

## ***Interactive comment on “BP Neural Network and improved Particle Swarm Optimization for Transient Electromagnetic Inversion” by Huaiqing Zhang et al.***

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Dear Editors and Reviewers: Thank you for your letter and for the reviewers' comments concerning our manuscript entitled “BP Neural Network and improved Particle Swarm Optimization for Transient Electromagnetic Inversion”. (MS No.: npg-2019-36). Those comments are all valuable and very helpful for revising and improving our paper, as well as the important guiding significance to our researches. We have studied comments carefully and have made correction which we hope meet with approval. Revised portion are marked in red in the paper. The main corrections in the paper and the responds to the reviewer's comments are as flowing:

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For your guidance, itemized response to each review's comments is appended below.

Reviewer #1: Dear reviewers: Comments: 1. Page 2, line 53 → Please provide a correct reference name for Fernndez et al. (2010). 2. Page 6, line 136 → There is no T k and O k terms in equation 14. In addition, is there no unit for the training error value calculated? 3. Page 7, line 148 → use slightly better instead of litter better. 4. Do you have any experimental studies (i.e., parameter tuning) for the PSO parameters used in the study? 5. The sentence given below requires a reference. “Comparing to the standard PSO (SPSO), a chaotic oscillation inertia weight PSO(COPSO) which can accelerate the convergence rate in the early stage was proposed naturally.”The inertia weight value used in SPSO-BP approach is not clear in the text. Based on my experiments for parameter estimation from geophysical anomalies (e.g., self-potential, gravity, magnetic) using PSO algorithm, the values including 2.041 (c 1 ), 0.948(c 2 ) and 0.729 (iAÛ) proposed by Carlisle and Dozier (2001) mainly provide quite efficient results. Please provide a comparison. 6. Considering the results presented in Table 2 and Fig.3, is there a possibility to use the same initial population during the evaluation process to provide a good comparison? 7. Please use more proper terms in the text regarding a geophysical optimization study(e.g., predict and desired outputs). 8. Please depicts and iAÛ e inertia weight values in title of Table 3. 9. Use true values instead of reference value and theoretical curve instead of theory curve. In fact, I do not see any curve in Fig. 11. They represent layer parameters. 10. Please define PSO parameter values used in the synthetic case. 11. Please discuss the main advantages and disadvantages of the BP compared to the metaheuristic approaches requiring a parameter space which can be chosen 12. Such a study must include the effect of the noise on the solution in the synthetic case.Besides uncertainty analyses for estimated parameters should be applied for data sets with and without noise. A field example must be also presented.

1-Reply: 1-Page 2, line 53 → Please provide a correct reference name for Fernndez et al. (2010). (1) We are sincerely sorry for the negligence of the author's name spelling

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when citing references. We have made changes and amend them as follows. At the same time, we are also very grateful for your careful review of the manuscript. Fernández et al. (2010) successfully introduced the PSO in 1-D resistivity inversion. 2-Page 6, line 136 → There is no T k and O k terms in equation 14. In addition, is there no unit for the training error value calculated? (2) Due to our negligence, 'Tk' and 'Ok' terms on line 136 of the page 6 are misspelled and have been modified as follows: Ts , Os are the expected and predicted output for training sample respectively. Meanwhile, in order to evaluate the effect of model training in this paper, the training error expression is adopted as: . In the formula, the training error E only represents the error value, so there is no unit for the training error value calculated. 3-Page 7, line 148 → use slightly better instead of litter better. (3) According to the meaning in the paper, it is more appropriate that 'slightly better' term than 'litter better', thank you again for your valuable suggestions. 4- Do you have any experimental studies (i.e., parameter tuning) for the PSO parameters used in the study? (4) In the research of this paper, some experiments are performed on the various different parameter values in the PSO algorithm. The experiment results show that the learning factor (c1 and c2), inertia weight (w), population size (M) and maximum iterations (Tmax) have a little influence on the PSO optimization results. In PSO, the learning factors c1 and c2 determine the influence of the experience of the particle itself and on the trajectory of the particle group, reflecting the information exchange between the particle swarms. Setting a larger value of c1 will cause the particles to linger too much in the local range, while a larger c2 will cause the particles to converge prematurely to the local minimum, thus setting a larger or smaller c1 and c2 is not conducive to the search of particles. Ideally, the particles should initially search the entire space as much as possible, and at the end of the search, the particles should avoid falling into local extrema. The general setting is c1=c2=2. Among the adjustable parameters of the algorithm, the inertia weight is the most significant, which determines the influence of the previous flight speed of the particle on the current flight speed. Therefore, the balance between the global search and the local search can be achieved by adjusting the value of the inertia weight w: when w is large, the global

