



41 and slopes is more variable than in the open ocean (Carter et al., 2005). Diapycnal diffusivity
42 observed on continental shelf and slope can span four orders of magnitude (Gregg and Özsoy, 1999;
43 Nash and Moum, 2001). Internal solitary wave is a kind of nonlinear internal wave, which usually
44 carries a large amount of energy. Numerical simulation results indicate that up to 73% of the internal
45 wave field energy may be in internal solitary waves (Bogucki et al., 1997). Therefore, internal
46 solitary waves propagating to the continental shelf and slope can greatly change the local mixing. A
47 number of researches have been carried out on mixing caused by internal solitary waves on the
48 continental shelf and slope. Observations have shown that the turbulence induced by shear
49 instability at the rear of internal solitary wave sharply increases the mixing (Sandstrom et al., 1989;
50 Sandstrom and Oakey, 1995; Moum et al., 2003; Richards et al., 2013). Mackinnon and Gregg (2003)
51 estimated that 50% of the dissipation in the thermocline occurred during the propagation of internal
52 solitary waves according to their observations. The elevation internal solitary waves propagating
53 near the seafloor enhances mixing, resuspending and transporting materials, which has an important
54 impact on the local ecological environment (Klymak and Moum, 2003; Moum et al., 2007).

55
56 Internal solitary waves are ubiquitous in the northeastern South China Sea (Zhao et al., 2003;
57 Klymak et al., 2006; Xu et al., 2010; Cai et al., 2012; Alford et al., 2015). They are generated by
58 interaction of internal tides and topography in the Luzon Strait and propagate toward Dongsha Atoll,
59 where their energy is dissipated in shoaling. The continental shelf and slope of the northeastern
60 South China Sea is close to the source, so that the amplitude and energy of internal solitary waves
61 in this area are large. The energy dissipation of internal solitary waves occurs most near Dongsha
62 Atoll and its southeastern shelf (Lien et al., 2005; Chang et al., 2006; St. Laurent, 2008).
63 Observations show that high turbulence mainly occurs in the continental shelf region, and the
64 average diffusivity can reach the order of $O(-3)$ $m^2 s^{-1}$, while the diffusivity in the continental slope
65 region is one order of magnitude lower (Yang et al., 2014). When nonlinear internal waves travel
66 cross the continental slope, the waveform changes into different types (Terletska et al., 2020). In
67 this process, mixing is enhanced, and about 30% of the energy dissipation occurs near the seafloor
68 (St. Laurent, 2008). The energy flux of internal solitary waves around the Dongsha Plateau is large.
69 Lien et al. (2005) estimated that, if all nonlinear internal waves break within water depth of 10 m
70 and in a range of 200×200 km^2 centered on Dongsha Plateau, the magnitude of diffusivity can
71 exceed an order of $O(-3)$. In addition, internal solitary waves shoaling near the Dongsha Atoll also
72 dissipate a lot of energy and improve the local mixing efficiency (Orr and Mignerey, 2003; St.
73 Laurent et al., 2011). The water in the northeastern South China Sea can exchange heat with the
74 water in the Pacific Ocean through the Kuroshio, and heat can be transferred to atmosphere through
75 the sea-air interface on the continental shelf as well. Therefore, internal solitary waves are an
76 important link for energy transfer in the South China Sea and play an important role in our
77 understanding of energy transfer between the ocean and climate environment.

78
79 Turbulence in the ocean is patchy and instantaneous. Therefore, it requires extensive observations
80 to accurately evaluate turbulent mixing (Whalen et al., 2012; Waterhouse et al., 2014; Kunze, 2017).
81 Seismic oceanography (Holbrook et al., 2003) has the advantages of wide observation range and
82 high spatial resolution (Ruddick et al., 2009), which is suitable for observing the spatial distribution
83 of turbulent mixing. Sheen et al. (2009) used reflection seismic data to give a diffusivity section of
84 oceanic front in the South Atlantic. Holbrook et al. (2013) comprehensively introduced the



85 theoretical basis for evaluating turbulent mixing from reflection seismic data. Subsequently, a large
86 number of scholars have used the reflection seismic method to study the spatial distribution of
87 turbulent mixing in different ocean regions or turbulent mixing induced by different ocean
88 phenomena (Fortin et al., 2016; Sallares et al., 2016; Dickinson et al., 2017; Mojica et al., 2018).

89

90 In this article, we used two-dimensional seismic data to observe the propagation of internal solitary
91 waves near the Dongsha Atoll, and calculated the spatial distribution of local diapycnal diffusivity
92 to evaluate the impact of internal solitary wave shoaling on turbulent mixing. Section 2 introduces
93 seismic data processing and the method of calculating turbulence mixing parameters. Section 3
94 describes the polarity reversal of internal solitary waves, horizontal slope spectrum and distribution
95 of turbulence diffusivity. In section 4 we analyze the relationship between diapycnal diffusivity and
96 reflection seismic events, and discuss the mechanism of turbulent mixing induced by internal
97 solitary waves. Besides, we compare the mixing scheme with our results. Section 5 gives a summary.

98

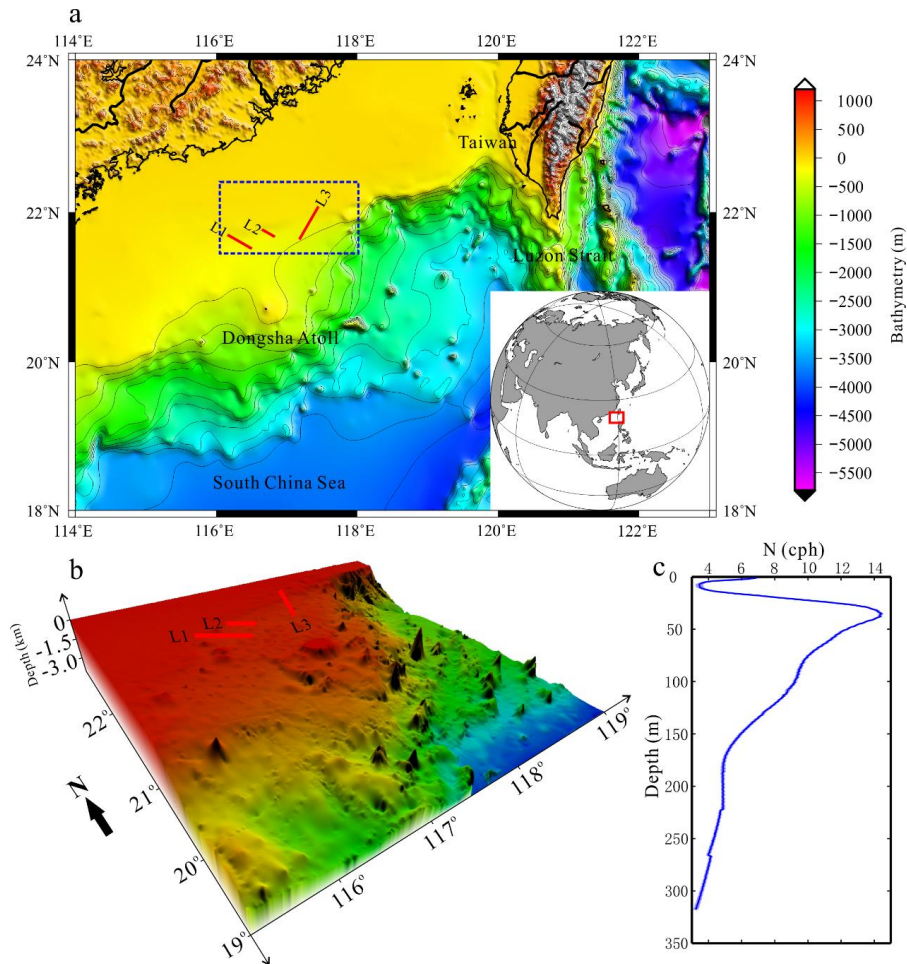
99 **2. Data and methods**

100 **2.1. Seismic data acquisition and processing**

101

102 The water is shallow on the continental shelf and slope near the Dongsha Atoll, so internal solitary
103 waves reach the transition point and their polarity changes from depression to elevation. In the
104 summer of 2009, the Guangzhou Marine Geological Survey (GMGS) set up a two-dimensional
105 seismic observation network in the Dongsha area. We found three internal solitary waves during the
106 polarity reversal process on the L1, L2, and L3 survey lines of the seismic data. The survey lines
107 are shown in Figure 1a, b. The streamer used in the acquisition process has a total length of 6 km
108 and 480 channels, the trace interval is 12.5 m, and the sampling interval is 2 ms. The airgun source
109 capacity is 5080 in³ (1 in=2.54 cm), and the main frequency of the source is 35 Hz. The shot interval
110 is 25 m, and the minimum offset is 250 m. The time interval of shots is about 10 s. Survey lines L1
111 and L2 are the in-lines, which were from the southeast to the northwest. Survey line L3 is a cross-
112 line, which was from the southwest to the northeast. We calculated the mean buoyancy frequency
113 (Figure 1c) of the region around seismic survey lines (latitude range 21.5°-22.5°, longitude range
114 116°-118°, blue box in Figure 1a) by reanalysis temperature and salinity data with a water depth of
115 100-350 m. This depth range matches the observation depth of the seismic data. The hydrographic
116 data are provided by Copernicus Marine Environment Monitoring Service (CMEMS).

