi'(J)$ 

<u>The stability</u> condition  $\partial f/\partial J > 0$  is equivalent to  $\varphi'(J) < 0$ , which corresponds to negative 232 233 differential resistance. This mathematical analysis provides insight into how the sign of channel 234 differential resistance determines the stability of lightning channel states and their transitions,

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252 Similar bistability, hysteresis, and critical transitions are widely observed in biological, 253 atmospheric, ecological, and other systems, and they can be described by similar dynamical 254 systems (Scheffer & Carpenter, 2003; Scheffer, 2009). The generation of instability and 255 bistability can be illustrated by the rolling ball model shown in Figure 2, where the peaks and 256 valleys represent unstable and stable points, respectively. Instability triggered by strong 257 nonlinearities (positive feedback) is an important factor causing the bistability (polymorphism) 258 of the system and the critical transition.





Fig. 2. Schematic representation of the locus of stability as a function of external conditions (adapted from Scheffer & Carpenter, 2003, reprinted with permission from Springer Nature)

263 2.3 The relationship between Lightning channel electric field and current.

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280	meanwhile, Larsson et al. (2005) proposed that the relationship between channel current and		删除了: suggested
281	electric field <u>can be described as:</u>		删除了: varies within the range of 10 <sup>2</sup> -10 <sup>4</sup> A
282	$E = 1600I^{-0.18} \tag{4}$		
283	This is consistent with the observations of Tanaka et al. (2003) and aligns with the		
284	suggestions of da Silva et al. (2019) . who suggested that the power law varies for different		删除了: differs
285	segments within the range of $10^2$ to $10^4$ A.		删除了: each segment
286	To develop a comprehensive description of the channel's electrical characteristics across		删除了: -10 <sup>4</sup> A. To better describe this relationship, we combined the data from King et al. (1961) and Larsson et al. (2005)
287	different current regimes, we combined two complementary datasets:	$\langle \rangle$	删除了: For currents less than 10 A, we used
288	<u>1. King et al. (1961) data for I &lt; 10 A, characterizing the initial breakdown phase where</u>	_ `	删除了: results of
289	electrode effects dominate.		删除了: ). For currents greater than 10 A, we applied the formula provided by
290	<u>2.</u> Larsson et al. (2005) measurements for $I > 10$ A, representing the fully developed		删除了: (Eq. 4) Both sets of data were
291	leader channel. The combined dataset was then fitted using a double power-law model that		删除了: with a formula.
292	captures both regimes		
293	$E = aI^b + cI^d \tag{5}$		
294	Where $a = 4278, b = -0.9788, c = 1799, d = -0.2006$ , The minimum current <u>used</u> for		
295	fitting <u>was</u> approximately 0, <u>1 A.</u>		删除了: is taken to be
296	Figure 3 shows the relationship between the electric field and current, with squares		<b>删除了:</b> 1A.
207	represent King's observations circles representing Tanaka's (2003) experiments and the solid		删除了: where the
297	represent King's observations, encies representing ranaka's (2005) experiments, and the solid	<	删除了: the
298	green line <u>representing</u> the <u>fitted curve</u> .		删除了: represent
299	•		删除了: represents
		$\langle \rangle$	<b>删除了:</b> fit



	Potential gradient (V/m)	
377	10 <sup>-2</sup> 10 <sup>-1</sup> 10 <sup>0</sup> 10 <sup>1</sup> 10 <sup>2</sup> 10 <sup>3</sup> Current (A)	
322		
324	Fig. 3. Electric field versus current in arc channel	<b>删除了:</b> A streamer channel's
325		<b>删除了:</b> of
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326	2.4 Differential resistance of the leader-streamer channel	
227		(删除了:)
327	<u>The resistance of a streamer channel</u> is determined by the potential difference $\Delta v_{T_{actoss}}$	删除了: denotes
328	the streamer zone of the leader head and the channel current $I$ , which can be expressed as	删除了: denotes
329	(Bazelvan & Raizer, 2000):	删除了:,
		删除了: follow
330	$I = q_c V_L = 2\pi \varepsilon_0 V_L \Delta U_T $	删除了: relationship
331	where $q_r$ represents the channel charge line density, and $V_r$ is the channel development speed.	
332	The relationship between $V$ and $I$ follows a power-law form (Bazelvan & Raizer, 2000; Popov,	
333	2009):	加除J:As
		m读了: exponents vary substantiany among
334	$V_{I} = kI^{\alpha} $ (7)	删除了:
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335	Since the power exponent $\alpha$ varies significantly in different studies, such as $\alpha \approx 1/3$	删除了: in
336	(Hutzler & Hutzler, 1982; Bazelyan et al., 2007) and $\alpha \approx 0.66$ (Kekez & Savic, 1983), this	删除了: paper, we adopt
337	study adopts $k = 1.88 \times 10^4$ , $\alpha = 0.67$ based on more recent works (Andreev et al., 2008:	删除了: studies
220	Bonoy, 2000; Bazelyon et al. 2000)	<b>删除了:</b> ,
538	ropov, 2009, dazeryan et al., 2009).	删除了:,

