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Observations of Shoaling Internal Wave Transformation Over a Gentle Slope in the South China Sea

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Last modified ~~April 14, 2022~~
Submitted to: Nonlinear Processes in Geophysics

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46 **Abstract**

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Four oceanographic moorings were deployed across the South China Sea continental slope near 21.85°N, 117.71°E, from May 30 to July 18, 2014 for the purpose of observing high-frequency nonlinear internal waves (NLIWs) as they shoaled across a rough, gently sloping bottom. Individual waves required just two hours to traverse the array and could thus easily be tracked from mooring-to-mooring. In general, the amplitude of the incoming NLIWs tracked the fortnightly tidal envelope in the Luzon Strait, lagged by 48.5 hours, but were smaller than the waves previously observed to the southwest near the Dongsha Plateau. The type a-waves and b-waves were observed, with the b-waves always leading the a-waves by 6-8 hours. Most of the NLIWs were remotely generated, but a few of the b-waves formed locally via convergence and breaking at the leading edge of the upslope-propagating internal tide. Waves incident upon the moored array with amplitude less than 50 m and energy less than 100 MJ m⁻¹ propagated adiabatically upslope with little change of form. Larger waves formed packets via wave dispersion. For the larger waves, the kinetic energy flux decreased sharply upslope between 342 m to 266 m while the potential energy flux increased slightly, causing an increasing ratio of potential-to-kinetic energy as the waves shoaled. None of the waves met the criteria for convective breaking. The results are in rough agreement with recent theory and numerical simulations of shoaling waves.

70 **1 Introduction**

71 Considerable field work has now been dedicated to observing and understanding
72 the very large amplitude, high-frequency nonlinear internal waves (NLIW) in the
73 northeastern South China Sea (SCS). It has now been well established that the
74 waves emerge from the internal tide which is generated by the flux of the barotropic
75 tide across the two ridges in the Luzon Strait [Buijsman et al., 2010a, 2010b; Zhang
76 et al., 2011]. Both tidal conversion and dissipation are high around the ridges
77 [Alford et al., 2011], but adequate energy survives to escape the ridges and
78 propagate WNW across the sea. As they do so, the internal tides steepen nonlinearly
79 until eventually the NLIW are formed [Farmer et al., 2009; Li and Farmer, 2011;
80 Alford et al., 2015; Chang et al., 2021a]. The longitude where this takes place
81 depends on the details of the forcing and stratification but based on satellite
82 imagery it is not until at least 120° 30'E, roughly 50 km west of the western (Heng-
83 Chun) ridge [Jackson, 2009]. This longitude is hypothesized to be the minimum
84 distance/time required for the internal tide to nonlinearly steepen and break, or
85 perhaps the first point where tidal beams intersect the sea surface west of the
86 western ridge. Once the NLIW have formed, they propagate WNW across the deep
87 SCS basin with remarkably little change of form [Alford et al., 2010; Ramp et al.,
88 2010]. Once the waves start to shoal on the continental slope however, roughly
89 between 1000m to 150m depth, the changes become quite dramatic. Wave
90 refraction due to the shallower depth and changing stratification tends to align the
91 wave crests with the local topography. Incident NLIWs which were initially solitary
92 may form packets via wave breaking or dispersion [Vlasenko and Hutter, 2002;
93 Vlasenko and Stashchuk, 2007; Lamb and Warn-Varnas, 2015]. Some very large
94 waves may split into two smaller waves [Small 2001a, 2001b; Ramp, 2004]. When
95 the wave's orbital velocity exceeds the propagation speed, usually between 300m -
96 150m depth, the largest waves may break and form trapped cores that transport
97 mass and nutrients onshore [Farmer et al., 2011; Lien et al., 2012, 2014; Rivera-
98 Rosario et al., 2020; Chang et al., 2021b]. Still farther onshore where the upper
99 layer thickness exceeds the lower, the depression waves are transformed into
100 elevation waves [Orr and Mignerey, 2003; Duda et al., 2004; Ramp et al., 2004; Liu et
101 al., 2004]. The elevation waves presumably continue propagating WNW towards
102 shore and dissipate in shallow water, but observations to the west of this point are
103 scarce.

104
105 Two types of NLIWs, called a-waves and b-waves, have been repeatedly observed, a
106 parlance first coined by Ramp et al. [2004]. Based on the Asian Seas International
107 Acoustics Experiment (ASIAEX) results, the a-waves consisted of rank-ordered
108 packets that arrived at the same time every day and were generally larger than the
109 b-waves, which were usually solitary and arrived one hour later each day. It has
110 subsequently been shown via longer data sets that the timing is not universal, and
111 that b-waves may sometimes be larger than a-waves [Alford et al., 2010; Ramp et al.,
112 2010]. It is now recognized that the a-waves are generated in the southern portion
113 of the Luzon Strait and the b-waves to the north [Du et al., 2008; Zhang et al., 2011;
114 Ramp et al., 2019]. The b-waves are subject to massive dissipation over the shallow

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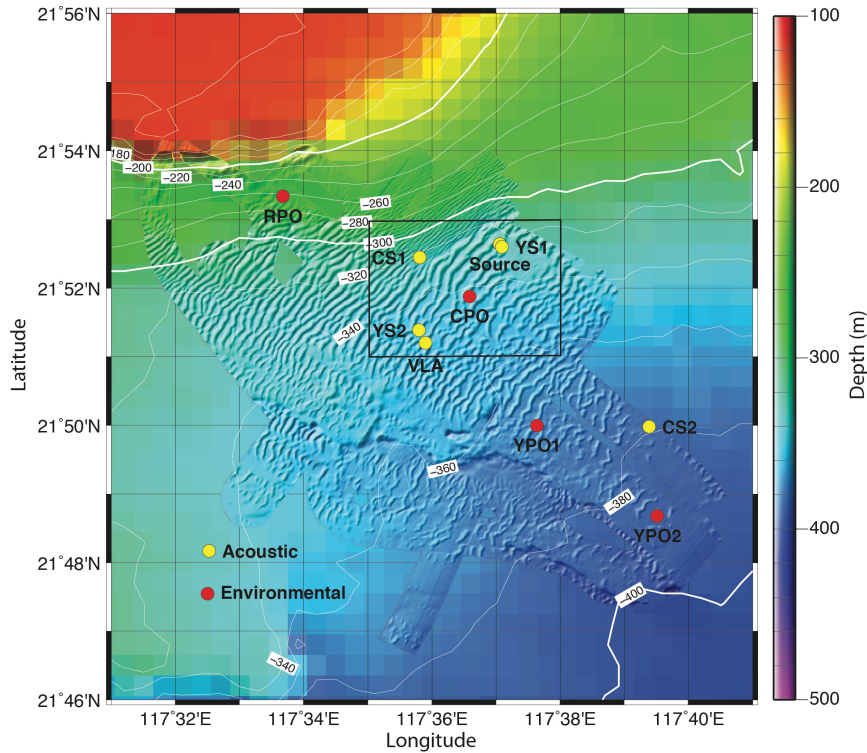
116 northern portion of the western (Heng-Chun) ridge [Alford et al., 2011] but the a-
117 waves are not. The distinction matters because the energy and propagation
118 direction of the trans-basin waves incident on the continental slope determines how
119 they behave as they shoal. These differences are explored further in this paper.
120

121 The present study was motivated by the discovery of large ($h > 15\text{m}$, λ order 350m)
122 undersea sand dunes on the sea floor along a transect southeastward from 21.93°N,
123 117.53°E in the northeastern South China Sea [Reeder et al., 2011]. Subsequent
124 multi-beam echo surveys (MBES) during 2013 and 2014 revealed that the dunes
125 occupy at least the region spanning 21.8 to 21.9°N and 117.5 to 117.7°E (Figure 1).
126 This region is on the continental slope slightly northeast of the Dongsha Plateau.
127 The bottom slope in the dunes region is relatively slight with respect to steeper
128 bottom slopes progressing both offshore and onshore from the dune field. The sand
129 dunes are of interest due to their impact on shallow-water acoustic propagation,
130 and their interaction with shoaling internal tides and NLIWs traveling WNW up the
131 slope. The acoustic issues are addressed in other papers emerging from the
132 program [Chiu and Reeder, 2013; Chiu et al., 2015]. Oceanographic questions of
133 interest include: 1) How are NLIWs transformed as they shoal over a gentle slope
134 between 388m and 266m over the continental slope? 2) What are the physical
135 mechanisms responsible for this transformation? and 3) How does the increased
136 bottom roughness in the dune field affect energy dissipation in the shoaling internal
137 tides and NLIWs, relative to other locations? Geophysical problems of interest
138 include: 4) What, if any, is the role of the NLIW in sediment re-suspension and dune
139 building? 5) What determines the spatial scales of the dunes? and 6) Why are the
140 dunes located where they are, and why are they not observed elsewhere?
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142 This paper addresses how the high-frequency nonlinear internal waves were
143 transformed under shoaling, while the NLIW dissipation and role in the dune-
144 building process will be addressed in separate works [Helfrich et al., 2022]. The
145 data and methods are described in section 2, the NLIW arrival patterns and their
146 relation to the source tides in section 3, and the wave transformations and energy
147 conservation in section 4. A summary and conclusion section follows.
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149 **2 Data and Methods**

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151 An array of four oceanographic moorings were deployed across the continental
152 slope from 21.81°N, 117.86°E (386 m) to 21.89°N, 117.56°E (266 m) during May 31
153 to June 18, 2014 (Figure 1, Appendix A). The moorings labeled YPO2, YPO1, CPO,
154 and RPO were separated by 4.10, 3.30, and 5.69 km respectively corresponding to
155 wave travel times of 36.5, 30.3, and 56 min between moorings. Temperature and
156 salinity were sampled at 60s intervals. Instrument spacing ranged from 15 m to a
157 maximum of 30 m in the vertical to resolve internal wave amplitudes. Currents at
158 RPO were sampled using three downward looking 300 kHz ADCPs moored at 27 m,
159 105 m, and 184 m depth which provided coverage of the entire water column except
160 the upper 20 m. Currents at CPO were also sampled using three 300 kHz ADCPs, one



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Figure 1. Locator map for the Sand Dunes 2014 field experiment. This paper primarily concerns the environmental moorings indicated by the red dots, although temperature from the “source” mooring is also used. The area within the black box is expanded in Figure 2.

downward-looking unit moored at 15 m depth, and an up/down pair at 264 m depth. Since the range of these instruments was nominally 100 m, there was an unsampled region spanning roughly 115 – 164 m depth at mooring CPO. Currents at YPO1 and YPO2 were sampled using one 75 kHz and one 300 kHz ADCP. The 75 kHz instruments were mounted downward looking in the top syntactic foam sphere at 20 m depth. The 300 kHz instruments were also mounted downward looking in cages at 300 m depth. The 300 kHz instruments burst-sampled for 20 s every 90 s, while the 75 kHz instruments sampled once per second and were averaged to 90 s intervals during post-processing. These sampling rates were adequate to observe the shoaling NLIWs with no aliasing. A fifth mooring labeled “source” on roughly the same isobath as CPO (Figure 1) sampled temperature only from 27 to 267 m.

179 This mooring was targeted for the same “trough” in the sand dune field as CPO to
180 examine along-crest acoustic propagation. It additionally proved useful to identify
181 the precise phasing and orientation of the internal wave crests in the along-slope
182 direction.