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search ability is strong, and the local search ability is weak; when w is small, the global search ability is weak, and the local search ability is strong. Thence, the proper inertia weight can improve the optimization ability, and reduce the iterations. However, there is still some difficulty to achieve the optimal performance, because when the inertia weight is large, it is conducive to global search with fast convergence rate, but it is not easy to get an exact solution. When the inertia weight is small, it is beneficial to local search and getting exacter solution, but the convergence is slow and sometimes it falls into local extremum. Therefore, in the PSO optimization algorithm, it is hoped that there will be a higher global search ability in the early stage to find a suitable seed, and a higher development capability in the later stage to accelerate the convergence speed. Thence, the inertial weight is used as a typical linear decreasing strategy. The formula of w is, in which, according to studies by Y. Shi et al. (1999), the initial value of inertia weight is wstart=0.9, and the end value of inertia weight is wend=0.4, which can make PSO explore more at the beginning and locate the approximate position of the optimal solution faster. As w gradually decreases, the particle speed slows down and a fine local search begins. This method enables PSO to better control global and local search capability, speed up the convergence and improve the performance of the algorithm. At the same time, in order to further improve the global search ability of the PSO algorithm, the chaotic oscillation inertia weight is adopted as , which , the experiments results prove that the best results can be obtained when  $x_0 = 0.234$  and  $\mu = 4$ , which the equation is in a completely chaotic state. As for the population size (M), the number of individuals contained in the population. In general, there are the higher population diversity and stronger the search ability for algorithm as the population size is larger, therefore, the probability of obtaining an optimal solution is greater, but it also takes more calculation time. Therefore, after a series of numerical experiments, it is reasonable as the population size M=60 and the maximum iteration number Tmax=30.

5-The sentence given below requires a reference. "Comparing to the standard PSO (SPSO), a chaotic oscillation inertia weight PSO(COPSO) which can accelerate the convergence rate in the early stage was proposed naturally." The inertia weight value

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used in SPSO-BP approach is not clear in the text. Based on my experiments for parameter estimation from geophysical anomalies (e.g., self-potential, gravity, magnetic) using PSO algorithm, the values including 2.041 (c1), 0.948(c2) and 0.729 (w) proposed by Carlisle and Dozier (2001) mainly provide quite efficient results. Please provide a comparison. (5)According to your suggestion, the corresponding reference has been added in the corresponding position of the article for the article more rigorous, the literature is as follows: Shi, X. M., Xiao, M., Fan, J. K., Yang, G. S., and Zhang, X. H.: The damped PSO algorithm and its application for magnetotelluric sounding data inversion, Chinese Journal of Geophysics., 52, 1114–1120, <https://doi.org/10.3969/j.issn.0001-5733.2009.04.029>, 2009. We are sorry that the SPSO-BP algorithm inertia weight value is not clearly explained in the manuscript. In this paper, the inertia weight is used as a typical linear decrement strategy, which the calculation formula (w) is . At the same time, the definition of SPSO algorithm inertia weight is supplemented on line 129 of the manuscript. Among them, according to a large number of experimental studies by Y. Shi et al. (1999), the inertia weight initial value (ws) is 0.9, and the inertia weight ending value (we) is 0.4, which can make PSO better control global search ability and local search ability, and speed up the convergence and improve the algorithm performance. The learning factors and inertia weight parameter values in PSO has been elaborated in the previous question (4). In fact, we found that different parameter values have certain influence on the PSO optimization results under different research models by a lot of researches, that is, when the different models achieve the best optimize results using PSO, the various parameter values are different. Therefore, through a series of test functions and geoelectric model inversion experiments, the good optimization results are obtained when the parameter value c1=c2=2, which the effect is better than the results optimized under 2.041 (c1), 0.948 (c2) and 0.729 (w). Among them, the results of SPSO-BP optimization under different parameter values are as follows: Table.1 Comparison of the different parameter values in SPSO-BP algorithm for testing functions Testing functions SPSO-BP c1=c2=2 w=0.729 SPSO-BP c1=2.041 c2=0.948, w=0.729 Average value Optimal value