117

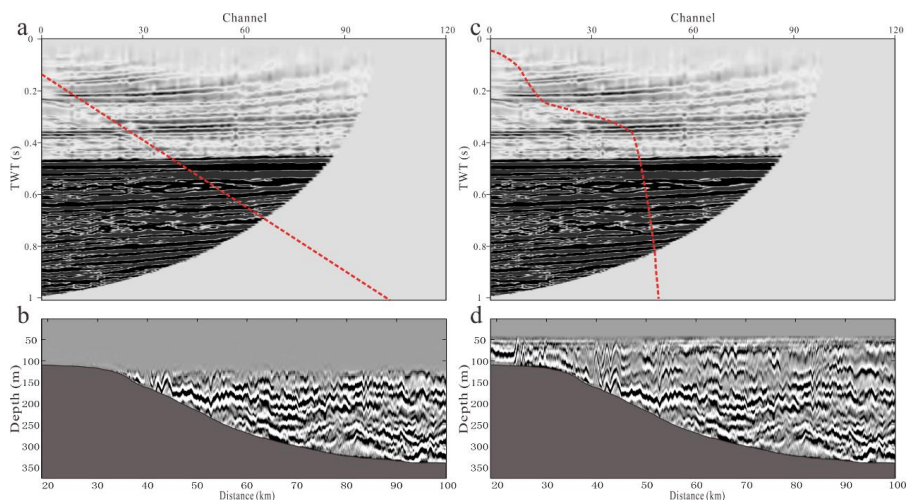


118
119 Figure 1. Bathymetry of the Dongsha area and the locations of seismic survey lines. (a) 2D bathymetry
120 map of the northeastern of South China Sea, with the red lines representing the seismic survey lines. (b)
121 3D bathymetry map around the Dongsha Atoll. (c) The mean buoyancy frequency around seismic survey
122 lines (blue box in (a)) and its 95% confidence interval (blue shadow).

123
124 After a conventional processing of the seismic data, an image of the ocean interior's structure can
125 be obtained. This image can be approximated as a temperature or salinity gradient map of the water
126 column (Ruddick, et al., 2009). The conventional processing of seismic data has 5 main steps,
127 including defining the observation system, noise and direct wave attenuation, velocity analysis,
128 normal moveout (NMO) and horizontal stacking. Then we use a bandpass filter to filter out low-
129 frequency noise below 8 Hz and high-frequency noise above 80 Hz. According to the linear
130 characteristics of the direct wave, we use a median filter to extract the direct wave signal, and
131 subtract it from the original signal to achieve the purpose of attenuating the direct wave.
132 Subsequently, we sorted the seismic data from shot gathers into common midpoint gathers (CMPs).
133 Sound speed is a function of depth and obtained through velocity analysis, and then the NMO is



134 applied to CMPs according to the function to flatten the reflection seismic events of the water
135 column. When NMO is applied, the seismic wave with large offset will be stretched, and the
136 stretched seismic waves need to be cut off. Usually, the default method is to use a linear function to
137 remove the stretched seismic waves (Figure 2a). This may lose a lot of shallow reflection signals
138 (Figure 2b). Bai et al. (2017) used the common offset seismic section to supplement the missing
139 information in shallow water, but the low signal-to-noise ratio of the common offset seismic section
140 cannot guarantee the imaging quality. In order to retain more shallow reflection signal, we used a
141 custom function to cut off the NMO stretch (Figure 2c), thereby satisfying the imaging requirement
142 of the shallow water column (Figure 2d). Finally, the seismic section of the water column can be
143 obtained by stacking the processed CMPs. Due to the shallow water depth, the seismic data is
144 seriously affected by swell noise. We filtered out the components of stacked seismic data in wave
145 number range corresponding to swells in the frequency-wave number domain. A detailed description
146 of the seismic data processing can be found in Ruddick et al. (2009).
147



148
149 Figure 2. Cutting off the stretch of NMO with a linear function (a) and the corresponding seismic section
150 (b). Cutting off the stretch of NMO with a custom function (c) and the corresponding seismic section (d).
151 The red dotted line shows the cut off trace, the right part of seismic data is cut off. The unit TWT of (a)
152 and (b) is the two-way travel time of seismic wave from source to receiver.
153

154 2.2. Diapycnal diffusivity estimates from seismic data

155
156 Klymak and Moum (2007b) found that the horizontal wavenumber spectrum of the vertical
157 isopycnal displacement can be interpreted as the internal wave spectrum at low wavenumbers and
158 the turbulence spectrum at high wavenumbers. The high wavenumber components of spectrum are
159 dominated by turbulence, and the spectral energy follows the $-5/3$ power of the wavenumber. The
160 turbulence part of the horizontal wavenumber spectrum can be expressed by a simplified Batchelor
161 model (Equation 2-1), so the turbulence dissipation \mathcal{E} can be estimated from the observed
162 horizontal wavenumber spectrum. And diapycnal diffusivity can be calculated from Equation 2-2
163 (Osborn, 1980).



164
$$\phi_{\zeta}^T = \frac{4\pi\Gamma}{N^2} C_T \varepsilon^{\frac{2}{3}} (2\pi k_x)^{-\frac{5}{3}} \quad (2-1)$$

165
$$K_{\rho} = \Gamma \varepsilon / N^2 \quad (2-2)$$

166 Where ϕ_{ζ}^T represents horizontal wavenumber spectrum, $\Gamma = 0.2$ is the mixing coefficient, N
167 is the buoyancy frequency, $C_T = 0.4$ is the Kolmogorov constant, ε represents the turbulence
168 dissipation, k_x is the horizontal wavenumber, and K_{ρ} represents the diapycnal diffusivity.

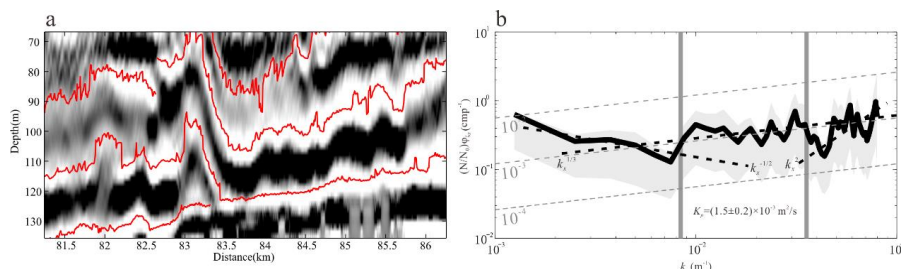
169
170 Observations (Nandi et al., 2004; Nakamura et al., 2006; Sallarès et al., 2009) and simulations
171 (Holbrook et al., 2013) show that the reflection seismic events and isopycnal are spatially consistent.
172 Therefore, the horizontal wavenumber spectrum calculated from the vertical displacement of the
173 reflection seismic events is equivalent to the horizontal slope spectrum that Klymak and Moum
174 (2007b) calculated from horizontal tow measurements. The turbulence dissipation and diapycnal
175 diffusivity can also be calculated from seismic data (Sheen et al., 2009; Holbrook et al., 2013). First,
176 we use the seismic interpretation software to pick up reflection events in the seismic section (Figure
177 3a). Then we calculate the vertical displacement of the reflection events. The vertical displacement
178 is the distance of the reflection events deviate from the equilibrium position in the vertical direction.
179 We take the mean water depth of the reflection events as the equilibrium position. Note that the
180 choice of equilibrium position will not affect the calculation result. The spectral energy ϕ_{ζ}^T of the
181 vertical displacement in the horizontal wavenumber domain can be obtained by Fourier transform.
182 In practical applications, we use the slope spectrum $\phi_{\zeta_x}^T$ instead of the displacement spectrum ϕ_{ζ}^T
183 to distinguish the turbulence subrange from the internal wave subrange. The spectral slope is as
184 follows (Holbrook et al., 2013):