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184 **3 Results**

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186 *3.1 The Nature of the Dunes*

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188 The stage is set by a zoomed-in view of the study region showing the seafloor sand
189 dunes as depicted by the MBES data (Figure 2). A change in the bottom slope forms
190 a very clear line of demarcation between lower (4 m) dunes with shorter (100 m)
191 wavelength and the larger (10-15 m) dunes with longer (260 m) wavelength. Dunes
192 in these regions were nearly sinusoidal. Farther down the slope in water > 360m
193 depth, the dunes were “parted” meaning the trough widths were much greater than
194 the crest widths. Mooring RPO was located in the first region with steeper slope,
195 CPO was in the second region of smaller slope and large sinusoidal dunes, and
196 moorings YPO1 and YPO2 were in a region with similar mean bottom slope but
197 parted dunes. Repeat MBES surveys indicated that during 2013-14, the dunes were
198 stationary to within the accuracy of the surveys. For purposes of this paper, the
199 most important fact about the bottom is the sharp, clear change of bottom slope
200 across the white dotted line (Figure 2) from $1:35 = .03 = 3\% = 2.0^\circ$ over the
201 shallower part to $1:160 = .006 = 0.6\% = 0.3^\circ$ over the deeper part. These slopes are
202 essential for comparing the observations to theory.

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206 *3.2 Wave Arrival Patterns*

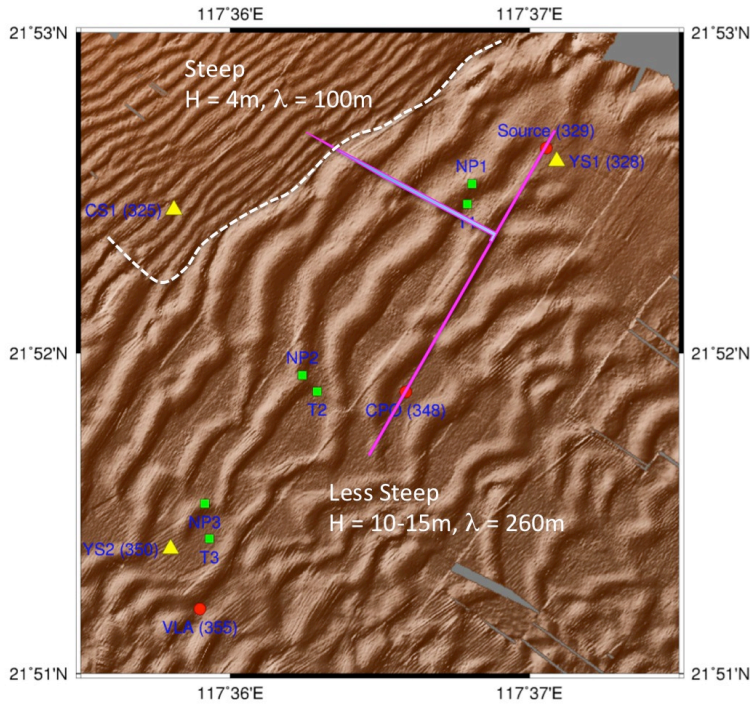
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208 While fine-tuning the NLIW generation problem is beyond the scope of this paper, the
209 fundamental properties of the wave arrival patterns can be understood via comparisons
210 with the generating tide in the Luzon Strait. Having no remote observations during
211 spring 2014, the wave arrival patterns at the sand dunes moored array were compared
212 with the barotropic tidal forcing in the Luzon Strait as obtained from the TPXO7.0 global
213 tidal model [Egbert and Erofeeva, 2002]. The model output has been shown to be in
214 good agreement with the limited observations available in the Luzon Strait [Ramp et al.,
215 2010] and is thus a good indication of the tidal amplitude and phase at generation.

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217 To begin, all the NLIWs arriving at the moored array were identified using large-scale
218 plots of temperature, salinity, and velocity. The arrivals were then summarized for the
219 entire time series by labeling the displacement of the 20°C isotherm from its mean
220 position at mooring RPO (Figure 3, top). The wave arrivals, as indicated by sharp
221 downward displacements of the isotherm, fall into two groups or “clusters” of waves each
222 within a fortnightly envelope. The waves were labeled using previous conventions, using
223 lowercase a- and b- for the first cluster and uppercase A- and B- for the second for
224 uniqueness. This nomenclature will be used to refer to individual waves subsequently.

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Figure 2. The sea floor in the study region as observed by a multi-beam echo sounder (MBES) survey during June 2014. The region is delineated by the black box in Figure 1. The dotted white line indicates a sharp change in bottom slope, steeper towards the northwest. The magenta arrow indicates the direction of propagation of the nonlinear internal waves (NLIW) as determined by wave arrival times at moorings CPO and "source" (pink line).

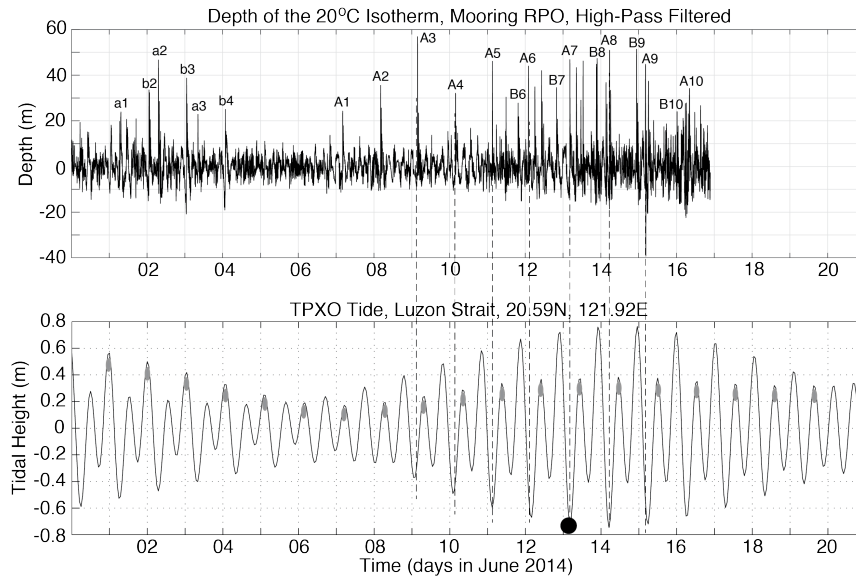
There is no dynamical difference implied by the upper- vs. lowercase names. A total of 21 NLIWs with amplitude greater than 20 m were observed, 13 a-waves and 8 b-waves. When b-waves were present, the waves arrived in b- and a- pairs with the b-wave always leading the a-wave by on average 6.6 hours. The a-waves began arriving earlier in the fortnightly cycle for instance 6/7 to 6/11. The b-waves began arriving later and grew larger later in the fortnightly cycle. With the exception of 6/3 and 6/15, the a-waves were larger than the b-waves.

The RPO wave amplitude time series was then plotted over the Luzon Strait tides (Figure 3, bottom) with the wave amplitudes lagged back by the propagation time from the

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253 *Figure 3. (Top) Time series showing the depth of the 20°C isotherm observed by*
 254 *mooring RPO located at the 266 m isobath (Figure 1). The time series was high pass*
 255 *filtered to separate thermal displacements due to NLIWs from the internal tides and*
 256 *mean (mesoscale and seasonal) flows. The sharp depressions of the isotherm indicate*
 257 *passing NLIWs. The type-a and type-b waves are labeled using lower case for the first*
 258 *fortnight and upper case for the second. (Bottom) Tidal amplitude in the central*
 259 *Luzon Strait from the TPXO global tidal model [Egbert and Erofeeva, 2002], at a point*
 260 *located between Batan and Itbayat Island in the Luzon Strait. The gray ellipses*
 261 *indicate how the major and minor tidal beats switched positions during the neap tide.*
 262 *The black circle indicates the time of the full moon on June 13th. The waves (top panel)*
 263 *have been lagged back by the propagation time from the strait (48.5 hours) to better*
 264 *align with the barotropic tidal envelope in the generating region. The vertical dashed*
 265 *lines show how the lagged a-waves aligned with the ebb tide in the straits.*
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268 source to the mooring. The lag time (48.5 hours) was estimated by making a small
 269 adjustment to the propagation time nearby (50.3 hours) which was calculated using a full
 270 year's data [Ramp et al., 2010]. Several obvious results emerge from this comparison.
 271 First, the NLIW amplitudes at RPO track the fortnightly tidal amplitudes in the Luzon
 272 Strait. The largest waves were generated at spring tide in the strait and no waves at all
 273 were generated during neap. This result is consistent with longer (11 month) time series
 274 obtained over the continental slope to the southwest [Chang et al., 2021a]. Second, the

275 generating tide was mixed, diurnal dominant, with a strong diurnal variation, but only the
276 major beats resulted in NLIWs in the far field. The minor beats and the neap tides were
277 apparently too weak to spawn NLIWs downstream. As a result, just one wave of each
278 type was generated per day, despite the generating tide being semidiurnal. The major and
279 minor beats switched positions during the neap tide, and the wave arrivals at the sand
280 dunes array switched positions accordingly. Third, the lagged a-waves aligned precisely
281 with the major ebb (eastward) tide in the Luzon Strait, in agreement with previous work.
282 This suggests generation by the lee wave mechanism [Buijsman et al., 2010a]. Finally,
283 the b-waves were sometimes aligned well with the major flood tide preceding each a-
284 wave, but we now believe this to be coincidence: The directional histograms (not shown)
285 show the a-waves on average traveling along a path about 24 degrees more northward
286 (294°) than the b-waves (270°), consistent with the primary source for the a-waves being
287 located farther to the south along the Luzon ridge system. The b-waves lead because
288 their generation site was closer to our observation point on the Chinese continental slope.
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290 One example of the daily moored temperature time series at mooring RPO is shown to
291 further illustrate these results (Figure 4). During June 9 to 13, the A-waves arrived at
292 about the same time each day while from June 14-18, they arrived about an hour later
293 each day. This result, that the A-wave arrival times were constant early in the fortnightly
294 tidal cycle but delayed an hour per day as the waves increased in amplitude later in the
295 cycle was consistent with the model results of [Chen et al., 2013]. Wave A7 on June 15
296 was anomalously late by about 2 hours relative to waves A6 and A8. This is attributed
297 to the passing of tropical storm Hagabus on June 14-15 with accompanying strong wind-
298 forced currents and upper ocean mixing. The B-wave arrivals began at about 20:00 on
299 June 13, and were subsequently delayed about an hour per day, similar to the
300 corresponding A-waves (Figure 4). The difference in the arrival times between the B-
301 waves and the A-waves was 6:30, 8:25, 6:15, and 5:50 on June 14-17 respectively. Wave
302 B7 was not delayed by the storm, which provides further evidence for different
303 propagation paths for the B-waves vs. the A-waves. On June 16-18 two A-waves of near
304 equal amplitude arrived about 2 hours apart. These “double A-waves” appeared over the
305 slope only near spring tide in the Luzon Straits, and the second one has been designated
306 by a prime. The origin of these waves is unclear. We speculate that the new A' waves
307 originated from a different (third) source in the Luzon Straits that is only active under
308 maximum barotropic forcing. More observations in the source region are needed to
309 understand the wave generation issues, including this double a-wave phenomenon.
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311 3.3 Wave Transformation Over the Slope

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314 Many significant wave transformations were observed between the 386 m (YPO2)
315 and the 266 m (RPO) isobaths over the upper continental slope. Three sections of
316 the record are shown to illustrate different phenomena. The first sequence from
317 June 2 to 6 (Figure 5) evolved out of moderate and decreasing forcing in the Luzon
318 Strait (Figure 3). The observations captured the local steepening and breaking of
319 the tidal front to form b-waves as it shoaled. The internal tides at YPO2 were
320 diurnal and nearly sinusoidal with an amplitude of about 4°C (blue line). The a-