362	From Equations (6) and (7), we derive the voltage drop across the streamer zone at the
363	leader head <u>:</u>
364	$\Delta U_{T} = \frac{I}{2\pi\varepsilon_{0}kI^{\alpha}} = \frac{I^{1-\alpha}}{2\pi\varepsilon_{0}k} $ (8)
365	Considering the leader channel potential drop $U_C = LE$ , where $L$ is the leader channel

366 length and E is the electric field of the channel as shown in <u>Equation</u> (4), and the streamer channel potential drop  $\Delta U_{T_{e}}$  from Equation (8), the total potential drop U of the leader-367 368 streamer system is; 260

378

$$U = L(\mathbf{aI}^b + c\mathbf{I}^d) + \frac{I^{1-\alpha}}{2\pi\varepsilon_0 k}$$

<u>(9)</u>

<u>Differentiating</u> both sides with respect to  $I_{\text{we obtain}}$  the total differential resistance: 371

372 
$$\frac{dU}{dI} = L(abI^{b-1} + cdI^{d-1}) + (1-\alpha)\frac{I^{-\alpha}}{2\pi\varepsilon_0 k}$$
(10)

#### 373 **3** Analysis results

Figure 4 illustrates how the differential resistance varies with channel current for different 374 375 Jeader channel lengths, where the horizontal line represents zero differential resistance. The point 376 at which the curve intersects the horizontal line, marks a change in the sign of the differential 377 resistance, with the corresponding current at this intersection representing the critical current. 25 0.8 20 (UX) (UX) 10/01 17 5 3.8 0 6.3 7.7 9.2 17 27 41 57 77 101 131 8

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Fig4

Current (A)

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411	Fig. 4. Dependence of total differential resistance of channel on current with varying channel lengths (km)		副除了.
412	The horizontal line represents zero resistance.		제)않了•··
413	Figure 5 shows that both the critical currents and the critical potential differences in the		
414	and the ender had increase with the abarrel length which is consistent with		
414	streamer zone at the leader head increase with the channel length, which is consistent with		
415	theoretical predictions. This trend aligns with Heckman's 1992 study on critical currents, and		删除了:. It is also shown that the critical potential difference for the streamer zone of the leader's head also increase with
416	supports the threshold condition for the critical potential difference proposed by Bazelyan &		leader length, which aligns with
417	Raizer (2000) and Mazur (2016a).		删除了: of the leader's development
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	Channel Length (km) 5.5 5.5 5.5 4.7 4.7 4.7 4.7 4.7 4.7 4.7 4.7		Fig5
419	Channel length (km)		
420	Fig. 5. Critical channel current and potential difference		
421	of the streamer channel at the leader tip vary with channel length.		
422	As the leader channel length increases, the ambient (stabilized) electric field decreases		删除了: It can be observed that
423	Between 0.1 km and 12 km, the stabilized leader-streamer field drops from 15.5 kV/m to 1.1	$\frown$	删除了: leader channel's
124	kV/m This trand is consistent with the findings of Lelande at al. (2002) and Becorra & Vernon	$\overline{)}$	删除了:,
424	k v/m, This tiend is consistent with the internet solution and becerra & vernon	$\sim$	删除了: ambient electrical field of the
425	(2006) who reported that the leader channel's ambient electric field decreases with channel		删除了:, this
426	height. Similarly, the internal electric field of the leader channel decreases (Figure 6). At a length	$\mathbb{N}$	删除了: channel's
427	of 0.1 km, the electric field is approximately 4.9 kV/m, while at 12 km, it drops to 0.65 kV/m.		删除了: (stabilized)
428	Syssoey & Shcherbakoy (2001) found that stable thermal leader channels with long electric		删除 J: the channel's
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429	fields $(30-50 \text{ m})$ <u>nad electric fields around</u> $3-10 \text{ kV/m}$ , which is <u>consistent with</u> our results.	1///	加限了: about4
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### 469 4 Discussion and conclusion