185
$$\phi_{\zeta_x}^T = (2\pi k_x)^2 \phi_{\zeta}^T \quad (2-3)$$

186 This conversion changes the wavenumber power law in the turbulence subrange from $-5/3$ to $1/3$,
187 so that it can be distinguished from the internal wave subrange with $-1/2$ power law ($-5/2$ in the
188 displacement spectrum). In calculating the turbulence dissipation in the seismic section, it is
189 necessary to grid the section and calculate the dissipation in each grid separately. The horizontal
190 grid is set as 5 km, and the grid step 2.5 km. As the water depth in the seismic data is shallow, the
191 reflection seismic events are less in the vertical direction. In order to ensure more than two events
192 in each grid, we set the vertical grid to be 75 m and the grid step 37.5 m. In each grid, we calculated
193 the spectral slope of each event and took the average as $\overline{\phi_{\zeta_x}^T}$. We fitted the averaged spectrum in
194 the turbulence subrange to the Equation 2-1 and calculated the turbulence dissipation ε . To reduce
195 uncertainty, we only calculated the cases with a length >1000 m in each grid. Experiments showed
196 that this length can correctly represent the slope of energy spectra in turbulence subrange (Figure
197 3b). After traversing all the grids, the turbulent dissipation section is obtained, and the diapycnal
198 diffusivity section can be obtained as well according to Equation 2-2. The uncertainty of the



199 turbulence dissipation and diapycnal diffusivity was evaluated by the error between observed
200 average slope spectrum and the fitted Batchelor model. We used a spline smoothing function to
201 smooth the meshing results.
202



203 Figure 3. (a) The reflection seismic events in a grid. (b) The average horizontal slope spectrum (black
204 line). The gray shadow represents the 95% confidence interval. The gray dashed lines represent the
205 diffusivity contour. The black dashed lines represent the spectral slopes in internal wave subrange,
206 turbulence subrange and noise subrange, respectively. The gray vertical lines indicate the boundaries of
207 turbulence subrange.
208

209

210 2.3. Estimating the horizontal wave-induced velocity of internal solitary wave

211

212 We estimated the wave-induced horizontal velocity of internal solitary wave according to the
213 method proposed by Moum et al. (2007). This method requires observation data to satisfy two
214 assumptions: 1) the isopycnal is parallel to the streamline; 2) the internal solitary wave satisfies the
215 KdV equation. Moum et al. (2007) picked the isopycnal from the high-frequency acoustic section
216 and fitted it with the KdV equation. The displacement equation of isopycnal can be obtained, and
217 the derivation of displacement equation is the wave-induced velocity. Seismic data satisfy the first
218 assumption. Although breaking induced polarity reversal of internal solitary waves close the
219 streamlines, it is difficult to record reflection seismic data from those areas with closed streamline
220 at the resolution scale of seismic data. The regional density gradient recorded by the reflection
221 events still exists, and the streamline is parallel to the isopycnal at this time. While areas with closed
222 streamlines are strongly mixed, and the density gradient weakens or even disappears, which cannot
223 be recorded in seismic data. Unfortunately, the internal solitary waves we observed do not satisfy
224 the second assumption. The KdV equation can simulate internal solitary waves with small amplitude
225 and weak nonlinearity, but the polarity reversal of the large-amplitude internal solitary waves we
226 observed cannot be simulated well. Here we did not use theoretical models to fit observations.
227 Although there are studies using theory to successfully simulate the polarity reversal of internal
228 solitary waves (Liu et al., 1998; Zhao et al., 2003;), it is difficult to match theories and observations.

229 We used the picked reflection seismic events to calculate the isopycnal displacement $\eta(x, z)$

230 (Figure 4b). The $\eta(x, z)$ is the distance that reflection seismic events deviate from the equilibrium

231 position, which is determined by the mean depth of two shoulders of one internal solitary wave

232 (Figure 4a). We smoothed $\eta(x, z)$ with a spline function same as that was used for smoothing



233 turbulence dissipation, so that the resolution of wave-induced velocity is consistent with that of
234 turbulence dissipation. Therefore, the stream function can be expressed as (Holloway et al., 1999):

$$235 \quad \Psi(x, z) = c\eta(x, z) \quad (2-4)$$

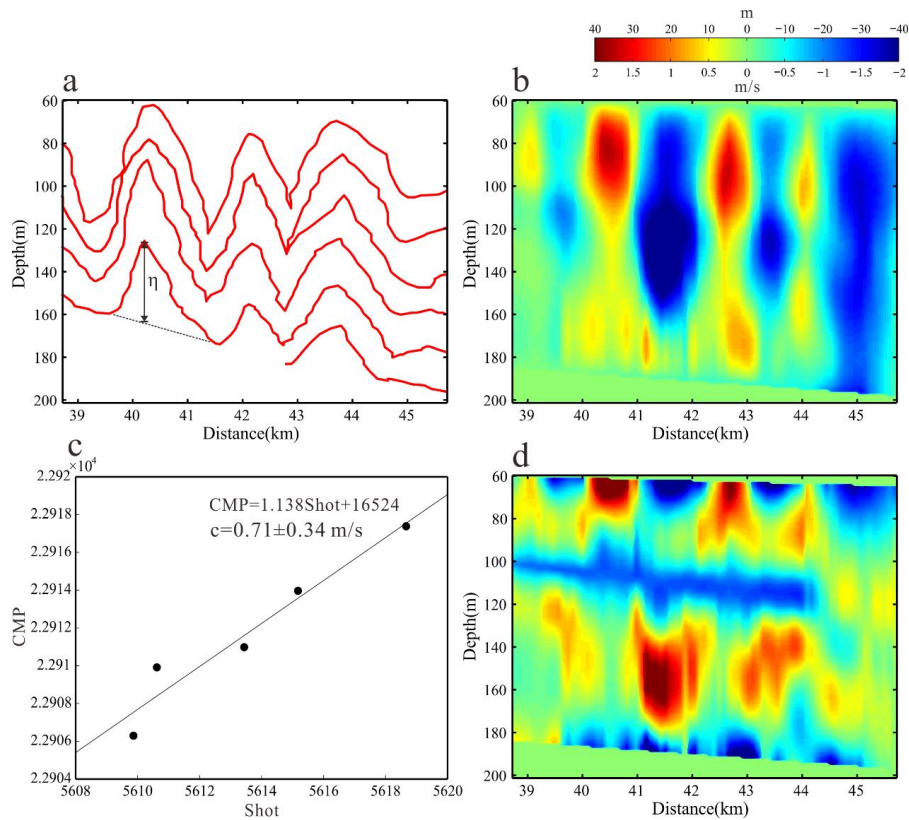
236 where c is the phase velocity of internal solitary waves. The c can be estimated from pre-stack
237 seismic data (Tang et al., 2014, 2015; Fan et al., 2021). The seismic data is redundant, because we
238 have made multiple observations of the same events, which allows us to study the movement of the
239 water column. Specifically, after sorting the seismic data into CMPs (section 2.1), we extract traces
240 with the same offset from CMPs to form common offset gathers (COGs). Multiple COGs can be
241 obtained in the order of offset from small to large. The larger the offset, the lower the signal-to-
242 noise ratio of the data. We selected the first five COGs to ensure the imaging quality. Pre-stack
243 migration of COGs yields COG sections. These COG pre-stack migration sections show images of
244 the same water column at different times. Tracking the change of shot-receiver pairs at a certain
245 reflection point yields the phase velocity (Fan et al., 2021). Figure 4c shows the change of the shot-
246 receiver pairs of internal solitary wave trough in the L1 survey line. The straight line represents the
247 fitting line of the shot-receiver pairs. The average phase velocity of the internal solitary wave during

248 the imaging time is $c = \frac{d_{cmp}}{dt_s} k$, where d_{cmp} is the half of the trace interval, dt_s the time

249 interval of shot, and k the slope of the fitted line. After calculating the flow function according to
250 Equations 2-4, the wave-induced horizontal velocity can be expressed as:

$$251 \quad u(x, z) = \frac{\partial \Psi}{\partial z} \quad (2-5)$$

252



253

254 Figure 4. (a) Schematic of calculating internal solitary wave isopycnal displacement using reflection
 255 seismic events. (b) The isopycnal displacement section of internal solitary wave. (c) Calculating the mean
 256 phase velocity of internal solitary wave by pre-stack seismic data. (d) The wave-induced horizontal
 257 velocity.

258

259 Note that the wave-induced velocity here is in the seismic resolution scale, which can be regarded
 260 as its low-frequency component only. The results are insufficient to characterize the high-frequency
 261 components. But such rough wave-induced velocity is useful, because the purpose of calculating
 262 wave-induced velocity is for the vertical mixing scheme. The wave-induced velocity makes the
 263 resolution scale of the mixing scheme equal to that of mixing parameters estimated from the seismic
 264 data, and the two are comparable. In addition, the error of the wave-induced velocity is mainly
 265 determined by the error of the phase velocity of the internal solitary wave. For internal solitary
 266 waves with polarity reversal, the error of the phase velocity is large, because the phase velocity
 267 gradually decreases when the internal solitary wave is shoaling (Bourgault et al., 2007; Shroyer et
 268 al., 2008). It can be seen from Figure 4c that the shot-receiver pairs do not completely fall on the
 269 fitted line.