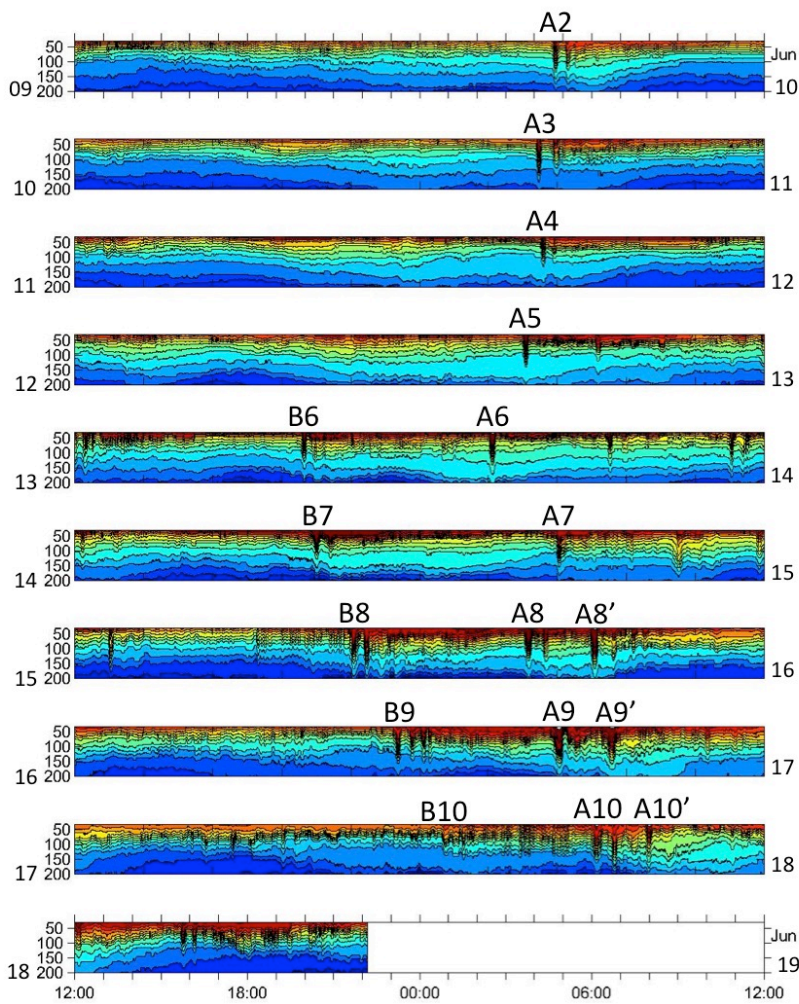
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323 waves were already evident at YPO2, but not the b-waves. Then, beginning at YPO1
324 and continuing to CPO, the leading edge of the tidal front became very steep with a
325 temperature change of $1^{\circ}\text{C} / \text{min}$ for 5 minutes at CPO (black ellipses in Figure 5).
326 This front subsequently broke and formed b-wave packets b2 and b3 observed at
327 mooring RPO. This example thus demonstrates a local b-wave formation process
328 via steepening of the leading edge of the tidal front. This steepening temperature
329 front was due to velocity convergence at the head of the westward-propagating
330 internal tide. The formation of a similar bore-like feature at shallower depths (200
331 m – 120 m) was noted in the ASIAEX data [Duda et al., 2004] but they did not make
332 the connection to b-wave formation. Waves a1 and a2 lost amplitude and formed
333 packets as they shoaled between YPO2 and RPO. This process will be compared
334 with some recent theoretical ideas in the discussion section. Wave a3 was small at
335 YPO2 but gained amplitude as the tide progressed up the slope. This is because the
336 barotropic forcing in the Luzon Strait was weaker on June 5 than on June 2-4 (Figure
337 3). All the waves subsequently disappeared on June 7-8 during neap tide in the
338 Luzon Strait.

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340 The second sequence during June 10-14 shows well developed A-wave packets
341 which originated from moderate but increasing remote forcing (Figure 6). Only A-
342 waves were observed until June 13 when the B-waves started to arrive. Wave B6
343 was weakly perceptible at YPO2 and increased in amplitude across the slope. The
344 temperature fluctuations induced by the A-waves increased across the slope and
345 reached a maximum of 7°C on June 11 at A3. The temperature gradients in the wave
346 fronts were again very steep, $1^{\circ}\text{C} / \text{min}$. The number of waves per packet increased
347 towards shallower water, most clearly in waves A2, A3, and A4. Two extraneous
348 solitary waves appeared trailing wave A5 on June 13 at CPO and RPO but were not
349 part of the A5 packet structure. Two similar waves appeared the next day trailing
350 wave A6 (Figure 7) and their origin is unclear.

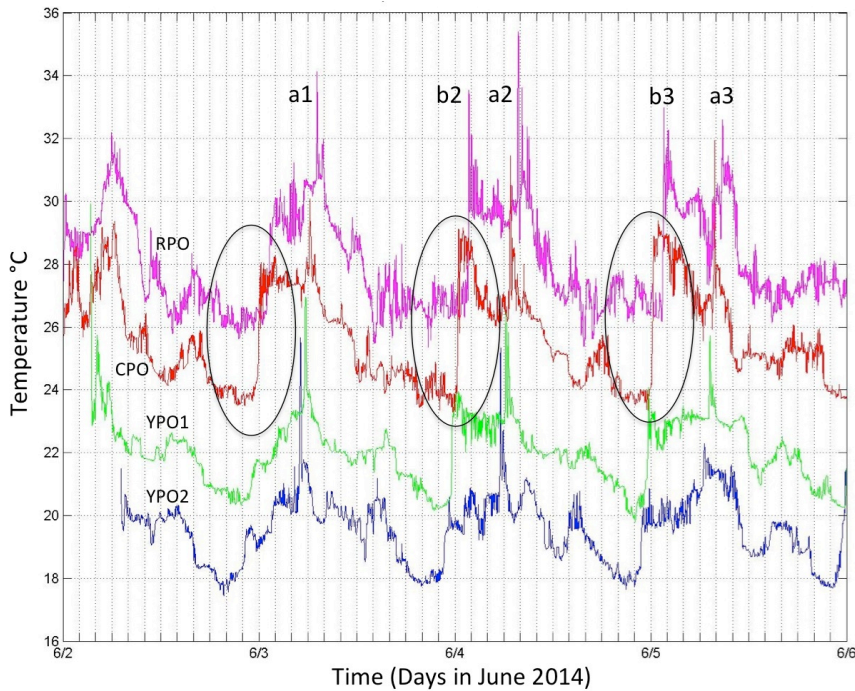
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352 The final sequence from June 14 to 18 was obtained during a period of maximal
353 forcing near spring tide at the source, and a very complicated field of NLIW emerged
354 (Figure 7). The B-waves were large and were evident at all the moorings. Wave B8
355 and B9 were solitary at YPO2 but had many waves per packet by the time they
356 reached RPO. The arrival timing was the same as the locally formed b-waves
357 (Figure 5) suggesting similar dynamics but faster/shorter development
358 time/distance when the forcing at the source was stronger. The A-waves continued
359 to grow at YPO2 during June 14-18. Interestingly, the temperature fluctuations due
360 to the largest waves did not increase monotonically as they traveled up the slope
361 from YPO2 to RPO. This is more clearly seen in a bar graph showing the maximum
362 amplitude of the isotherm of maximum displacement (Figure 8). Smaller waves
363 (June 9-12) gained amplitude as they shoaled. All waves larger than about 50 m
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Figure 4. Temperature contour plots for mooring RPO from June 9 to 19, 2014. Each panel from top to bottom is one day centered on midnight, to capture both the A- and B-wave arrivals. The A-waves were prominent throughout this fortnightly cycle. The B-wave arrivals began on June 13, five days after the A-waves. The double A-waves (A8'-A10') arrived only during June 16-18. This and similar plots were used to label the waves in Figure 3.

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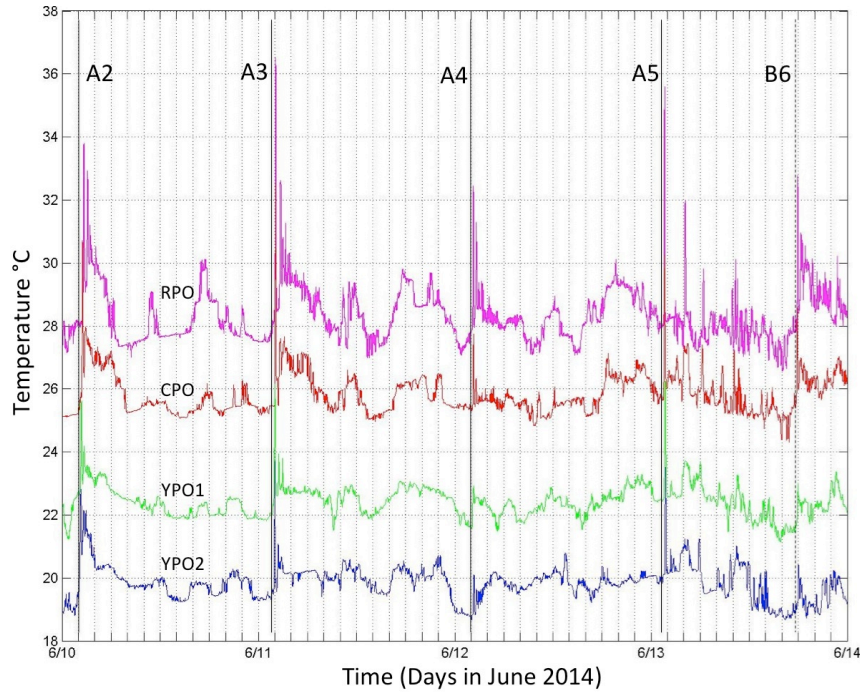
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379 *Figure 5. Temperature vs. time during June 2-6 at all four moorings across the*
380 *continental slope. The observations are from 75m, 79m, 97m, and 99m from moorings*
381 *RPO, CPO, YPO1, and YPO2 respectively. Each time series has been offset vertically by*
382 *2 °C for clarity. The black ellipses highlight the region of strong temperature fronts at*
383 *CPO that subsequently broke and formed b-waves at RPO.*

384

385 offshore (June 13-18) lost amplitude as they shoaled, most clearly between CPO and
386 RPO, where the biggest change in bottom depth and slope occurred. This result is
387 consistent with the numerical results of [Lamb and Warn-Varnas, 2015] who also
388 found that smaller amplitude waves continued to gain amplitude into shallower
389 water but the larger waves did not. This fundamental result, that NLIW first gain
390 amplitude and then lose it as they shoal, is consistent with EKdV theory [Small,
391 2001; Vlasenko et al., 2005]. Note that all the wave amplitudes (Figure 8) were
392 smaller than those observed previously over the continental slope 44, 87, and 145
393 km to the southwest [Ramp et al., 2004; Lien et al., 2014; Chang et al., 2021a; Ramp
394 et al., 2022]. This is because, as seen in hundreds of satellite images (typified by
395 Figure 9), the NLIWs have maximum amplitude in the region just north of the
396 Dongsha Plateau near 20°N decreasing both northward and southward from there.
397 Along-slope observations have also shown a reduction in the upslope energy flux