470	This paper extends the discussion on lightning discharge channel stability and differential
471	resistance from the leader channel to the leader-streamer system. Using bifurcation theory and
472	critical transition theory from nonlinear dynamics, we studied the extinction, re-excitation, and
473	critical transition of intermittent events (such as recoil leaders) in the lightning process, By
474	analyzing the sign changes in the differential resistance of the leader-streamer system, we
475	determined the critical current and the critical potential difference at the channel end. Our results
476	show that as the channel length increases, both the critical current and the critical potential
477	difference at the channel end increase. Meanwhile, the average ambient electric field and the
478	electric field required for stable transmission gradually decrease after an initial sharp drop. These
470	electric field fequiled for subje transmission graduary decrease after an initial sharp drop. These
479	findings are consistent with existing research.
479 480	findings are consistent with existing research. The <u>exact</u> mechanism behind the sudden change in channel conductivity remains unclear.
479 480 481	findings are consistent with existing research. The <u>exact</u> mechanism behind the sudden change in channel conductivity remains unclear, but <u>it is likely</u> related to instability caused by positive feedback <u>within</u> the channel. The re-
479 480 481 482	findings are consistent with existing research. The <u>exact</u> mechanism behind the sudden change in channel conductivity remains unclear, but <u>it is likely</u> related to instability caused by positive feedback <u>within</u> the channel. The re- excitation of a decayed leader channel is <u>typically</u> due to <u>the</u> uneven distribution of current and
479 480 481 482 483	findings are consistent with existing research. The <u>exact</u> mechanism behind the sudden change in channel conductivity remains unclear, but <u>it is likely</u> related to instability caused by positive feedback <u>within</u> the channel. The re- excitation of a decayed leader channel is <u>typically</u> due to <u>the</u> uneven distribution of current and electric field, which becomes more pronounced with increasing channel length. This asymmetry
479 480 481 482 483 484	findings are consistent with existing research. The <u>exact</u> mechanism behind the sudden change in channel conductivity remains unclear, but <u>it</u> is <u>likely</u> related to instability caused by positive feedback <u>within</u> the channel. The re- excitation of a decayed leader channel is <u>typically</u> due to <u>the</u> uneven distribution of current and electric field, which becomes more pronounced with increasing channel length. This asymmetry is particularly evident in the channel structure: the leader head <u>maintains</u> higher charge
479 480 481 482 483 484 485	findings are consistent with existing research. The <u>exact</u> mechanism behind the sudden change in channel conductivity remains unclear, but <u>it</u> is <u>likely</u> related to instability caused by positive feedback <u>within</u> the channel. The re- excitation of a decayed leader channel is <u>typically</u> due to <u>the</u> uneven distribution of current and electric field, which becomes more pronounced with increasing channel length. This asymmetry <u>is particularly evident in the channel structure</u> : the leader head <u>maintains</u> higher charge concentration and conductivity, <u>remaining</u> active and often merging with adjacent channels.

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510 while the rear part exhibits lower conductivity and greater susceptibility to disconnection and 511 splitting 512 In the case of negative ground flashes, the electric field in the upper channel becomes 513 non-uniform due to the low current in the positive leader section, which is insufficient to 514 maintain conductivity in the lower channel. Recent observations show that the low current in the 515 positive leader and poor conductivity in the rear section lead to negative charge deposition in the 516 center of the rear channel. This creates negatively polarized needle structures that trigger nonlinear instability (Williams & Montanya, 2019; Hare et al., 2019; Pu & Cummer, 2019; Hare 517 et al., 2021). The current in the rear positive leader decreases, leading to disconnection from the 518 negative leader. The increased potential difference at the paused negative leader causes re-519 520 breakdown and reconnection, resulting in multiple strokes. In contrast, positive ground flashes, 521 feature stronger current at the negative leader head, making the channel less prone to splitting, 522 which typically results in a single stroke. 523 The transition from a semiconductor to a <u>conductive</u> state in the leader channel may be driven by ionization-thermal instability caused by positive feedback. As shown in previous 524 studies (Bazelyan & Raizer 2000: Popov 2009: da Silva et al., 2019), the pulsed mechanism of 525 the stepped leader is related to electric field inhomogeneity among the streamers at the leader 526 527 head (Syssoev & Iudin, 2023). This instability may exacerbate the electrical inhomogeneity in 528 the streamer zone, which is thought to be triggered by attachment instability (Douglas-Hamilton & Mani, 1974; Sigmond, 1984; Luque et al., 2016; Malagón-Romero & Luque, 2019). If the 529 mechanism in positive stepped leaders is similar to that of negative stepped leaders, the 530 531 excitation of the leader should occur in the streamer zone at the leader head (Tran & Rakov, 532 2016; Kostinskiy et al., 2018; Huang et al., 2020; Wang et al., 2020). 533 Furthermore, the inhomogeneities, instabilities, and critical transitions observed in the 534 leader channel and streamer zone, whether during initiation or transmission, as well as the 535 emergence of pulse events of various scales and the interactions between leader channels, streamers, and other streamers, all exhibit collective, fractal, and critical properties. These 536 537 phenomena may require more unified explanations based on fractal analysis and critical

538 dynamics.

539 Acknowledgments

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theory to observation," by Marten Scheffer and Stephen R. Carpenter, published
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## 665 Code/Data Availability

666 The data and code used in this study are available from the corresponding667 author on reasonable request.

# 668 Author Contribution

669 •	Xueqiang Gou: Conceptualization, Methodology, Software, Validation,
670	Formal analysis, Investigation, Writing - Original Draft, Review &
671	Editing, Visualization, Supervision, Project administration.

- Chao Xin: Software, Formal analysis,
- Liwen Xu: Visualization.
- Ping Yuan, Yijun Zhang, Mingli Chen: Review & Editing Supervision

675 Competing Interests

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删除了: Conceptualization,

678 The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported 679 680 in this paper.

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