270

271 **2.4. Mixing scheme for internal solitary waves shoaling**

272



273 Shoaling and breaking of internal solitary waves on the continental shelf and slope enhance mixing.
274 Vlasenko and Huntter (2002) studied the breaking of internal solitary waves over slope-shelf
275 topography by numerical simulation. In their model, the mixing scheme (PP scheme) proposed by
276 Pacanowski and Philander (1981) was improved, and a vertical mixing scheme for resolving
277 breaking internal solitary waves was given. In this scheme, the vertical turbulence kinematic
278 viscosity and diffusivity are determined by the Richardson-number-dependent turbulence
279 parameterizations. The expression is as follows:

$$280 \quad Ri = \frac{N^2}{u_z^2} \quad (2-6)$$

$$281 \quad \nu = \frac{\nu_0}{(1 + \alpha Ri)^n} + \nu_b \quad (2-7)$$

$$282 \quad \kappa = \frac{\kappa_0}{(1 + \alpha Ri)^n} + \kappa_b \quad (2-8)$$

283 Where u_z is the vertical gradient of horizontal wave-induced velocity, ν is vertical turbulence
284 kinematic viscosity, κ is vertical turbulence kinematic diffusivity. Vlasenko and Huntter (2002)
285 selected the best model parameters after a series of experiments. They are $\nu_0 = 10^{-3} m^2 s^{-1}$,
286 $\nu_b = 10^{-5} m^2 s^{-1}$, $\kappa_b = 10^{-6} m^2 s^{-1}$, $\alpha = 5$ and $n = 1$. Based on this model, they simulated the
287 process of internal solitary wave shoaling and breaking on slope-shelf topography and studied the
288 breaking criterion.

289

290 3. Results

291 3.1. Polarity reversal of internal solitary wave in seismic section

292

293 When one internal solitary wave propagates cross the transition point, it converts from a depression
294 wave to an elevation wave. In the two-layer ocean model, the transition point is defined as the
295 position where the pycnocline is close to the mid-depth (Grimshaw et al., 2010). The three seismic
296 sections in Figure 5 capture the images of internal solitary waves passing the transition point. Figure
297 5a is the seismic section of survey line L1. It shows that the water depth becomes shallower from
298 southeast to northwest, and the bottom slope is steeper between 30-60 km. In the deep-water region
299 of 60-100 km, internal waves are developed, and the reflection seismic events fluctuate obviously.
300 Near the seafloor around 80 km, the reflection seismic events are uplifted and discontinuous,
301 forming a fuzzy reflection area. A mode-1 depression internal solitary wave can be identified at 53
302 km, indicating that the transition point has not been reached yet. The internal solitary wave has
303 reversed polarity in the area of 40 km, and a packet of three elevation waves is formed during the
304 polarity reversal process. The reflection seismic events is continuous here, and no obvious wave
305 breaking is found. Five elevation waves can be identified around 24-37 km, among which four
306 elevation waves at 24 km may be formed continuously, while the elevation wave at 37 km formed
307 later.



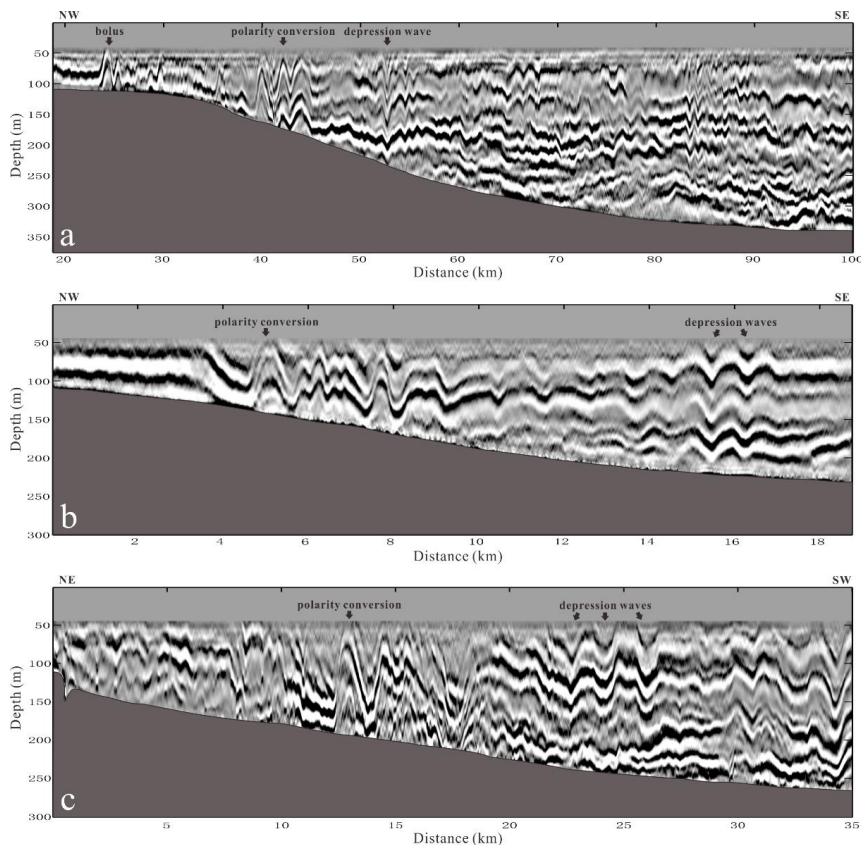
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309 Figure 5b gives another internal solitary wave polarity reversal process captured by the survey line
310 L2. There are two obvious depression waves at 16 km. There are multiple waves with smaller
311 amplitude around 10-15 km. The polarity of internal solitary wave is reversing within 4-8 km. The
312 length of the head wave becomes wider and the slope becomes gentler. The leading wave is followed
313 by a packet of multiple elevation waves. The reflection seismic events are continuous in the whole
314 section.

315

316 L3 is a cross line whose observation direction is perpendicular to survey line L1 and L2 (Figure 5c).
317 There are multiple depression waves with large amplitude around 20-35 km, and the reflection
318 seismic events are continuous. The wave polarity is reversing within 10-20 km, and the reflection
319 seismic events are discontinuous in this region. At 10 km, there is a large-amplitude elevation
320 internal solitary wave, and the wave front is almost parallel to seafloor. There is a large-amplitude
321 depression wave at 17 km, and the wave trough has interacted with topography. The reflection
322 seismic events before 10 km are discontinuous, and the events near the seafloor are fuzzy. It
323 indicates that internal solitary waves break and induce strong mixing during the process.

324



325

326 Figure 5. The seismic sections of survey line L1 (a), L2 (b) and L3 (c). The gray regions in the sections
327 represent seafloor. Internal solitary waves can be clearly seen in all three cases.



328

329 3.2. The horizontal slope spectrum

330

331 We picked the reflection seismic events in the three sections (Figure 7) and calculated the horizontal
332 slope spectrum using the method described in section 2.2. Figure 6 shows the average horizontal
333 slope spectrum of the three sections. We calculated the horizontal slope spectrum of all tracked
334 events and averaged in logarithmic space to determine the wavenumber of turbulence subrange. The
335 turbulence subrange of the survey line L1 section is $0.005\text{-}0.069\text{ m}^{-1}$, as shown by the gray vertical
336 line in Figure 6a. The corresponding wavelength is 15-200 m. The average diapycnal diffusivity is
337 $(7.0\pm 1.2)\times 10^{-4}\text{ m}^2/\text{s}$, which is one order of magnitude larger than the open-ocean value ($10^{-5}\text{ m}^2/\text{s}$).
338 The spectral energy in internal wave subrange is larger than that in turbulence subrange, indicating
339 that the energy is dominated by internal waves. This is confirmed by internal waves in the seismic
340 sections. The difference from Holbrook et al. (2013) is that the calculated horizontal slope spectrum
341 does not include harmonic noise. This may be because the harmonic noise has been removed when
342 we filtered the swell noise. In addition, we have not smoothed the events, so some high wavenumber
343 ranges are reserved. If the events are smoothed, the spectral energy will decrease rapidly in the high
344 wavenumber range (Holbrook et al., 2013; Tang et al., 2019).