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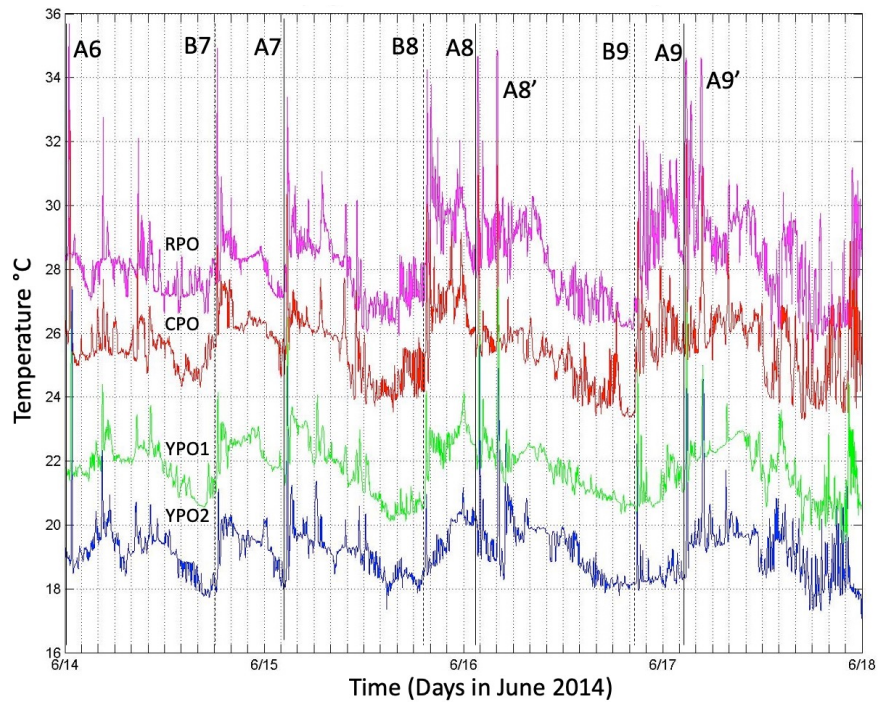
402 *Figure 6. As in Figure 5, except during June 10-14, 2014. In this plot, the time series*
 403 *have additionally been shifted relative to YPO2 by the propagation time between*
 404 *moorings so that individual waves line up. The lag times used are 36.5 min for YPO1,*
 405 *66.8 min for CPO, and 122.8 min for RPO.*

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407 off-axis towards the northeast [Chang et al., 2006]. The Sand Dunes site is near the
 408 northeastern extremity of the wave crests as viewed in the imagery: a bit farther to
 409 the northeast the waves vanished. A practical ramification of this is that the
 410 undersea sand dunes were located in a region where the forcing due to encroaching
 411 NLIWs was not maximal. Other factors such as the bottom slope and sediment
 412 supply must also play an important role in determining the dune formation location.

413

414 The double A-wave phenomenon mentioned earlier (Figure 4) was again evident in
 415 Figure 7. These waves differed from the smaller waves trailing A5 and A6 in that
 416 they were already well-developed by the time they arrived at YPO2. As in Figure 6,
 417 many waves which were solitary at YPO2 formed packets as they crossed the array.
 418 Waves B9, A9, and A9' can be clearly seen in the satellite ocean color imagery
 419 (Figure 9). The timing of the imagery at 0310 was conveniently just as wave A9 was
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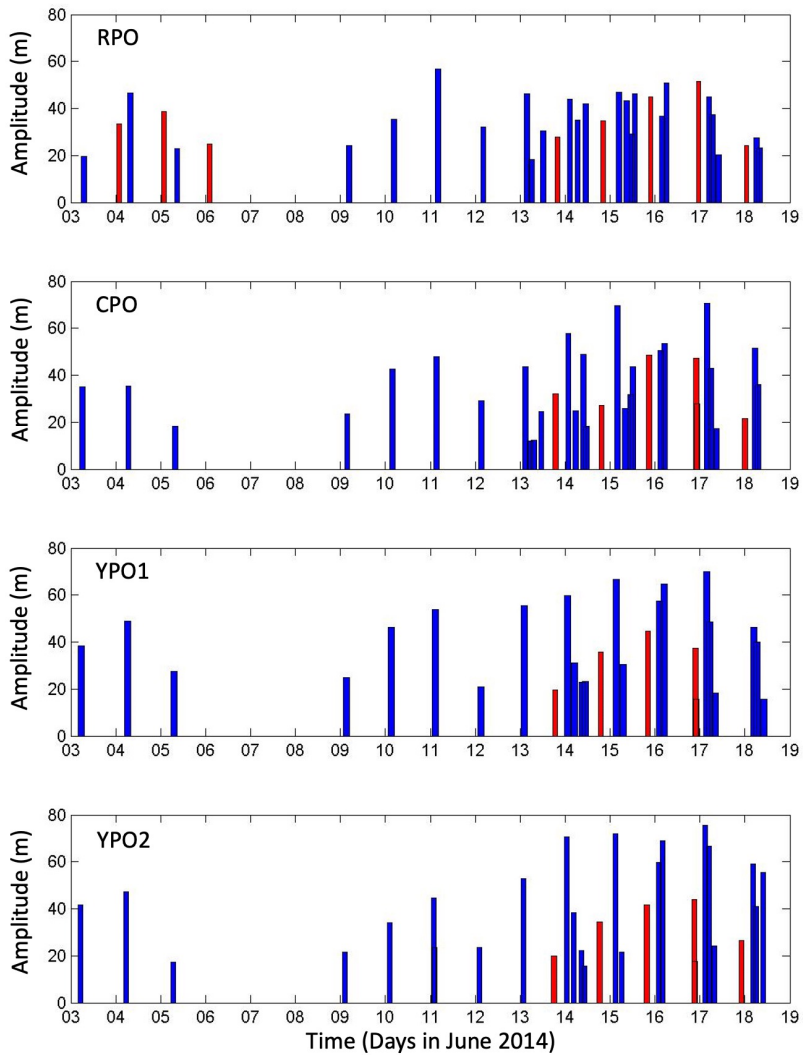


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Figure 7. As in Figure 6 except for June 14-18.

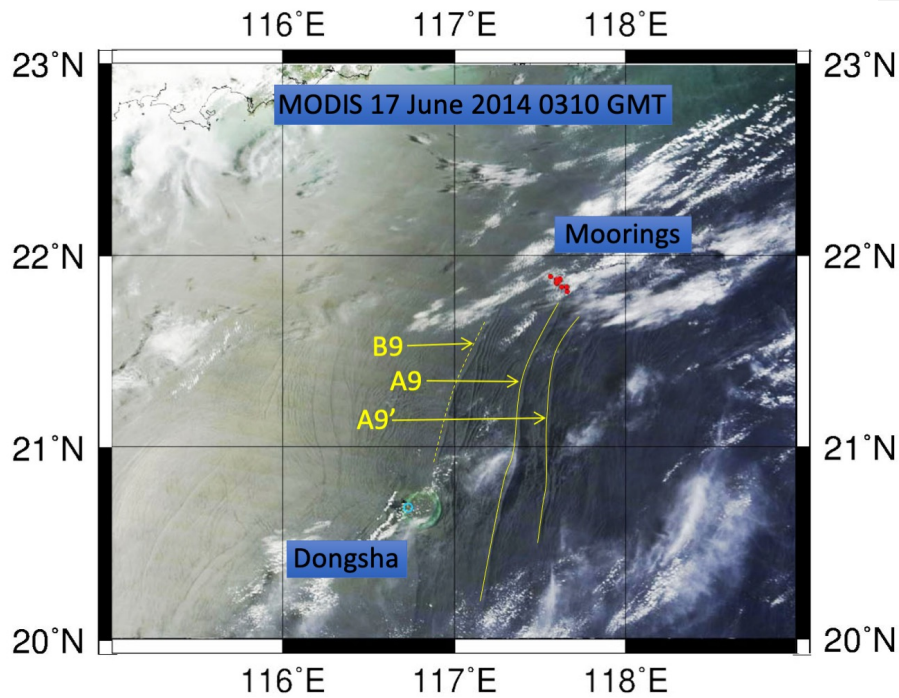
impacting mooring YPO2. The B-wave packets and solitary nature of A9 and A9' are easily seen in the image.

Two examples of velocity and temperature across the slope are shown to illustrate the difference between weakly and strongly forced waves. Mooring YPO1 is not shown since it was very similar to mooring YPO2 (Figure 10). The weaker case begins at YPO2 on June 3-4 (Figure 10, column 1) which shows a clear a-wave near 0530 but no b-wave. Wave a2 was observed towards the rear of the northwestward-propagating internal tide (blue near the surface). The a-wave was traveling NW near the surface and in the opposite direction in the lower water column, with a nodal point near 100 m. While not obvious in temperature, the velocity plots show a weak second wave about 20 min behind the lead wave forming a 2-wave packet. By mooring CPO (column 2), located 7.3 km away, the leading edge of the internal tide had steepened to form a sharp front in both velocity and temperature near midnight on June 3. There was strong convergence in the upper



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Figure 8. Bar graph of wave amplitudes across the slope. The amplitudes were calculated as deviations of the 20 °C isotherm from its mean position. The a-waves are indicated by blue bars and the b-waves by the red.

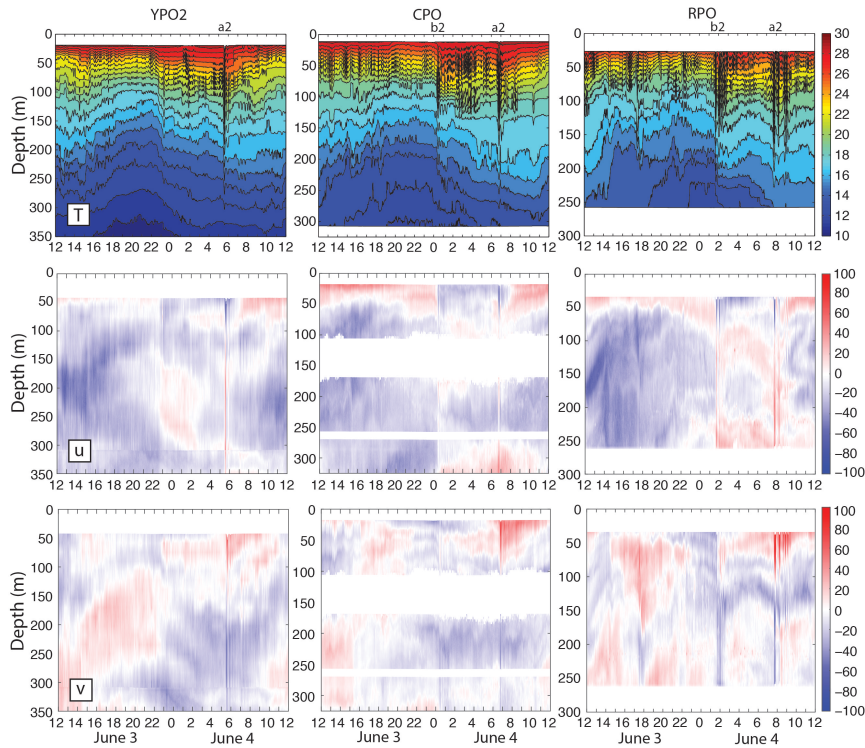


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450 *Figure 9. A sea surface ocean color image obtained at 0310 on June 17, 2014 from the*
 451 *Moderate Resolution Imaging Spectroradiometer (MODIS). The Sand Dunes moorings*
 452 *are indicated by the red dots. The site of the former ASIAEX and WISE/VANS mooring*
 453 *S7 is indicated by the yellow triangle. The surface signatures of NLIWs B9, A9, and*
 454 *A9' are indicated by the yellow arrows. Wave A9 was impinging upon mooring YPO2 at*
 455 *this moment, as seen in Figure 7.*