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Optimal value Average value Optimal value Rosenbrock 2.375e-3 2.300e-5 0.3911 3.1665e-04 Bohachevsky 0.225 1.024e-3 0.2832 0.0013

Table.2 Inversion comparison of three-layer H type geoelectric model H type resistivity ( $\Omega \cdot m$ ) thickness h(m) total relative error(%) 1 2 3 h1 h2 reference value 100 10 100 100 200 – SPSO-BP relative error(%) c1=c2=2 w=0.729 0.062 -0.322 -0.737 -0.579 -0.970 2.672 SPSO-BP relative error(%) c1=2.041 c2=0.948, w=0.729 0.2438 2.3154 -0.566 0.9707 -0.3327 4.4290

6- Considering the results presented in Table 2 and Fig.3, is there a possibility to use the same initial population during the evaluation process to provide a good comparison? (6) According to your suggestion, the same initialized population is used for the test function optimization. The search curves for the Rosenbrock and Bohachevsky test functions are shown below, and made changes in the manuscript. However, the comparative study results show that the same initial population has no significant effect on the final optimization results, so that it is almost negligible.

7-Please use more proper terms in the text regarding a geophysical optimization study(e.g., predict and desired outputs). (7) Thank you for your suggestion. For the rigor of the article, we have modified the inappropriate terminology, such as 'predict output' modified to 'predict value', 'desired output' modified to 'actual value', 'reference value' modified to 'true values'. 8-Please depict ws and we inertia weight values in title of Table 3. (8) In order to reasonably compare the effects of four different inertia weights in the PSO algorithm, the same initial inertia weight value and end inertia weight value are used in this paper, such as inertia weight  $\omega_s = 0.9$ ,  $\omega_e = 0.4$ . At the same time, based on the valuable comments made by the reviewers, in order to facilitate the reader to more clearly understand the comparison effect for different inertia weights, we have refined the title of Table 3 as follows: Table.3 Comparison of different inertia weights in PSO algorithms ( $\omega_s = 0.9$ ,  $\omega_e = 0.4$ ). 9-Use true values instead of reference value and theoretical curve instead of theory curve. In fact, I do not see any curve in Fig. 11. They represent layer parameters. (9) Thank you very much for

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pointing out the incorrect terminology in the paper and giving appropriate revisions. We have made corresponding revisions, such as the 'reference value' in Table 4 and Table 5 is modified to 'true values', the 'theory curve' is modified to 'theoretical curve'. As you can see, the theoretical curve in Figure 11 of the first draft does represent the layered parameter value. However, due to the inappropriate naming of the line segments in the figure, it is inconvenient for the reader to understand, so after careful consideration, the 'theory curve' is modified to 'True values' as shown below.

(a) Three-layer H type geoelectric model (b) Five-layer KHK type geoelectric model Fig. 11 Inversion comparison for different geoelectric models