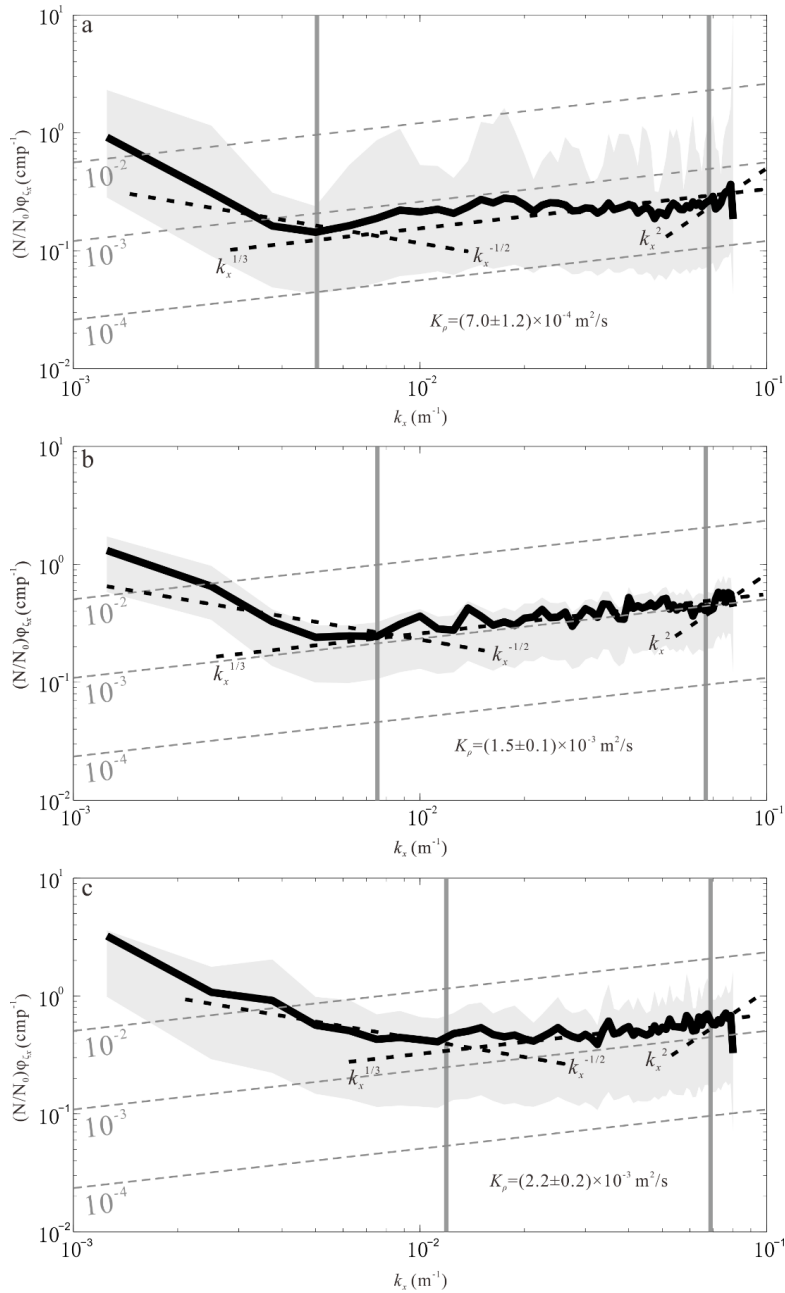
345

346 The horizontal slope spectrum of the L2 section is shown in Figure 6b. The turbulence subrange is
347 $0.008\text{-}0.068\text{ m}^{-1}$, and the corresponding wavelength is 15-133 m. Compared with the survey line L1,
348 the turbulence shifts to a smaller scale. The spectral energy in internal wave subrange has the same
349 order of magnitude as the spectral energy in turbulence subrange, which indicates that the energy is
350 transferring to small-scale turbulence. This process is closely related to the polarity reversal of
351 internal solitary waves. The average diapycnal diffusivity is $(1.5\pm 0.1)\times 10^{-3}\text{ m}^2/\text{s}$, which is two
352 orders of magnitude larger than the background value.

353

354 Figure 6c is the horizontal slope spectrum of the L3 section. It can be seen from the spectrum that
355 the turbulence subrange is small, ranging from $0.011\text{-}0.07\text{ m}^{-1}$. The corresponding wavelength scale
356 is 14-89 m. The internal wave energy is larger and occupies a larger scale range. It can be seen from
357 the seismic section of survey line L3 (Figure 5c) that the amplitudes of the internal waves are large.
358 It indicates that the internal waves carry more energy, so the spectral energy in internal wave
359 subrange is larger (Figure 6c). In addition, there are many discontinuous and weak reflections in the
360 seismic section caused by breaking internal solitary waves. Internal solitary wave breaking weakens
361 the density gradient and enhances local mixing. This phenomenon is most obvious in the survey line
362 L3, where the average diffusivity is the largest of the three sections, $(2.2\pm 0.2)\times 10^{-3}\text{ m}^2/\text{s}$.

363

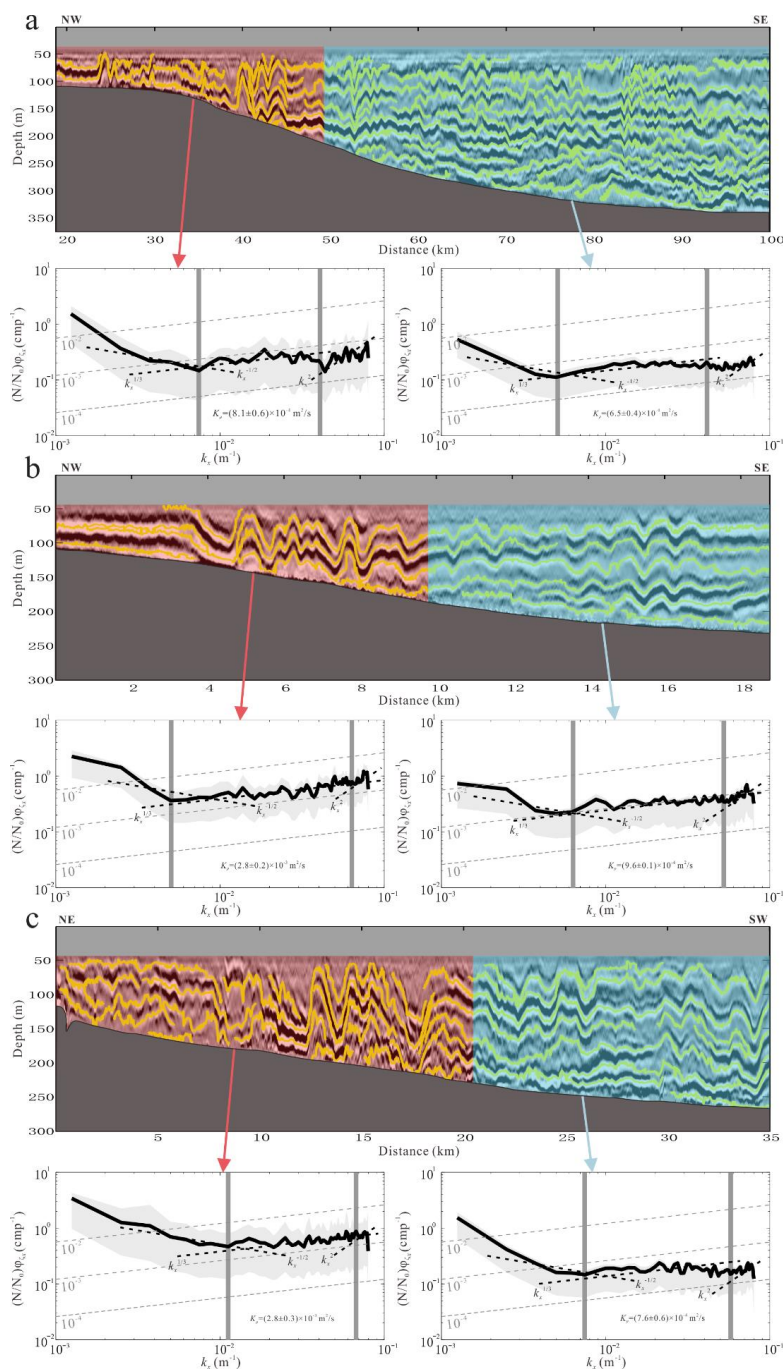


364

365 Figure 6. The average horizontal slope spectrum of L1 section (a), L2 section (b) and L3 section (c). The
 366 black line is the spectrum, the gray shadow represents the 95% confidence interval, the gray dashed lines
 367 represent the diffusivity contour, the black dashed lines represent the spectral slopes in internal wave
 368 subrange, turbulence subrange and noise subrange, respectively. The gray vertical lines represent the
 369 boundaries of turbulence subrange.