456

457 50 m with eastward flow (red shades) ahead of the front and westward flow (blue
 458 shades) behind it. A solitary b-wave appeared on this convergent front which was
 459 absent at YPO2. Wave a2 at CPO looked similar to YPO2, perhaps slightly stronger.
 460 By mooring RPO, 5.7 km and 80 m farther up the slope (column 3), the b-wave
 461 increased in amplitude and formed a 2-wave packet, and the leading a-wave
 462 spawned a 4-wave packet. These waves were particularly clear in the v-component
 463 since the waves refracted towards the north as they propagated up the slope (Figure
 464 1). The nodal point remained near 100 m for all the leading waves. Note that the
 465 background internal tide (most easily seen in the deep water) was diurnal at
 466 moorings YPO2 and CPO but became more semidiurnal at RPO. This indicates the
 467 presence of a locally generated tide at RPO where the bottom slope was steeper than
 468 at the other moorings farther offshore. In fact, the bottom slope at YPO2-CPO



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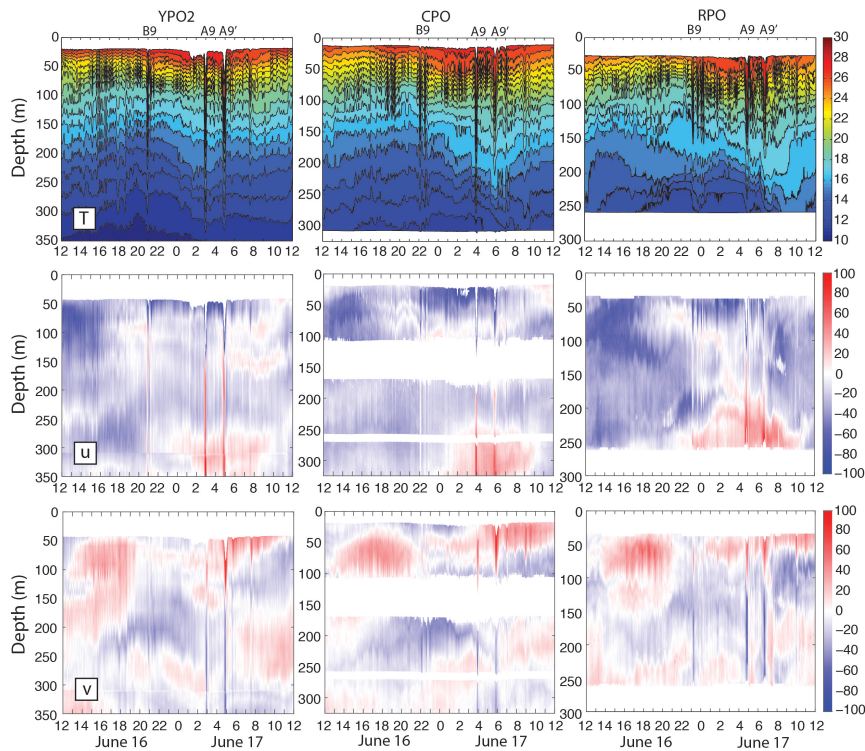
Figure 10. Temperature (top), u-component of velocity (middle) and v-component of velocity (bottom) from 3-4 June 2014 from moorings YPO2 (left), CPO (center), and RPO (right). The wave propagation time between moorings was 67 min from YPO2 to CPO, and 56 min from CPO to RPO. Positive (u, v) represents (east, north) respectively. White space at mooring CPO indicates regions not sampled by the three ADCPs. These data were obtained during a period of moderate and declining tidal forcing, see Figures 3 and 5 for context.

479 (Figures 1, 2 right of the dotted white line) was critical to the diurnal tide while the
480 slope at RPO (left of the dotted white line) was critical to the semidiurnal tide. The
481 interaction of the tidal currents with the bottom is maximal where the slope of the
482 tidal beams parallels the bottom and this likely contributes to the different nature of
483 the sand dunes offshore vs. onshore of the dotted white line (Figure 2). At all
484 moorings, there was only one westward surface internal tide per day. The b-waves
485 all emerged at the leading edge of this westward tide, while the a-waves emerged
486 towards the rear, and this clear velocity signature represents another way to
487 distinguish the two types of waves. The two wave arrivals were separated by 6:20

488 on this day. The strongest bottom velocities were down-slope (southeast) and were
489 greater in the NLIW than in the internal tide.

490
491 The strong example (Figure 11) shows that unlike the previous example, both the B-
492 wave packet and the A-wave packet had already formed by mooring YPO2 on June
493 16-17. (Remember there is no dynamical significance to upper vs. lower case a, b:
494 the lettering is chosen to remain consistent with the nomenclature established in
495 the earlier figures and refers to the first and second cluster.) The waves were
496 traveling in the same direction as the June 3-4 waves, but had a deeper nodal point
497 located near 120-130 m. The A-wave in this case was a double A-wave mentioned
498 earlier. These resembled individual waves rather than a packet in the usual sense.
499 The two waves A9 and A9' were about the same amplitude: on this day the first
500 wave (A9) was slightly larger, but the opposite was true the day before (not shown).
501 The A9' wave was slightly wider than the A9 wave. This may be due to constructive
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Figure 11. As in Figure 10, except for June 16-17, 2014. These data were obtained during a period of strong tidal forcing, see Figures 3 and 7 for context.

509 interference with the tail of wave A9 which was just two hours ahead of it. Wave B9
510 formed a 2-wave packet at CPO (column 2) and a 3-wave packet at RPO (column 3).
511 Wave A9 formed a 2-wave packet between moorings CPO and RPO. As before, the u-
512 component shows the B-wave was coming off the leading edge of the westward
513 surface tide (eastward bottom tide). The A9 wave grew out of the middle of the tide
514 and the A9' wave emerged from the trailing edge of the same westward internal
515 tide. The surface westward velocities exceeded 97 cm s^{-1} , 162 cm s^{-1} , and 153 cm s^{-1}
516 at YPO2, CPO, and RPO respectively. The eastward bottom velocities exceeded 20
517 cm s^{-1} , 85 cm s^{-1} , and 80 cm s^{-1} respectively. The smaller lower layer velocities
518 below the nodal point were consistent with a thicker lower layer and with theory
519 [Lamb and Warn-Varnas, 2015]. The strongest bottom velocities outside the waves
520 were about half the wave velocities. Clearly the strongest bottom velocities
521 observed over the upper continental slope were generated by the passing NLIWs,
522 although these high velocities were very brief compared to the internal tide.
523 Referring once again to Figure 8, the B-wave (just before midnight on June 16)
524 started at YPO2 with just over 40 m amplitude and grew shoreward across the shelf.
525 In contrast, the much larger A-waves just after midnight on the 17th started out
526 with 70 – 75 m amplitude at YPO2 and lost amplitude across the shelf. This is
527 consistent with the earlier discussion surrounding Figure 10.

528
529 Many ordinary internal waves can be seen in Figure 11 in between the nonlinear
530 waves. These waves were likely generated by tropical cyclone Hagabus which
531 passed over the array on June 14-15 with winds exceeding 25 m s^{-1} .

532
533 On June 16 a packet of convex mode-2 waves appeared from 1500-2100 centered
534 near 60 m and extending from 50 to 100 m depth (Figure 11, bottom row). These
535 waves strengthened upslope from YPO2 to RPO and trailed the double-A waves
536 from the day before (not shown). There looked to be about 6 waves in the mode-2
537 packet at mooring RPO. All three of the double-A waves on 16, 17, and 18 June had
538 this feature associated with them. The observation is consistent with [Yang et al.,
539 2009, 2010] who observed mode-2 waves trailing mode-1 waves in the ASIAEX
540 region nearby and attributed this to the adjustment of shoaling mode-1 waves.
541 These observed wave transformations are now discussed further below in light of
542 the theory for shoaling solitary waves.

544 **4 Discussion**

546 *4.1 Theoretical Framework*

547 In this section, the observed NLIW characteristics are compared with laboratory and
548 numerical studies to determine what kind of changes might be expected as the waves
549 shoal over the sand dunes region. The possibilities include adiabatic shoaling, dispersion,
550 breaking, and conversion to waves of elevation. The latter may be easily ruled out for
551 this study since this only happens when the nonlinear coefficient α from the KdV
552 equation changes sign, which typically takes place between 100 – 120 m depth over the
553 Chinese continental shelf [Hsu and Liu, 2000; Orr and Mignerey, 2003; Liu et al., 2004].

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555 Even accounting for some temporal variability due to the local internal tides, this “critical
556 point” where the upper- and lower-layer depths were equal was always well inshore of
557 the sand dunes region.

558 The wave progression WNW from deeper to shallower water may be conveniently
559 framed in terms of the two regions demarcated by the dotted white line in Figure 2.
560 Moorings YPO1, YPO2, CPO were all located in the region where the mean bottom slope
561 was $.006 = 0.6\% = 0.3$. Mooring RPO was in the region where the bottom slope was $0.03 =$
562 $3\% = 1.7$ degrees. The bottom slope is considered gentle when it is less than $0.03 =$
563 1.7° [Grimshaw et al., 2004; Vlasenko et al., 2005; Lamb and Warn-Varnas, 2015;
564 Rivera-Rosario et al., 2020]. Dynamically speaking then the mean bottom slopes in the
565 sand dunes region ranged from weak to practically flat. Under these conditions, the
566 response of shoaling NLIWs depends primarily on three factors: the bottom depth, wave
567 amplitude, and thermocline depth [Small, 2001; Vlasenko and Hutter, 2002; Lamb, 2002;
568 Vlasenko and Stashchuk, 2007; Grimshaw et al., 2014; Lamb and Warn-Varnas, 2015;
569 Rivera-Rosario et al., 2020]. Waves can potentially break when wave orbital velocity
570 $u_{max} >$ the propagation speed c [Lien et al., 2014; Rivera-Rosario et al., 2020; Chang et
571 al., 2021b] and

$$572 \quad a_m > (H_b - H_m)0.4 \quad (1)$$

573 where a_m is the maximum possible wave amplitude, H_b is the bottom depth, and H_m is the
574 upper layer thickness, here approximated by the thermocline depth [Helfrich and
575 Melville, 1986; Helfrich, 1992; Vlasenko and Hutter, 2002]. This expression can be used
576 to evaluate the isobath where a wave of given amplitude will break, or alternatively, to
577 determine the wave amplitude necessary for wave breaking at a given isobath. For the
578 Sand Dunes data set, these criteria were examined for moorings CPO in region 1 and
579 RPO in region 2. The depth of the 23°C isotherm was used to estimate the thermocline
580 depth at both moorings. The undisturbed isotherm depth, determined by time-averaging
581 the low-pass filtered data, was similar at both moorings, 60 m at CPO and 57 m at RPO.
582 Substituting these values in (1) shows that a wave amplitude of 112 m would be required
583 at CPO for wave breaking to occur. Moving on to RPO, the required amplitude for wave
584 breaking there would be about 84 m. Comparing with the observed wave amplitudes at
585 CPO and RPO (Figure 8), all the observed wave amplitudes were less than the above
586 criteria, and no wave breaking events are expected in this array. Some combination of
587 adiabatic shoaling and packet formation via wave dispersion is more likely instead.
588

589 Using this guidance, the temperature and velocity structure at site RPO is studied in
590 greater detail for three examples: a statistically common a-wave (Figure 12), a very
591 large a-wave (Figure 13) and a b-wave (Figure 14). For wave A3 on June 11 (Figure
592 12), which typifies A-waves between June 3-13, the wave was symmetric in both
593 velocity and temperature with no sign of back-side steepening. The wave amplitude
594 was 57 m, and the maximum orbital velocity was 1.04 m s^{-1} and was located near
595 the surface. This was much less than the local phase speed of 1.60 m s^{-1} . The
596 opposing lower layer velocity was order 0.75 m s^{-1} commensurate with the thicker
597 lower layer. Such bottom velocities were commonly observed and are easily enough
598