10- Please define PSO parameter values used in the synthetic case. Due to our negligence, it not clearly account for the various parameters values of PSO algorithm in the Layered model and parameter analysis part. However, in fact, the PSO parameter value in this synthetic case is the same as the PSO parameter value of Algorithm Testing part. Therefore, the following is added to Section 4.3 of this paper. A 3-layered and 5-layered geoelectric models were investigated, which the PSO parameter values are the same as those of the Algorithm Testing parts in the paper. 11-Please discuss the main advantages and disadvantages of the BP compared to the metaheuristic approaches requiring a parameter space which can be chosen. Regarding the advantages and disadvantages of BP compared to the metaheuristic approaches requiring a parameter space which can be chosen, which has been elaborated in the paper discussion part, and its detailed description is as follows: At present, heuristic algorithms are mainly based on natural body algorithms, which mainly includes ant colony algorithm, simulated annealing method, particle swarm optimization, ant optimization, fish swarm algorithm, bee colony algorithm and so on. And heuristic algorithms have a common feature: starting from a random feasible initial solution, an iterative improvement strategy is adopted to approximate the optimal solution of the problem. The advantage of the heuristic algorithm is that it is more efficient than the blind search method. In addition, a carefully designed heuristic function often gets

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the optimal solution in a very short time. However, the heuristic algorithm needs to repeatedly call the forward algorithm for each iteration in nonlinear resistivity inversion, resulting in a long calculation time. However, BP neural network is the most active branch for nonlinear resistivity inversion. The inversion algorithm is different from the nonlinear heuristic method based on global solution space search, which it does not need to call the forward algorithm repeatedly, so its calculation time is short. At the same time, BP can approximate any nonlinear continuous function with arbitrary precision, which makes BP have strong nonlinear mapping ability. In addition, BP neural network can automatically extract "reasonable rules" between output and output data through learning, and adaptively memorize the learning content in the weight of the network, that is, BP neural network has the ability of high self-learning and self-adaptation; and BP neural network can be trained after training mode or noise-contaminated mode for correct prediction, that is, BP neural network has the generalization ability to apply learning results to new knowledge; in addition, the BP neural network does not have a great impact on the global training results after the local or part of the neurons are destroyed, that is, the BP neural network has certain fault tolerance. However, the weight of the BP neural network is gradually adjusted by the direction of local improvement, which causes the algorithm to fall into local extremum, and the weight converges to the local minimum point, which leads to network training failure; in addition, BP is very sensitive to the initial network weights, initializing the network with different weights, which tends to converge to different local minima, resulting in different results for each training; and BP algorithm is essentially a gradient descent method, resulting in BP has a slow convergence rate; and the approximation and generalization ability of the BP neural network model is closely related to the learning samples, that is, the BP neural network depends on the sample selection. In view of the fact that the neural network is sensitive to the initial weight and easy to fall into the local minimum, the heuristic global search particle swarm optimization algorithm with simple structure, fast convergence and high precision is used to optimize the initial weight and threshold of the neural network. The method is stable and effective, and is not easy to fall into local

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optimum, and has better performance.

12-Such a study must include the effect of the noise on the solution in the synthetic case. Besides uncertainty analyses for estimated parameters should be applied for data sets with and without noise. A field example must be also presented. (12) Anti-noise tests and a field example are added as follows. Since the result of the inversion is affected by various control parameters, computer system performance and programming planning in the algorithm, parameter uncertainty analysis should be performed in the paper, which it is the insufficiency of the research work, and it is also the direction we need further research. We sincerely hope to get your understanding. (4) Robust performance analysis In order to verify the algorithm robustness, 5%(26dB) and 10%(20dB) Gaussian random noise was added in TEM data for three-layer geoelectric model. Three kinds of inversions were implemented respectively. The results and comparison were shown in Table.3. The Hz(t) and data with 5% noise were shown in Fig.4. Table 3 Comparison of inversion results for three-layer H type (with noise) model model parameters resistivity ( $\Omega\hat{A}m$ ) thickness h(m) Total relative error(%)

1	2	3	h1	h2	true value	100	10	100	100	200	-	without noise	BP	99.724	9.937	100.765					
99.031	198.701	3.284	COPSO-BP	100.031	9.991	99.310	100.234	200.886	1.487	5%	noise	BP	101.374	9.966	98.283	101.255	199.282	5.039	COPSO-BP	100.252	9.977
98.222	101.206	199.228	3.847	10%	noise	BP	90.525	9.931	99.481	101.748	203.105	13.976	COPSO-BP	104.472	9.96050	101.345	100.570	199.437	7.064		

Fig.5 Forward data of Hz and data with 5% noise As can be seen from Table 3, after applying 5% and 10% Gaussian noise the COPSO-BP inversion has higher robust ability. The accuracy was obviously improved based on the total relative error data.