370
371 Figure 6 shows that the spectral energy of the L1 section is smaller than that of the other two sections.
372 This may be because the imaging range of the L1 section is different. The observations in the L2
373 and L3 sections are the polarity reversal of internal solitary waves, while the L1 section includes
374 not only the polarity reversal process, but also internal waves in deep water. The spectral energies
375 of these two processes should be different. We calculated the average horizontal slope spectrum of
376 the polarity reversal region and the non-polarity reversal region, respectively (Figure 7). The
377 spectral energy of the polarity reversal region in L1 section is higher than that of the non-polarity
378 reversal region, so does diapycnal diffusivity (Figure 7a). It implies that the wave energy will
379 accelerate to dissipate and transfer to turbulence when its polarity is reversed. Compared with the
380 non-polarity reversal region, the turbulence subrange of the polarity reversal region is smaller. The
381 lower boundary of the turbulence subrange of the polarity reversal region is slightly larger than that
382 of the non-polarity reversal region. It indicates that the turbulence in this region has a smaller scale.
383 The diapycnal diffusivity in the polarity reversal region in L2 section is about 3 times that of the
384 non-polarity reversal region (Figure 7b). The turbulence subrange of the polarity reversal region in
385 L2 section is slightly larger than that of the non-polarity reversal region. From the L2 section, it can
386 be seen that the events are continuous during the polarity reversal process, which indicates that the
387 wave breaking is weak. The internal solitary wave gradually fissions into several tails during the
388 polarity reversal, and energy is dissipated constantly. Therefore, there will be a large turbulence
389 subrange in the lateral direction (Figure 7b). This process can dissipate much more energy compared
390 with direct breaking of internal solitary waves (Masunaga et al., 2019). The diapycnal diffusivity in
391 the polarity reversal region in L3 section is larger, more than 3 times that of the non-polarity reversal
392 region. Although there are more internal (solitary) waves with larger amplitude in the non-polarity
393 reversal region, the diapycnal diffusivity is lower. The polarity reversal of internal solitary waves
394 significantly increases the diapycnal diffusivity. The turbulence subrange of the polarity reversal
395 region is small, and the lower boundary of the turbulence subrange is greater than 0.01 m^{-1} .
396



397

398 Figure 7. The horizontal slope spectra of the polarity reversal and non-polarity reversal regions calculated
 399 from L1 section (a), L2 section (b) and L3 section. The yellow lines are tracked reflection seismic events.

400



401 **3.3. Diapycnal diffusivity maps**

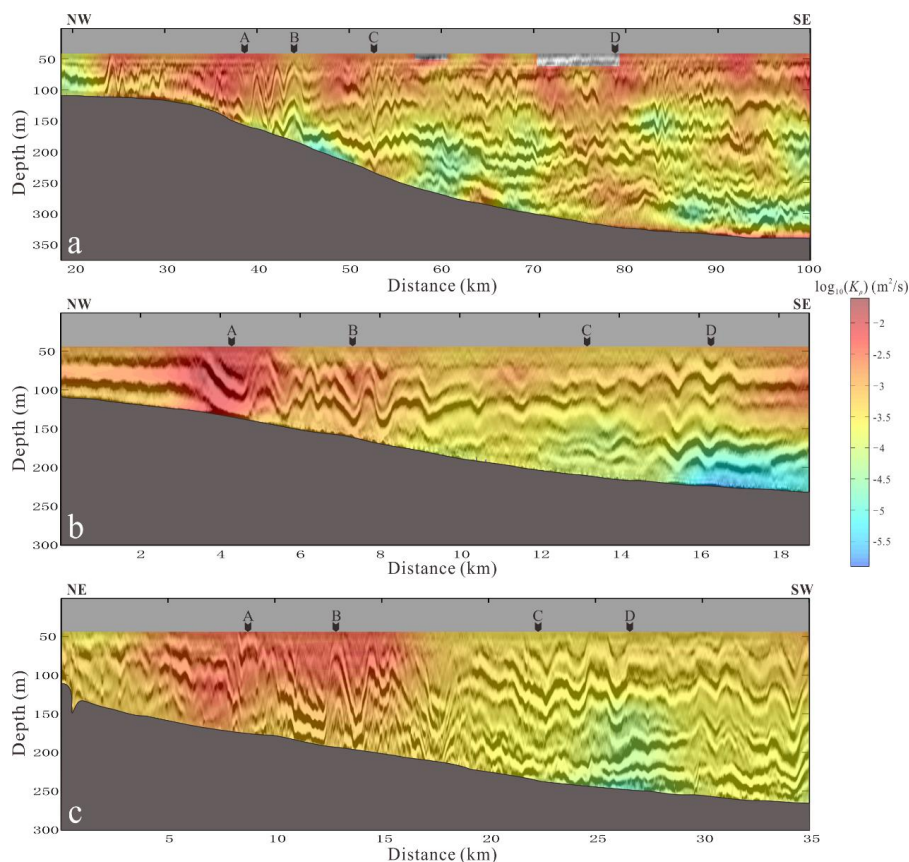
402

403 The diapycnal diffusivity maps of the three survey lines are shown in Figure 8. Figure 8a shows the
404 map of the survey line L1. The diffusivity is higher than that of the open ocean. The high value
405 presents a patchy distribution, mainly distributed in the depth between 50-150 m. The low diffusivity
406 values are mainly distributed in the depth between 150-300 m. Some high values are also distributed
407 near the seafloor. The diffusivity is larger in the polarity reversal region (24-45 km). Compared the
408 diffusivity of the four adjacent elevation internal solitary waves (24-30 km), we find that the
409 diffusivity is proportional to the amplitude of internal solitary waves. It means that the large
410 amplitude internal solitary waves contribute more to mixing. In the polarity reversal region (40-45
411 km), the diffusivity of the head wave's front is higher, that is, where the slope of the wave front
412 becomes gentle. While the diffusivity of the two elevation waves followed the head wave is small.
413 It indicates that the mixing induced by the internal solitary wave polarity reversal is stronger at the
414 beginning, and more energy is dissipated at this time. In the non-polarity reversal region (50-100
415 km), the diffusivity is low. The mode-1 depression internal solitary wave at 52 km increases the
416 diffusivity. There is an abnormal reflection area near the seafloor at 80 km, and the diffusivity is
417 high. In addition, there is also an area with increased diffusivity between 100-250 m at 93 km. This
418 may be related to the activity of large amplitude internal waves.

419

420 The diffusivity map of the survey line L2 is shown in Figure 8b. The high value is mainly distributed
421 at the front of head wave during polarity reversal process (4 km), which is consistent with the
422 characteristics on L1. The diffusivity after the head wave is low, but it is still higher than that in
423 other regions. The diffusivity in the non-polarity reversal region is almost uniform. The two internal
424 solitary waves at 15-16 km did not increase the diffusivity. There is a low diffusivity area near the
425 seafloor around 16-18 km, which is caused by not tracked reflection seismic events in this area. The
426 diffusivity map of survey line L3 (Figure 8c) is similar to that of L2. The high value is distributed
427 in the polarity reversal region and the diffusivity of head wave is still high. However, unlike the
428 diffusivity map of L2, the high diffusivity is mainly distributed in the shallow part of the head wave
429 (water depth 50-120 m), while the diffusivity of the whole head wave in L2 is high. In the non-
430 polarity reversal region, the diffusivity is small and the distribution is uniform too. The diffusivity
431 near the seafloor at 25-27 km is slightly lower than other regions.

432



433

434 Figure 8. The diapycnal diffusivity map of survey line L1 (a), L2 (b) and L3 (c). The black arrows
435 represent the position of vertical diffusivity profile.

436

437 4. Discussions

438 4.1 The relationship between diffusivity and reflection seismic events

439

440 When there is a significant impedance difference in the water column, a reflection seismic event
441 will occur (Holbrook et al., 2003; Ruddick et al., 2009). The impedance difference in the ocean is
442 contributed by temperature gradient and salinity gradient, where the former is usually greater than
443 the latter (Ruddick et al., 2009; Sallarès et al., 2009). Density is a function of temperature and
444 salinity, so the reflection seismic events are related to the density gradient. The enhanced mixing
445 reflects the structure of density gradient, thereby changing the appearance of the reflection seismic
446 events. Understanding the relation between diffusivity and reflection seismic events can help us
447 analyze the spatial distribution of diapycnal mixing by seismic section. Figure 8 shows that the
448 reflection seismic event in the high diffusivity region is obviously different from that in the low
449 diffusivity region. In the high diffusivity area (red in Figure 8), the reflection seismic events are
450 fuzzy, discontinuous or bifurcate. While in the low diffusivity area (yellow and blue in Figure 8),
451 the reflection seismic events are clear and continuous. This is because regions with high diffusivity