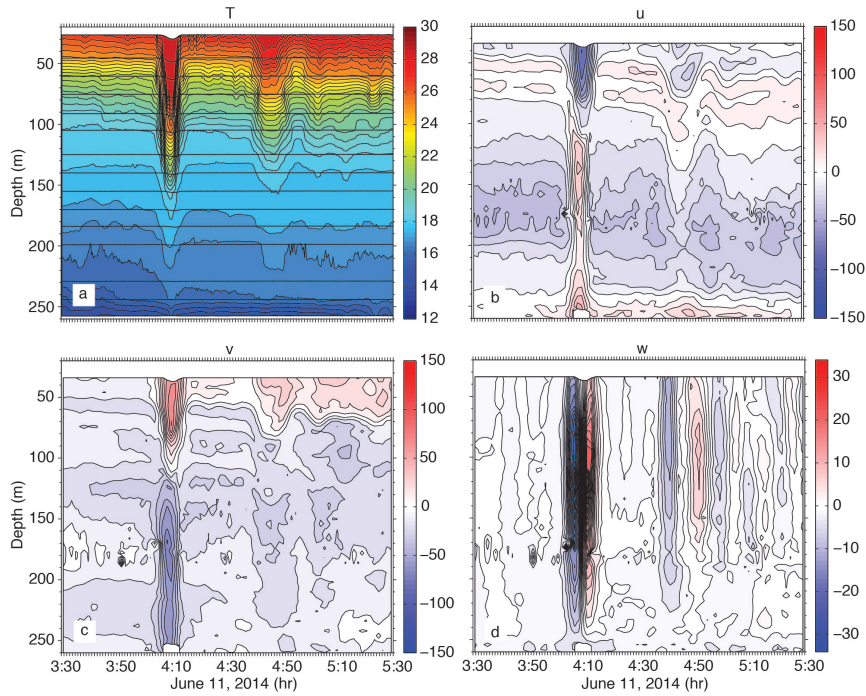
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600 to produce both bedload and suspended sediment transport among the dunes
601 [Reeder et al., 2011]. The w-profile was nearly symmetric at $\pm 0.25 \text{ m s}^{-1}$, downward
602 ahead of the wave and upward behind it, with the maxima located near mid-depth.
603 One or possibly two trailing waves were observed: the first was centered near 4:48
604 and had vertical velocities of $\pm 0.8 \text{ m s}^{-1}$ while the second was near 5:00 with
605 vertical velocities of just a few cm s^{-1} . A fourth wave-like feature was observed in
606 the temperature plot near 5:20 but it cannot be discerned in the velocity structure.
607 To summarize, wave A3 consisted of a primary wave and 2-3 trailing waves about
608 30 min behind. The wave was symmetric in velocity and temperature with no sign
609 of breaking or trapped core formation.

610
611 The largest wave observed was wave A9 on June 17. This wave showed several
612 characteristics of breaking or near-breaking waves (Figure 13). The back side of the
613 wave was steeper than the leading side, and the jagged temperature contours in the
614 wave core were indicative of breaking and/or mixing. A “pedestal” was starting to
615 form behind the wave as described by [Lamb and Warn-Varnas, 2015]. Several
616 more smaller depression waves were emerging from the “pedestal.” The velocity
617 contours were likewise asymmetric and showed a subsurface maximum near 60-70
618 m which was about 0.20 m s^{-1} greater than the surface. This is typical of waves with
619 trapped cores [Lien et al, 2012, 2014; Lamb and Warn-Varnas, 2015]. The
620 maximum near-surface velocity was 1.55 m s^{-1} , which was close to the local phase
621 speed (1.60 m s^{-1}). It is possible that the surface velocities above 20 m depth were
622 slightly larger but were not observed. At site CPO, this same wave had a maximum
623 velocity of 1.80 m s^{-1} , also very close to the local phase speed. The vertical velocities
624 were actually smaller than wave A3, at -12 and $+20 \text{ cm s}^{-1}$ with at least two and
625 possibly more of the trailing depression waves visible as down/up pairs. To
626 summarize, this wave appears to be about to break or just starting to break,
627 however, this wave was the exception rather than the rule: only one such wave was
628 observed. It is possible that the trailing double-A waves A8’ and A9’ might also meet
629 these criteria, however their form was distorted by interference from the trailing
630 packet of the leading A8 and A9 waves two hours earlier, making their
631 characteristics difficult to discern. The South China Sea NLIW amplitudes in June
632 are near their maximum values observed in July and August [Chang et al., 2021a]. It
633 is thus unlikely that breaking waves are ever prevalent in the sand dunes region.
634 This situation contrasts with a similar depth range farther southwest, where larger
635 waves were already actively breaking at the 300 m isobath [Chang et al., 2021b].

636
637 It is worth noting that subsurface velocity maximum in the wave may be caused by
638 phenomena other than wave breaking. Tropical cyclone Hagabus passed over the
639 array on June 14-15 and forced strong near-surface currents which opposed the
640 wave velocities. This was especially obvious on June 15 (not shown) when
641 westward currents at 80 m depth in wave A7 exceeded the surface currents by over
642 0.80 m s^{-1} at RPO and by over 1.00 m s^{-1} at CPO. This likely explains why wave A7
643 arrived 2 hours late with respect to waves A6 and A8 (Figure 4). The storm also left
644 behind a surface mixed layer 40 m deep which lingered to the end of the record.
645 This means all the largest waves forced near spring tide propagated into a region

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650 *Figure 12. a) temperature, b) u-component of velocity (positive east), c) v-component*
651 *of velocity (positive north), and vertical velocity (positive up) for wave A3 on June 11,*
652 *2014. This rank-ordered packed with a symmetrical leading wave typifies most of the*
653 *type-a waves observed during the experiment.*

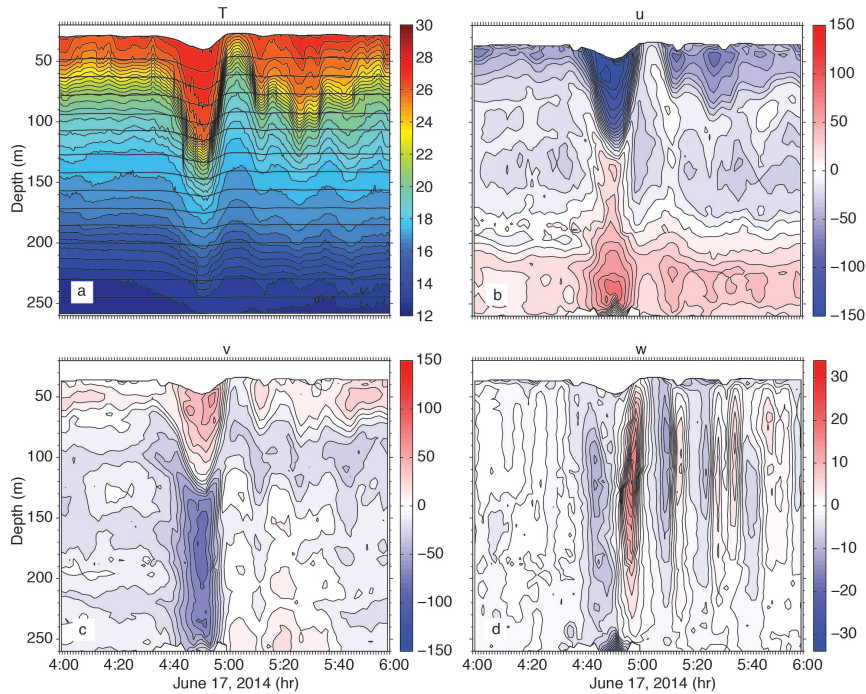
654

655 with an unusually deep surface mixed layer. The effect of this is to severely limit
656 wave breaking [Lamb, 2002]. In fact, the scenario described above in the results
657 section rather closely resembles the model results of [Lamb, 2002] when a surface
658 mixed layer was added (their Figure 10). The shoaling solitary wave in the model
659 produced a second trailing solitary wave, followed by the dispersive tail of mode-1
660 depression waves, followed by a packet of mode-2 waves. The observations
661 reported here closely resembled this pattern not only on June 16-18, but also on
662 June 3-5 trailing waves a1 and a2.

663

664 We conclude that most of the packets that formed as the waves traveled up the
665 slope from YPO2 to RPO were formed by dispersion rather than wave breaking.
666 Rotational effects seem locally unimportant, given that the packets formed in just
667 two hours while the local inertial period was 32 hours. Rotation may have played a

668



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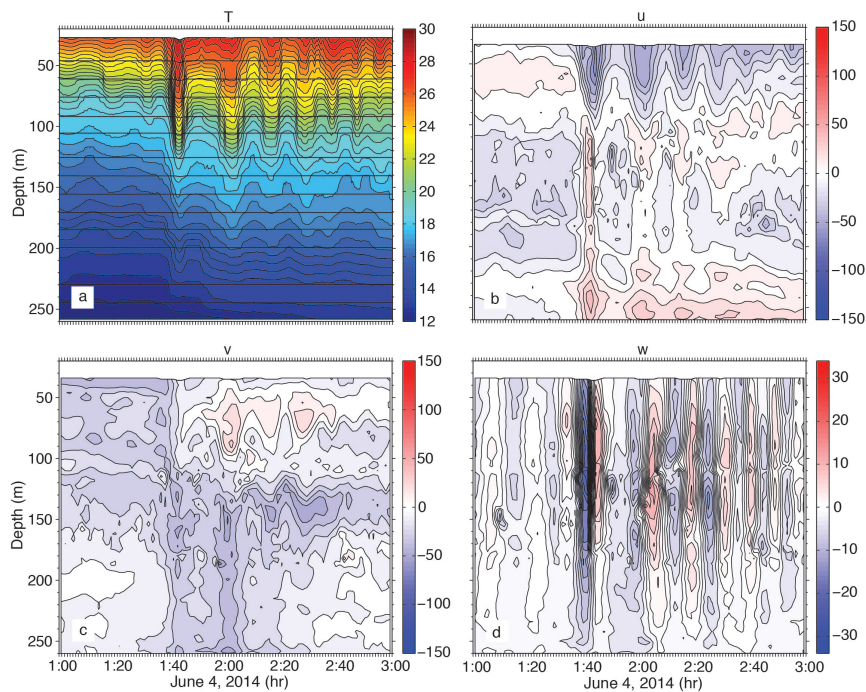
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671

672 *Figure 13. As in Figure 12, but for wave A9 on June 17, 2014. The steepening back side*
673 *and subsurface velocity maximum suggest breaking or imminent breaking.*

674

675 role farther offshore, establishing the initial perturbations (inertial gravity waves)
676 that then grow and become a trailing packet as the waves shoal [Grimshaw et al.,
677 2014]. This effect could not be investigated without observations in deep water.
678 Trailing undular bores of the sort modeled by [Grimshaw et al., 2014] by including
679 rotation were not observed, but are likely not observable since in the real ocean, the
680 waves arrive periodically and the trailing undular bores would be destroyed by each
681 subsequent arriving NLIW before they have a chance to develop. It is most likely
682 then an imbalance between nonlinearity and dispersion that causes the new trailing
683 waves to form [Vlasenko and Hutter, 2002; Lamb and Warn-Varnas, 2015]. The
684 large lead ISW in the Sand Dunes array never split in two, but rather slowly
685 decreased in amplitude as energy was transferred to the dispersive tail. Phenomena
686 such as wave splitting and breaking likely took place inshore of the sand dunes
687 array in the vicinity of the 150 m isobath, as was observed previously at the ASIAEX
688 site nearby.
689



690
 691 *Figure 14. As in Figure 12, except for wave b2 on June 4, 2014. This example typifies*
 692 *waves formed locally by breaking of the tidal front between moorings YPO and RPO.*
 693

694 The situation for the locally formed b-waves (b2-b4) was completely different.
 695 These waves were non-existent at YPO2 but formed well-defined, evenly spaced
 696 packets by the time they reached RPO (Figure 14). For wave b2 on June 4, six waves
 697 can be clearly seen in T and w, with most all the horizontal velocity in u, that is these
 698 waves were traveling westward. The amplitude of the lead wave was about 40 m,
 699 the near surface velocity 60 cm s^{-1} westward, and near-bottom velocity 40 cm s^{-1}
 700 eastward. The waves were formed all at once by the collision and breaking of the
 701 westward internal tide with the off slope propagating eastward tide. This is a
 702 different mechanism than that described for shoaling ISWs in the literature.
 703

704 4.2 Energy and energy flux

705
 706 The data set provides an opportunity to observe how the horizontal kinetic (HKE)
 707 and available potential (APE) energy in the high-frequency nonlinear internal waves
 708 changes as the waves propagate up a gentle slope. In turn, the energy pathways
 709 provide some insight to the dynamics underlying the wave transformation process.