4.4 Field example analysis In order to test the effectiveness of the method, a transient electromagnetic vertical magnetic field (Hz) with 10 measuring points at the 380m to 1280m of the No. 1 line from a mining area in Anhui Province was selected. After the data processing, the inversion was performed using the 3-layer neural network model in the previous section, and the results of BP and COPSOBP inversion were

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compared. Figure 13 shows the comparison between the surveyed data and the inversion data at 380m of the No. 2 line in the mining area. Figure 14 displays the pseudo-sections of the 10 sets of inversion data combined with the geological data interpolation smoothing. It can be seen from Fig. 14 that the first layer is a low resistivity ( $100\sim 200\ \Omega\hat{A}m$ ), which is inferred to be the second layer (T2g22) gray dolomite of the Middle Triassic old Malague section, with a thickness of about 200 m; the second layer is the second highest resistivity ( $300\sim 400\ \Omega\hat{A}m$ ), which is surmised to be the first layer (T2g21) dolomite of the Middle Triassic old Malaga section, with a thickness of about 400m; the third layer is high resistivity ( $600\sim 800\ \Omega\hat{A}m$ ), which is speculated to be the 6th layer (T2g16) limestone dolomite of the Middle Triassic old group. The results are basically consistent with the geological conditions of the mining area, indicating the feasibility and effectiveness of the neural network method. And the results of COPSO-BP inversion are better than those of BP, which the inversion position is more accurate, the shape and spacing are clearer, and the resistivity of each layer is more consistent with the those of the actual geological model.

(a) BP (b) COPSOBP Figure 13. 1D inversion forward results. (a) BP; (b) COPSOBP.

(a)BP (b) COPSO-BP Figure 14. Inversion results of BP (a) and COPSO-BP (b).

Special thanks to you for your good comments.

Reviewer #2: Dear reviewers: Comments: 1. The main problem is the TEM forward calculation in this manuscript. It is not clear for me. Is it frequency or time domain? The authors said that this is a transient EM. However, they started derivation with the frequency domain expression using Kaufman's (1983) book, then they obtained Hz(t) response using Gravier –Stehfest method. If you start a frequency domain, after getting a layered response function you need to get the Fourier transform to get back to in the time domain. Either frequency or time domain we need to use some kind of filter function, since there is no analytic solution for a layered earth. Thus, we use some approximations. In addition, I don't see an apparent resistivity formula in the manuscript.

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Do they use a late time or early time approximation for the apparent resistivity calculation (or all time approximation)? I would like to see a clear explanation about the apparent resistivity formula and TEM forward response explanation in the manuscript. Please be clear about the TEM forward calculation. 2. There is no field data for the inversion as an example, which is very important. All calculation is synthetic. The manuscript can be published in this journal after my suggestion completed.

2-Reply: 1- The main problem is the TEM forward calculation in this manuscript. It is not clear for me. Is it frequency or time domain? The authors said that this is a transient EM. However, they started derivation with the frequency domain expression using Kaufman's (1983) book, then they obtained  $H_z(t)$  response using Gravier-Stehfest method. If you start a frequency domain, after getting a layered response function you need to get the Fourier transform to get back to in the time domain. Either frequency or time domain we need to use some kind of filter function, since there is no analytic solution for a layered earth. Thus, we use some approximations. In addition, I don't see an apparent resistivity formula in the manuscript. Do they use a late time or early time approximation for the apparent resistivity calculation (or all time approximation)? I would like to see a clear explanation about the apparent resistivity formula and TEM forward response explanation in the manuscript. Please be clear about the TEM forward calculation. We are sincerely sorry that the TEM forward calculation has not been explained clearly in the manuscript. After careful consideration and modification, the relevant content has been added in the Forward Model part of article and was elaborated as follows: TEM forward response explanation The forward model of this paper belongs to the time domain. Due to the high-frequency oscillation and slow decay characteristics of the Bessel function in the formula (15) of this manuscript, the analytical solution can only be obtained in uniform half-space. However, the layered geoelectric model can only be solved by numerical calculation method. Considering the Hankel transformation of the first-order Bessel function, Anderson used a linear numerical filtering method with a filter coefficient of 283, which achieved better results. Then based on Anderson's research, D.Guptasarma and B.Singh (1997) improved the digital