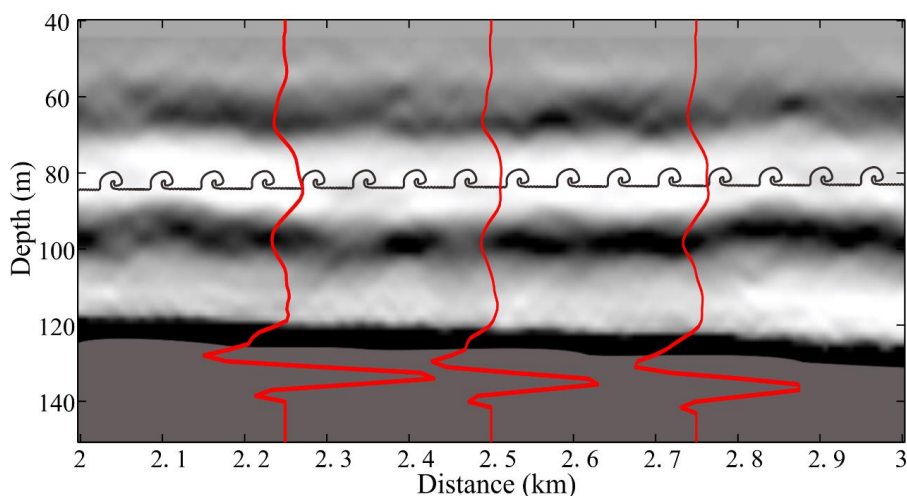


452 are strongly mixed. The density gradient is changed by mixing, so that it affects the appearance of
453 reflection seismic events. For example, in the polarity reversal region of three seismic sections, the
454 diffusivity is high, and the reflection seismic events are fuzzy and discontinuous. Especially in the
455 range of 5-10 km in Fig. 8c, the events are obviously break and weak. The diffusivity is low in areas
456 where the events are clear, such as the region near the seafloor around 45-50 km and the region near
457 the sea floor around 93-99 km in Figure 8a, and the region near the sea floor around 24-27 km in
458 Figure 8c.

459

460 The diffusivity is not only related to the continuity of the reflection events, but also related to the
461 fluctuation intensity of the events. The greater the fluctuation intensity of the events, the higher the
462 spectral energy, and the greater the diffusivity value. There is a mode-1 depression internal solitary
463 wave at 50-58 km in Figure 8a, and the reflection seismic event is clear and continuous at 180 m.
464 But the diffusivity is high, because the reflection events fluctuate more strongly. It can be seen from
465 the figure that, in addition to the amplitude of the internal solitary wave, there are also many high-
466 frequency waves at the shoulders of the internal solitary wave. These waves increase the spectral
467 energy and result in a higher diffusivity. In addition, the reflection seismic events before 4 km in
468 Figure 8b is continuous and without obvious fluctuations, but the diffusivity is higher. It can be seen
469 from the figure that the reflection events of this region are thicker than that of other regions. The
470 seismic data processing of the three sections in Figure 8 is the same, so the thicker events in Figure
471 8b do not stem from the low frequency of seismic waves. We think this may be caused by small-
472 scale mixing between layers, such as K-H instability. Figure 9 is an enlarged view of the location
473 between 2-3 km in the seismic section of L2 (Figure 5b). The wavelength of the seismic wave (red
474 line) at 80 m is larger than that at the seafloor, which is formed by the overlap of multiple wavelets.
475 It can be seen from the figure that a weak reflection event is barely visible at 80 m, which indicates
476 a thin reflection layer with weak impedance differences. The K-H instability can continue for a long
477 distance in the lateral direction (Seim and Gregg, 1994; Haren et al., 2014; Chang et al., 2016; Tu
478 et al., 2019) and enhance local ocean mixing. This structure can form at the tail of internal solitary
479 wave (Moum et al., 2003). The vertical scale of the K-H instability is small and usually appears on
480 the isopycnal. On the one hand, K-H instability weakens the density gradient so that the reflected
481 seismic wave energy is reduced. On the other hand, the vertical scale of K-H instability is lower
482 than the seismic wave resolution (a quarter of the seismic wave wavelength), so it makes overlapped
483 wavelets and stretched wavelength (Figure 9). Therefore, the reflection event in this area is thicker.
484 Besides, the horizontal scale of the K-H instability train is large, which may explain the larger
485 turbulence subrange on the horizontal slope spectrum (Figure 7b).

486



487

488 Figure 9. Schematic of the K-H instability. The red lines are the seismic waves, and the black billows
489 represent the K-H instability.

490

491 4.2 Enhanced diapycnal mixing induced by the polarity reversal of internal solitary waves

492

493 Strong mixing in the ocean mainly occurs near rough topography or area with strong tides (Simpson
494 et al., 1996; Rippeth et al., 2001, 2003; Nash and Moum, 2001; Klymak et al., 2008; Jarosz et al.,
495 2013; Staalstrøm et al., 2015; Wijesekera et al., 2020; Voet et al., 2020). The Dongsha Atoll region
496 in the South China Sea possesses both above features. On one hand, the Dongsha Atoll lies on the
497 continental slope with variable topography. On the other hand, large amplitude internal solitary
498 waves (Alford et al., 2015) propagating from the Luzon Strait reflect, refract, and shoal in this region.
499 This process will dissipate most of the energy carrying by the internal solitary waves. Especially in
500 the shoaling process, polarity reversal and breaking occur and the energy of internal solitary waves
501 transfer to smaller-scale waves. Our results (Figure 6) indicate that the average diffusivity has the
502 magnitude order of $O(-4)$ - $O(-3)$, consistent with previous observations by other techniques. St.
503 Laurent (2008) observed turbulent mixing on the continental shelf and slope, and found that the
504 mixing is higher at the shelf break, and the magnitude order of average dissipation is $O(-7)$ - $O(-6)$.

505 According to the average buoyancy frequency $N = 6cph$, the magnitude order of the average

506 diffusivity is $O(-4)$ - $O(-3)$ and consistent with our result. Yang et al. (2014) observed diapycnal
507 mixing on the continental shelf and slope, and found that the average diffusivity can reach the
508 magnitude order of $O(-3)$ too. Similar results have been reported in the study of internal solitary
509 waves shoaling in other regions. For example, Sandstrom et al. (1989) observed the turbulent
510 diffusivity caused by the nonlinear internal wave group on the continental slope of Canada, and
511 found the average diffusivity of $2.4 \times 10^{-3} \text{ m}^2/\text{s}$. Carter et al. (2005) observed the elevation internal
512 solitary waves in Monterey Bay and a diffusivity on the magnitude order of $O(-4)$. Richards et al.
513 (2013) observed the shoaling of nonlinear internal waves at the St. Lawrence Estuary, which induced
514 high turbulence and enhanced mixing. Therefore, it is reasonable that diapycnal mixing induced by
515 nonlinear internal waves on the continental shelf and slope in the northern South China Sea can



516 reach 100 times that in the open ocean.

517

518 The high diffusivity is mainly in the leading internal solitary wave during the polarity reversal. We
519 suggest that strong mixing may be caused by internal wave breaking due to convective instability.
520 In Figures 8a and 8c, the reflection seismic events are obviously discontinuous in the high
521 turbulence area of the leading wave, indicating that the density gradient is weakened by internal
522 wave breaking. The trough of the internal solitary wave decelerates first when the polarity is
523 reversed (Shroyer et al., 2008), which makes the Froude number (Fr) greater than 1 and causes
524 convective instability. This phenomenon can be found in other observational data. In the high-
525 frequency acoustic section, the backscatter at the top of internal solitary wave is increased when it
526 changes from depression to elevation wave (Orr and Mignerey, 2003), which indicates that the
527 turbulence of the front increased. However, in the seismic section of Figure 8b, we did not find the
528 events break at the front the polarity reversal internal solitary wave. The strong mixing of this
529 internal solitary wave may be induced by shear instability (Figure 9). Therefore, both convective
530 instability and shear instability are responsible for the enhanced mixing in this process. In addition,
531 the non-polarity reversal region in Figure 8a has a higher diffusivity in 50-150 m than other regions.
532 This range is in the thermocline (Figure 1c). The internal waves usually greatly increase mixing in
533 the thermocline, which is related to the shear instability of internal waves (Mackinnon and Gregg,
534 2003). Shear instability is an important mechanism of internal wave dissipation (Farmer and Smith,
535 1978), and it more likely occurs in nonlinear internal waves than convective instability (Zhang and
536 Alford, 2014). The results of high-frequency acoustic observations show that the enhanced
537 backscatter at the bottom of the thermocline represents higher shear instability when the internal
538 solitary waves are shoaling (Orr and Mignerey, 2003), which is consistent with the depth range of
539 high diffusivity in our results.

540

541 What is inconsistent with the observed distribution of mixing is that our results are not able to show
542 diffusivity in the bottom boundary layer. Because our seismic data was collected in summer, the
543 strong stratification at this time limits the vertical range of the bottom boundary layer (Mackinnon
544 and Gregg, 2003). So that the bottom boundary layer near the Dongsha Atoll is thin and lower than
545 the thickness that can be recorded by seismic data. So, the diffusivity we calculated does not include
546 the bottom boundary layer. The enhanced diapycnal mixing induced by the polarity reversal of
547 internal solitary waves plays an important role in local environment and primary productivity. On
548 one hand, diapycnal mixing on the continental slope and shelf makes an important contribution to
549 ocean heat flux, which affects climate and the ocean through heat exchange of local water column
550 (Rahmstorf, 2003; Tian et al., 2009). On the other hand, the vertical flux caused by turbulence can
551 redistribute materials in the ocean and have an important impact on the marine ecological
552 environment (Sharples et al., 2001; Moum et al., 2003; Klymak and Moum, 2003; Wang et al., 2007).