710 The theoretical expectation for linear and small-amplitude nonlinear internal waves
711 is that the energy will be equipartitioned for freely propagating long waves away
712 from boundaries. This is not the case however for finite amplitude nonlinear,
713 nonhydrostatic internal solitary waves whose KE typically exceeds the PE by a
714 factor of 1.3. This result was found theoretically via exact solutions to the fully
715 nonlinear equations of motion [Turkington et al., 1991] and has also been noted
716 observationally [Klymak et al., 2006; Moum et al., 2007]. Thus, the KE is expected to
717 slightly exceed the PE for the waves arriving at mooring YPO2. For shoaling NLIW
718 however, the flux of PE theoretically exceeds the flux of KE which causes the PE to
719 exceed the KE in shallower water [Lamb, 2002; Lamb and Nguyen, 2009]. This is
720 because the flux of PE remains nearly constant while the KE flux decreases as the
721 upper- and lower-layer thicknesses become more equal. Shoaling waves observed
722 in the Massachusetts Bay displayed this property [Scotti et al., 2006]. Thus, a shift
723 from greater KE to greater PE might be expected as the waves shoal from YPO2 to
724 RPO, although it depends on the details of the wave amplitude, stratification, bottom
725 slope, etc.

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726
727 To compute the energies and energy fluxes from moorings, time series of density
728 and velocity which are uniform in space and time are required. Moorings RPO and
729 CPO had good coverage of temperature and salinity in the vertical (Appendix A)
730 however moorings YPO1 and YPO2 sampled temperature only. Two methods to
731 compute the density at YPO1 and YPO2 were explored. The first used a constant
732 salinity (34.42, the vertical average from a nearby CTD cast) paired with the
733 observed temperature at each sensor to compute density. This method assumes
734 that most of the density variability comes from the temperature fluctuations rather
735 than salinity. The second method used the salinity profiles from all the CTD casts
736 taken during the cruise to compute a mean T/S curve, which was then used as a
737 look-up table to determine the salinity to use with each observed temperature. The
738 CTD casts were all within 12 km of each other and were thus treated as a time
739 series. The profiles fell into two groups, namely before tropical storm Hagabus
740 passed by on June 14, with little-to-no surface mixed layer, and after the storm when
741 the mixed layer was about 40-50 m deep. Thus, two mean T/S curves were actually
742 used, one from before the storm and one after. The benchmark for these methods
743 was to compare the density calculated using the T/S curves with the actual density
744 calculated using the observed salinity on moorings RPO and CPO. The APE
745 computed using the mean T/S curve was found to agree much better with the
746 observations than the APE computed using a constant value for the salinity. Both
747 techniques were slight underestimates of the true APE, but the T/S method much
748 less so than the constant method. For this reason, the mean T/S curves were used
749 to compute the density time series, and thus APE for moorings YPO1 and YPO2.

750
751 The observed time series also had velocity gaps of varying severity in the water
752 column due to the range limitations of the ADCPs. Mooring CPO had a mid-depth
753 gap spanning roughly 110-170m and a second smaller gap from 255-265m (see
754 Figures 10 and 11). These gaps were filled using the least squares fit normal mode
755 techniques described in [Nash et al., 2005]. Theoretically as many as seven modes

759 (number of instruments in the vertical – 1) were possible, but the most stable
 760 results were achieved with just three modes. No attempt was made to fill in the
 761 upper 20 m of the water column where both velocity and temperature were
 762 unsampled by the moorings.

763
 764 Once clean time series were available to operate on, the energies and energy fluxes
 765 were computed from the data via established techniques [Nash *et al.*, 2005, 2006;
 766 Lee *et al.*, 2006]. The baroclinic velocity and pressure fluctuations induced by the
 767 waves were first computed as

$$769 \quad \bar{u}'(z,t) = \bar{u}(z,t) - \bar{u}(z) - \frac{1}{H} \int_{-H}^0 [\bar{u}(z,t) - \bar{u}(z)] dz \quad (1)$$

770
 771 and
 772

$$773 \quad p'(z,t) = g \int_z^0 \rho'(\xi,t) d\xi - \frac{g}{H} \int_{-H}^0 \int_z^0 \rho'(\xi,t) d\xi dz \quad (2)$$

774
 775 where

$$777 \quad \rho'(z,t) = \rho(z,t) - \bar{\rho}(z) \quad (3)$$

778
 779 is the density anomaly with respect to the time-mean density profile. In equations
 780 (1) and (2), the last term satisfies the baroclinicity requirement that the primed
 781 quantities integrate to zero over the entire water column [Kunze, *et al.*, 2002]. Over
 782 bars indicate temporal means. The HKE and APE can then be computed as

$$784 \quad HKE = \rho_0 (u'^2 + v'^2) / 2 \quad (4)$$

$$785 \quad APE = \frac{1}{2} \frac{g^2 \rho'^2}{\rho_0 N^2} \quad (5)$$

786
 787 where ρ_0 is the mean density, g is the acceleration of gravity and N^2 is the buoyancy
 788 frequency.

789
 790 The energy flux due to highly nonlinear internal waves is given by

$$792 \quad \bar{F}_E = \bar{u}'(p' + HKE + APE) \quad (6)$$

793
 794 where the first term on the right is the pressure work and the second and third
 795 terms represent the advection of horizontal kinetic and available potential energy
 796 density [Nash *et al.*, 2012]. For the small amplitude, linear, hydrostatic case the flux
 797 equation is often approximated as the first term only

798

$$\bar{F}_E = \bar{u}' p' \quad (7)$$

800

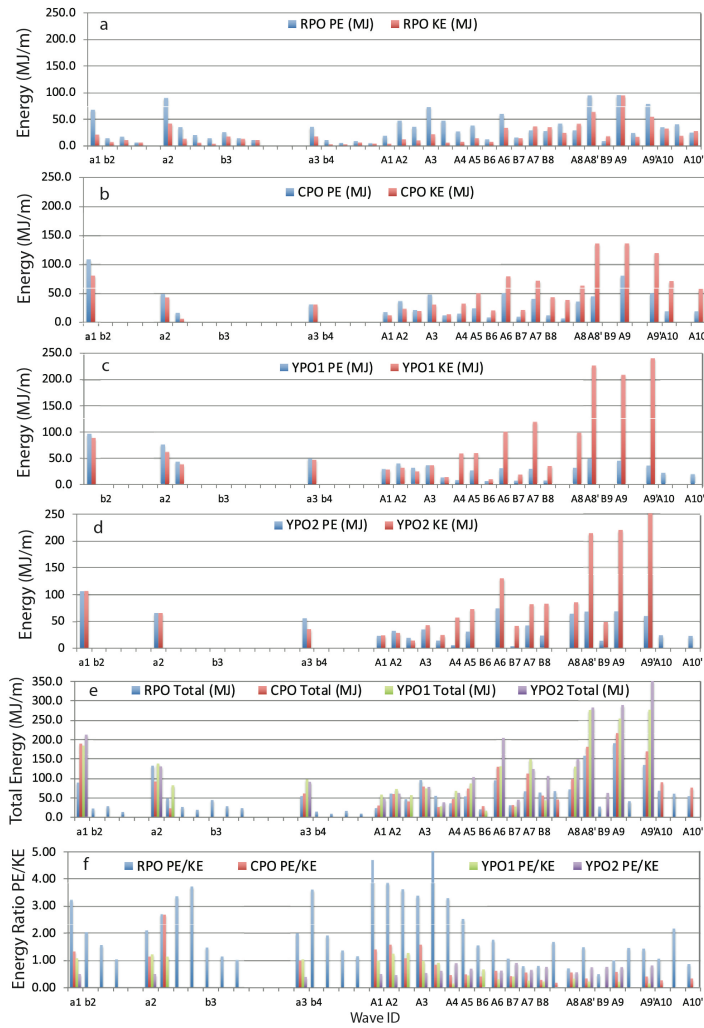
801 but since it is not obvious that this approximation is valid for the strongly nonlinear
802 shoaling waves observed in the sand dunes region, all three terms of the flux
803 equation were computed.

804

805 The resulting changes in the wave energy distribution across the slope depended on
806 the wave amplitude (Figure 15). For waves up to and including A3 on June 11, the
807 APE exceeded HKE offshore and continued to increase up the slope. This is
808 interpreted to mean the waves were still growing and had not yet reached
809 maximum amplitude. Smaller waves can penetrate farther upslope adiabatically
810 than larger waves. Wave A4 was anomalously small for which no obvious
811 explanation has been found. Perhaps the wave was obliterated by the leading edge
812 of tropical storm Hagabus. Starting with wave A5 on June 13, as the remote
813 barotropic tidal forcing continued to increase, the HKE exceeded APE at YPO2 by a
814 factor averaging 1.7 and increased to its maximum value at mooring YPO1. This
815 ratio is even larger than the theoretical expectation of 1.3 [Turkington 1991; Lamb
816 and Nguyen, 2009] and indicates highly nonlinear waves with large amplitudes.
817 Between CPO and RPO, there was a dramatic change when the APE increased and
818 the HKE sharply decreased, resulting in greater APE than HKE at mooring RPO
819 (Figure 15a). The energy ratio at RPO (Figure 15f) was commonly three to four but
820 suddenly decreased sharply with the arrival of wave A6 on June 14 and remained
821 near one for the remainder of the time series. This is attributed to the increased
822 surface mixed layer depth as the tropical storm went by which wiped out the upper
823 ocean stratification and reduced the APE. The total energies (Figure 15e) integrated
824 both vertically and over a wavelength, followed an envelope consistent with the
825 remote tidal forcing and maxed out at around 250 MJ m^{-1} . This was less than half
826 the energy (550 MJ m^{-1}) previously reported over the Dongsha Plateau [Lien et al.,
827 2014] where the maximum observed wave amplitudes exceeded 150 m vs. 80 m
828 here. The total energy appears approximately conserved across the slope for many
829 of the waves as indicated by color bars of approximately equal length (Figure 15e).
830 The losses in HKE were compensated for by the increases in APE, in reasonable
831 agreement with theory and numerical simulations [Lamb and Nguyen, 2009; Lamb
832 and Warn-Varnas, 2015]. For the larger waves however, such as a1, A6, A8', A9, and
833 A9' the total energy decreased upslope (Figure 15e). The HKE was lost much faster
834 than the APE was gained. This is attributed to strong dissipation over the rough
835 bottom in the dune field [Helfrich et al., 2022].