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filtering algorithm and gave filter coefficients which of 61 and 120 points J0, 47 and 140 points J1, and getting higher calculation accuracy. This paper adopts the improved digital filtering method, the filter coefficient of 47 points J1 is selected by a large number of experiments, so that the frequency domain response of layered earth with the center loop source can be obtained. Then, according to the Laplace transform and the related properties, the frequency domain response is converted into a complex frequency domain. Next, due to the accuracy of the Gaver-Stehfest algorithm is higher than that of the Guptasarma algorithm in the late stage, and the method has the characteristics of slow filtering speed and pure real number operation, which makes it faster than cosine transform, so that the algorithm can be used to solve complex terrains. Finally, the Gaver-Stehfest algorithm is selected to transform the complex frequency domain response into a time domain response. Among them, the 12-point filter coefficient is used in the G-S transform algorithm, and the detailed derivation process and explanation are as follows: 1) Frequency domain response of the center loop source For circular emission loops, the analytical solution is typically derived from the area of the perpendicular magnetic dipole source or the line integral of the horizontal magnetic dipole. Consider the vertical dipole  $dm()$ , and the emission current  $I$ . Calculate the area of  $dm$  along the entire loop through a surface integral: (1) Using the following formula: (2) Bring into equation (1) and interchange the integral with the summation order: (3) In the above formula, the inner layer integral is not zero only when  $n=0$ , so there are: (4) Using the below relation: (5) We can obtain (6) Similarly, we can get: (7) where  $a$  is the radius of the circular transmitting coil. Therefore, the frequency domain response of the center loop ( $=0$ ) can be acquired as:

(8) Among them, the recursive relationship can be gained after a series of derivations: (9) Analytic calculation of frequency domain response in uniform half space Through the above formula, the frequency domain response of the central return line  $H_n=1$  in a uniform half space can be obtained as follows: (10) Also, we can gain the analytical formula of the vertical magnetic field (11) Numerical calculation of frequency domain response for layered geoelectric model (Hankel trans-

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form) In the integral formula (7), due to the high-frequency oscillation and slow decay of the Bessel function, the analytical solution can be obtained only in the uniform half-space. But for the solution of the layered earth, only the numerical calculation method can be used. Anderson used linear numerical filtering, using 283 as the filter coefficient, and achieved ideal results. Based on Anderson's research, D.Guptasarma and B.Singh (1997) improved the digital filtering algorithm and gave the filter coefficients of 61 and 120 points J0 and the filter coefficients of 47 and 140 points J1. Its calculation accuracy is higher. The calculation formula for the improved digital filtering method of Guptasarma and Singh is: (12) In the formula  $\lambda_i = 1/r \times 10^{[a+(i-1)s]}$ ,  $W_i$  is the filter coefficient. After the numerical simulation experiment, the 47-point J1 filter coefficient is selected, so that the frequency domain response of the layered earth transient electromagnetic can be obtained, which lays a foundation for the solution of the next time domain response. 2) Time domain response of center loop source According to the Laplace transform and related properties, the correlation complex frequency domain response function can be obtained, and then The supply current  $I(s)$  is multiplied by the vertical magnetic field frequency domain response function to obtain the time domain response and time partial derivative  $\partial H_z / \partial t$  (13) If the supply current is a unit positive step response, its corresponding Lagrangian transformation is  $s^{-1}$ ; if the supply current is a unit step response: (14) Where  $T_1$  is the off time and its corresponding Lagrangian transformation is  $e^{-sT_1}$  (15) In actual exploration work, to avoid the electromagnetic noise generated by the sky power, the detecting device usually observes the signal induced voltage: (16) where,  $S$  is the area of the receiving coil, and  $n$  is the number of turns of the coil. The induced voltage is proportional to the rate of change of the vertical component of the magnetic induction.