553

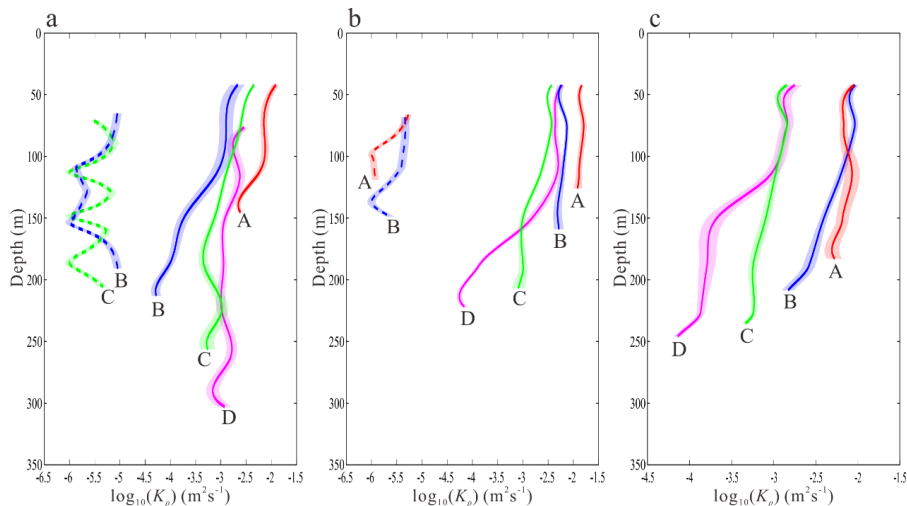
554 **4.3 The mixing scheme of internal solitary wave shoaling**

555

556 We compared the vertical distribution of diffusivity with the vertical mixing scheme of internal
557 wave breaking proposed by Vlasenko and Huntter (2002). Although Klymak and Legg (2010) also
558 proposed a mixing scheme for internal wave shoaling and achieved good results in numerical
559 simulation, we cannot use this method to calculate mixing parameters because of lacking high



560 resolution density observation data. Figure 10 shows the vertical distribution of diffusivity from
 561 seismic data (solid line) and the diffusivity calculated from mixing scheme (dashed line) at 4
 562 positions of the three survey lines (black arrows in Figure 8). The reflection events in the L3 section
 563 are broken, and it cannot be guaranteed that the events are parallel to the streamline. Therefore, we
 564 did not use the method described in section 2.3 to calculate the wave-induced velocity, and thus did
 565 not obtain the diffusivity of the mixing scheme. It can be seen from Figure 10 that the turbulent
 566 diffusivity gradually decreases from shallow to deep water. Except for the local low diffusivity value
 567 in the deep water at the position D of Figure 10b and 10c, the diffusivity reduction rate at the other
 568 location is similar. Figures 10a and 10b show that the parameterized diffusivity is nearly 2--3 orders
 569 of magnitude smaller than our result, but they have a similar trend of change. In Figure 10a (line
 570 L1), the parameterized diffusivity (blue dotted line) at position B decreases an order of magnitude
 571 within 50-100 m. This tendency is same as our results. However, the parameterized diffusivity
 572 within 150-200 m increases by one order of magnitude, which is inconsistent with our results (solid
 573 blue line). The parameterized diffusivity at position C fluctuates periodically and also keeps a
 574 decreasing trend on the whole. In the survey line L2, we selected position A and position B to
 575 calculate the parameterized diffusivity. The diffusivity at position A (red dashed line) decreases
 576 rapidly within 60-100 m, and then almost keeps unchanged. This is different from our result (solid
 577 red line), and the reduction rate of the diffusivity is larger than our result. The trend of the diffusivity
 578 at position B (blue dashed line) above 110 m is consistent with our results (solid blue line), but the
 579 diffusivity below 110 m decreases rapidly and then rises again. In our results, the diffusivity
 580 decreases slowly at the same depth. The value is consistent with that in the open ocean. However,
 581 the mixing enhanced obviously on the continental shelf and slope, because of the internal wave
 582 shoaling. The mixing scheme underestimates mixing, especially the strong mixing induced by the
 583 polarity reversal of internal solitary waves. Our results indicate that near the Dongsha Atoll, where
 584 large amplitude internal solitary waves develop, mixing will be enhanced by the shoaling internal
 585 solitary waves. The diffusivity gradually decreases from shallow to deep water (not including the
 586 bottom boundary layer). This has important implications for improving the mixing scheme for
 587 models on the continental shelf and slope.
 588



589



590 Figure 10. The vertical distribution of diffusivity from seismic data compare with the mixing scheme.
591 The solid line represents the vertical distribution of diffusivity at the four positions A (red), B (blue), C
592 (green) and D (magenta), and the dotted line represents the parameterized diffusivity at the corresponding
593 positions. The shadow indicates the margin of error.

594

595 5. Conclusions

596

597 We have observed the polarity reversal of internal solitary waves by reflection seismic data near the
598 Dongsha Atoll in the South China Sea, and calculated their slope spectra (Figure 6) and diapycnal
599 diffusivity (Figure 8). The results show that the average diapycnal diffusivities of the three survey
600 lines are about two orders of magnitude greater than the open-ocean value. We calculated the
601 average spectral slope of the polarity reversal and non-polarity-reversal regions (Figure 7), and
602 found that the former is about 3 times larger than the latter. The diffusivity maps reveal that
603 horizontally high diffusivity is mainly in the leading wavefront of an internal solitary wave in
604 reversing polarity, and vertically high diffusivity is mainly in the thermocline (50-100 m).

605

606 We analyzed the relation between reflection seismic events and diapycnal diffusivity. The result
607 indicates that continuous and clear reflection events correspond to low diffusivity, while
608 discontinuous or fuzzy events correspond to high diffusivity. The strength of the events also affect
609 the magnitude of diffusivity. The stronger the fluctuation, the higher the spectral energy, and the
610 higher the diffusivity. In addition, we observed an area of high diffusivity with a large horizontal
611 scale in L2, and the reflection events did not appear to be discontinuous or fuzzy. We suggest that
612 this is enhanced mixing induced by the K-H instability (Figure 9). The vertical scale of the K-H
613 instability is smaller than the resolution of our seismic data, so we cannot observe clearly in the
614 seismic data. But its high-energy characteristics can be recorded by reflection events.

615

616 Our results show that shoaling internal solitary wave enhance local mixing. The magnitude order of
617 diapycnal diffusivity is consistent with previous studies. We suggest that there are two mechanisms
618 accounting for the enhanced mixing. On one hand, the polarity reversal of internal solitary waves
619 results in convection instability, which induces internal solitary wave breaking. This mechanism
620 appears at the leading edge of one internal solitary wave in the survey lines L1 and L3. The
621 discontinuous reflection events indicate that the internal solitary wave is broken. While in the
622 seismic section of L2, the reflection events are continuous and clear at the leading edge of the
623 internal solitary wave and other strong mixing areas in the three sections. Such strong mixing is
624 mainly caused by shear instability.

625

626 We picked four positions from the diffusivity maps to analyze the vertical distribution of diapycnal
627 diffusivity (Figure 10). Our result shows that the diffusivity gradually decreased from shallow to
628 deep water (excluding the bottom boundary layer). Compared with previous one mixing scheme,
629 the parameterized diffusivity is about 2--3 orders of magnitude smaller than our result. This means
630 that the mixing scheme underestimates mixing induced by internal solitary wave shoaling near the
631 Dongsha Atoll. However, the vertical pattern of the parameterized diffusivity is consistent with our
632 result.

633



634 **Code and data availability.** The bathymetry data were provided by the General Bathymetric
635 Chart of the Oceans (GEBCO, <http://www.gebco.net/>), and prepared using the Generic Mapping
636 Tools (GMT, <https://generic-mapping-tools.org/>). The hydrological data set we used were product
637 by Copernicus Marine Environment Monitoring Service (CMEMS,
638 <https://resources.marine.copernicus.eu/>). The seismic data were processed using Seismic Unix
639 (<https://wiki.seismic-unix.org/start/>).

640

641 **Author contribution.** The concept of this study was developed by Haibin Song and extended
642 upon by all involved. Yi Gong implemented the study and performed the analysis with guidance
643 from Haibin Song. Zhongxiang Zhao, Yongxian Guan, Kun Zhang, Yunyan Kuang and Wenhao Fan
644 collaborated in discussing the results and composing the manuscript.

645

646 **Competing interests.** The authors declare that they have no conflict of interest.

647

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