836

837 In the simplest sense the energy flux is just the energy times the group velocity (or
838 phase velocity for non-dispersive waves). Since the phase velocity varied from 1.87
839 m s^{-1} between YPO2 and YPO1 to 1.69 m s^{-1} from CPO to RPO, the flux/energy ratio
840 is expected to vary little across the slope and the flux patterns should resemble that
841 of the total energies. This is indeed the case as seen by comparing the envelope of
842 the curves for the total flux (Figure 16b) and the total energy (Figure 15e). The



843
844

845 *Figure 15. Energy transformations across the slope. The total HKE and APE,*
846 *computed by integrating the wave energy both vertically and horizontally at moorings*
847 *RPO, CPO, YPO1, and YPO2 are shown in panels a-d respectively. The total pseudo-*
848 *energy (HKE + APE) at all four moorings is shown for each wave in panel e, and the*
849 *APE/HKE ratio in panel f.*

850 vertically integrated flux tends to decrease upslope primarily due to the decreasing
851 water depth. Of greater interest is the change in the various terms of equation (6).
852 The pressure work is indeed the largest term but not by much: The PW comprised
853 57%, 56%, 43%, and 52% of the total flux at YPO2, YPO1, CPO, and RPO
854 respectively. The large percentage still remaining was accounted for by the
855 advection of HKE and APE and shows that the waves were indeed strongly
856 nonlinear. The increase in APE with respect to HKE at mooring RPO versus CPO can
857 be accounted for by the change in the fluxes at those moorings (Figure 16a). From
858 CPO to RPO, the kinetic energy flux dropped by 50% (blue line to green line) while
859 the potential energy flux went up slightly (red line to purple line).

860

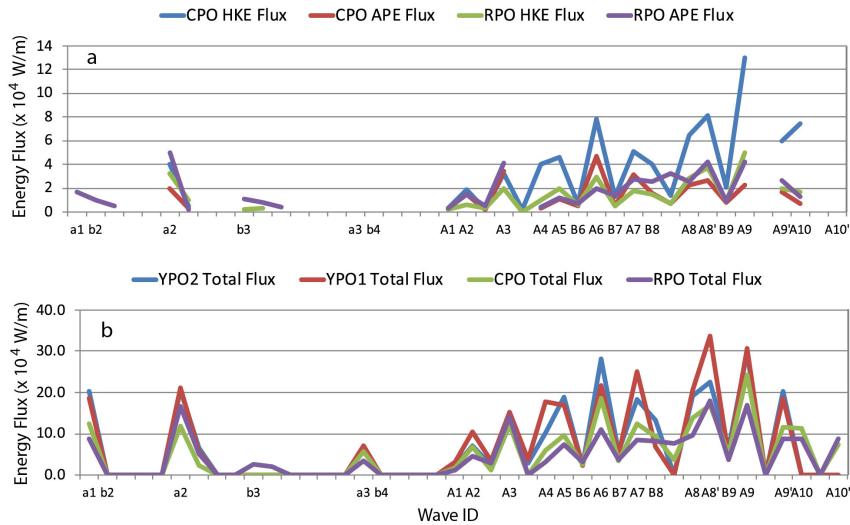
861 **5. Summary and conclusions**

862

863 An 18-day time series of high-resolution velocity and temperature data were
864 obtained at four closely spaced moorings spanning 386-266 m depth on the
865 continental slope 160 km northeast of Dongsha Island in the South China Sea. The
866 experiment was motivated by the need to understand ocean variability and how it
867 interacts with large (15 m) sand dunes on the sea floor. The dominant signal
868 observed consisted of sets of large amplitude nonlinear internal waves (NLIWs)
869 impinging on the continental slope from the southeast. These were in fact the very
870 same waves that impact the Dongsha Island region and have been reported by many
871 previous authors. The “sand dunes” waves however were about 50% smaller and
872 less energetic than the “Dongsha” waves, since the location was near the northern
873 extremity of the wave crests rather than near the main axis of the waves. The mean
874 bottom slope along the sand dunes mooring line was also gentler than farther
875 southwest. While the internal tides are no doubt important to the dune-building
876 process, this paper focuses entirely on the NLIW properties, most especially how the
877 waves were transformed as they shoaled up a very gradual bottom slope. New
878 information gleaned includes the packet formation process, further insights on the
879 difference between a-waves and b-waves, and the energy transformation processes
880 which took place during wave shoaling.

881

882 During the fortnight observed, the a-waves began arriving several days ahead of the
883 b-waves and traveled in a more northerly direction. Once they started arriving, the
884 b-wave always lead the a-wave by 6-8 hours. In any given pair, the a-wave was
885 generally larger, but b-waves generated near spring tide may be larger than a-waves
886 generated near neap. The a-waves generally arrived at the site as 2-3 wave packets,
887 but the b-waves may also form packets as they shoal. The wave generation location
888 and their positioning relative to each other and the internal tide determines the
889 wave classification. The b-waves were located near the head of the upslope internal
890 tide while the a-waves developed more towards the back. The wave arrival patterns
891 rigorously tracked the tidal structure in Luzon Strait, even to the point of shifting by
892 six hours when the strong beat/weak beat pattern reversed in the strait during neap
893 tide. The arrival patterns were consistent with earlier work showing that the a-
894 waves were generated in the southern portion of the Luzon Strait and the b-waves
895 in the north.



896
897

898 *Figure 16. The energy fluxes up the slope for each of the nonlinear internal waves*
 899 *identified in the sand dunes moored array data. a) The kinetic and potential energy*
 900 *flux for moorings CPO and RPO. b) The total energy flux for all four moorings. This is*
 901 *the sum of the kinetic, potential, and pressure work terms.*

Deleted: flux

902
903 A conundrum remains the arrival of two large a-waves with nearly equal amplitude
 904 separated by two hours during the period of maximal tidal forcing, spring tide plus
 905 or minus one day. Additional work is needed to understand the origin of these
 906 waves.

907
908 At least two packet-generating mechanisms were clearly observed. Most a-waves
 909 had already formed in the deep basin by the time they were incident upon the most
 910 offshore mooring, YPO2 at the 388 m isobath. The behavior of these waves
 911 depended on their amplitude: waves smaller than about 50 m and 100 MJ m⁻¹
 912 propagated adiabatically upslope with little change of form. Waves larger/more
 913 energetic than this formed packets via wave dispersion. Wave breaking was not
 914 observed at any time, with the possible exception of the largest wave that was
 915 steepening on the backside at the shallowest mooring, RPO at 266 m depth. The
 916 waves likely break, and/or reflect, inshore of 266 m where the bottom is also
 917 steeper. On the other hand, some of the b-waves were incident on YPO2 while
 918 others were absent at YPO2 and formed while the internal tide shoaled between
 919 YPO2 and RPO. These waves and wave packets were formed by the breaking of the
 920 leading, strongly convergent edge of the upslope-propagating internal tide (not to
 921 be confused with a breaking NLIW). This process took place near mooring CPO on

923 the 342 m isobath. This process occurred just once per day and was most easily
924 discerned by the downslope tidal current near the bottom which was not
925 complicated by upper ocean processes.

926
927 The energy transformations also depended on wave amplitude. For the smaller
928 waves ($E < 100 \text{ MJ m}^{-1}$), the incident APE was greater than the HKE and continued to
929 grow upslope. For the larger waves, the incident HKE was larger than the APE, but
930 the flux of HKE decreased sharply upslope especially between 342m to 266 m, while
931 the flux of APE in that depth range increased slightly, resulting in greater APE than
932 HKE farther onshore. These results are in rough agreement with recent theory and
933 numerical simulations of shoaling waves.

934
935 With the possible exception of one (largest) wave, no breaking NLIWs were
936 observed anywhere in the moored array. This is because neither of the criteria for
937 breaking waves was met: The orbital velocities never exceeded the propagation
938 speed, and wave amplitudes were too small. This situation contrasts with a similar
939 depth range farther southwest, where larger waves were already actively breaking
940 at the 300 m isobath. The more periodic, less turbulent environment presented to
941 the subaqueous sand dune field may be relevant to its formation location along the
942 slope. This and other forcing factors will be taken up in more detail in a subsequent
943 work.

944
945
946

947 **Acknowledgements**

948

949 This work was supported by the U.S. Office of Naval Research (ONR) under grant
950 N000141512464 and by the Taiwan Ministry of Science and Technology (MOST).
951 Wen-Hwa Her (IONTU) and Marla Stone (NPS) led the mooring work at sea. We
952 thank the officers and crew of the research vessels OCEAN RESEARCHER 1, OCEAN
953 RESEARCHER 3, and OCEAN RESEARCHER 5.

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APPENDIX A

Table 1. Mooring and Instrument Locations and Performance												
Mooring	Latitude (north)	Longitude (east)	Bottom Depth (m)	Instrument	Instrument Depth (m)	Start	Stop	Record Length (d)	Sample Interval (s)	Number of Points		
RPO	21 53.334	117 33.676	266			6/1/14	6/18/14	18				
				★ADCP 300 kHz	31				90	17198		
				★ADCP 300 kHz	105				90	17197		
				★ADCP 300 kHz	190				90	17198		
				SBE 37 (TSP)	27, 105, 184, 244				20	76354		
				SBE 39 (TP)	61, 91, 141, 170, 258				10	154792		
				SPE 56 (T)	45, 75, 125, 155, 199, 229				10	154794		
CPO	21 51.879	117 36.587	342			6/1/14	6/18/14	18				
				★ADCP 300 kHz	11				90	16394		
				◆ADCP 300 kHz	263				90	16398		
				★ADCP 300 kHz	269				90	16410		
				SBE 37 (TSP)	43, 109, 169, 230, 307				10	148066		
				SBE 39 (TP)	78, 139, 200, 286				10	148066		
YPO1	21 49.998	117 37.600	372			6/2/14	6/19/14	18				
				✚ADCP 75 kHz	20				90	16537		
				★ADCP 300 kHz	306				90	16537		
				SBE 19 (TSP)	369		6/13/14	12	15	63517		
				SBE 39 (TP)	35, 56, 92, 117, 178, 240				10	148845		
				SBE 39 (TP)	300		6/17/14	16	10	134727		
				SBE 39 (TP)	354		6/10/14	9	10	70620		
				SBE 56 (T)	76		6/8/14	7	10	54078		
				SBE 56 (T)	147, 209, 270, 325				10	148845		
				Star Oddi (TP)	148, 188		6/11/14	10	10	77398		
YPO2	21 48.679	117 39.512	386			6/2/14	6/19/14	18				
				✚ADCP 75 kHz	20				90	16916		
				★ADCP 300 kHz	301				90	16915		
				SBE 39 (TP)	58, 97, 118, 180, 241				10	152252		
				SBE 39 (TP)	37, 354		6/17/14		10	133147		
				SBE 56 (T)	78, 149, 201, 272, 328				10	152252		
Source	21 52.630	117 37.128	328			6/1/14	6/18/14	18				
				SBE 37 (TSP)	26, 86, 147, 208, 268				10	142186		
				SBE 39 (TP)	55, 116, 174, 238, 310				10	1142186		
				★4-m bins down-looking, 30 pings per ensemble								
				◆4-m bins up-looking, 30 pings per ensemble								
				✚16-m bins down-looking, 10 pings per ensemble								

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