Analytic calculation of time domain response in uniform half space According to the formula (11) and (13), the positive step response of the central loop can be obtained: (17) According to  $f(t) = f(\infty) - f(t) e^{-\lambda t}$ , the negative step response of the center loop and the time derivative of the vertical magnetic field can be obtained: (18) (19) Numerical calculation of time domain response of geoelectric model (G-S transform-

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tion) Through the above, the numerical solution of the frequency domain response of the layered geoelectric model is gained, and then the time domain response is got by frequency-time domain conversion. At present, the main frequency-time domain conversion methods include Fourier transform method, delay spectrum method, Guptasarma filtering algorithm and Gaver-Stehfest inverse Lagrangian transform method. The four methods have their own advantages, disadvantages and applicable scope. Although the Fourier transform method can be used for a variety of geoelectric models and launchers, multiple frequency and kernel function samplings make the calculations large and computationally slow. The delay spectrum method is also called the attenuation spectrum method. The required calculation frequency is small and the calculation amount is small, but the generalized solution of the ill-conditioned matrix needs to be solved, and the late transient response is not stable enough. The late response of the Guptasarma filtering algorithm is more stable than the delay spectrum method, but the number of frequency samples required is increased and is only suitable for calculating a simple geoelectric model. The Guptasarma filtering algorithm is large, but Gaver-Stehfest algorithm has the advantages of pure real number operation, high calculation precision, less required frequency points and can be used to calculate complex geoelectric models. It has wider applicability in electromagnetic detection. The complexity of the frequency domain electromagnetic field makes it difficult to solve the time domain theoretical response by Fourier transform method, but the time domain response can be numerically calculated by Gaver-Stehfest inverse Lagrangian transform (G-S transform). Therefore, this paper selects the Gaver-Stehfest algorithm to realize the time-frequency conversion of the central loop. Through a series of derivation and conversion simplification, we can get the Gaver algorithm formula: (20) Stehfest improved the above equation using an interpolation formula whose calculation expression is: (21) where  $s_m = (\ln 2/t) \times m$ ,  $K_m$  is the filter coefficient of the G-S transform algorithm: (22) where  $k$  is the integer part of  $[(m+1)/2]$  and  $N$  is digital length of the computer. At a certain time, the time domain transient response  $h_z(t)$  is the sum of the product of the selected discrete  $F(s_m)$  and the coefficient  $K_m$ , thus realizing the frequency do-

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main to time domain conversion. Therefore, the Gaver-Stehfest algorithm is chosen to transform the central loop frequency domain response into a time domain response, in which 12-point filter coefficients are used in the G-S transform algorithm. The apparent resistivity problem Since the vertical magnetic field response  $H_z$  is used as input value to the neural network in the manuscript, the apparent resistivity formula is not listed in detail. Regarding the magnetic field strength and apparent resistivity, the method of defining all time apparent resistivity using the magnetic field strength (or magnetic induction) can better reflect the geoelectric model. Among them, when the magnetic resistivity time partial derivative or induced electromotive force is used to define the all time apparent resistivity, multiple solutions or no solutions will occur, and there are obvious false extremums. This method blurs the correct reflection of the formation parameters. The all time apparent resistivity defined by the magnetic field strength or the magnetic induction intensity is a single-valued function, and there is no false extremum. Therefore, the method of defining the apparent resistivity by using the magnetic field strength (or magnetic induction) can better reflect the geoelectric model. It is also meaningful to convert the induced voltage measured in the survey into a vertical magnetic field. Its detailed description of the all time apparent resistivity is as follows: 1) Definition of apparent resistivity of the central loop At present, there are many methods for defining the all time apparent resistivity of the transient electromagnetic method. According to the data source, it can be roughly divided into two types: based on the magnetic field strength (magnetic induction intensity) and based on the induced electromotive force. The transient response  $LHz \approx \frac{\partial H_z}{\partial t}$  at the center of the center loop in a uniform half-space is as shown in equations (2.51) and (2.52): (23) The expression of the magnetic induction and its time partial derivative is: (24) (25) The all time apparent resistivity can be expressed as: (26) When using the magnetic induction time partial derivative or the induced electromotive force to define the all time apparent resistivity, multiple solutions or no solutions will occur, and there are obvious false extremums. This method blurs the correct reflection of the formation parameters, and the magnetic field strength or The full-area apparent resistivity defined by magnetic

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induction is a single-valued function, and there is no false extremum. Therefore, it is better to use the magnetic field strength (or magnetic induction) to define the all time apparent resistivity. 2) Method of converting induced voltage into vertical magnetic field From the above analysis, it can be seen that the all time apparent resistivity defined by the magnetic field strength can better reflect the geoelectric model, therefore, it is very meaningful to convert the induced voltage measured into a vertical magnetic field in the exploration. The relationship between the center loop induced voltage  $V_z(t)$  measured by the transient instrument and the vertical magnetic field  $H_z(t)$  is: (27) Integrate on both sides of equation (27): (28) When the upper limit of the integral is the time variable  $t$  or the lower limit of the integral takes the time variable  $t$ , the above formula can be changed to: (29) (30) If  $H_z$  is calculated by equation (29),  $H_z(a)$  at time  $a \rightarrow 0$  is required, but due to the existence of turn-off time, an error will inevitably occur in the calculation, and as time increases, the relative error will continue. Increases will cause late response distortion. It can be seen from the response curve that when the time  $t$  is large, the response values of the vertical magnetic field and its time partial derivative tend to be zero, so the response value of the last sampling point can be replaced by 0. When  $b$  is large in the formula (30),  $H_z(b)=0$ , when  $t$  decreases continuously, the value of  $H_z(t)$  increases continuously, and the relative error also decreases. The error for early calculation can be neglected. The calculation formula is: (31)

2-There is no field data for the inversion as an example, which is very important. All calculation is synthetic. The manuscript can be published in this journal after my suggestion completed. (Note: Upon request I can provide a field data set to the Authors. I am running a project; the project includes TEM field measurement. ) (2) Thank you very much for your comments, a field example are added as follows. At the same time, we sincerely hope to get your TEM measured data set, we will be particularly grateful.

4.4 Field example analysis In order to test the effectiveness of the method, a transient electromagnetic vertical magnetic field ( $H_z$ ) with 10 measuring points at the 380m to 1280m of the No. 1 line from a mining area in Anhui Province was selected. After

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the data processing, the inversion was performed using the 3-layer neural network model in the previous section, and the results of BP and COPSOBP inversion were compared. Figure 13 shows the comparison between the surveyed data and the inversion data at 380m of the No. 2 line in the mining area. Figure 14 displays the pseudo-sections of the 10 sets of inversion data combined with the geological data interpolation smoothing. It can be seen from Fig. 14 that the first layer is a low resistivity ( $100\sim 200\ \Omega\cdot\text{m}$ ), which is inferred to be the second layer (T2g22) gray dolomite of the Middle Triassic old Malague section, with a thickness of about 200 m; the second layer is the second highest resistivity ( $300\sim 400\ \Omega\cdot\text{m}$ ), which is surmised to be the first layer (T2g21) dolomite of the Middle Triassic old Malaga section, with a thickness of about 400m; the third layer is high resistivity ( $600\sim 800\ \Omega\cdot\text{m}$ ), which is speculated to be the 6th layer (T2g16) limestone dolomite of the Middle Triassic old group. The results are basically consistent with the geological conditions of the mining area, indicating the feasibility and effectiveness of the neural network method. And the results of COPSOBP inversion are better than those of BP, which the inversion position is more accurate, the shape and spacing are clearer, and the resistivity of each layer is more consistent with the those of the actual geological model.

(a) BP (b) COPSOBP Figure 13. 1D inversion forward results. (a) BP; (b) COPSOBP.

(b)BP (b) COPSO-BP Figure 14. Inversion results of BP (a) and COPSO-BP (b).

Special thanks to you for your good comments.

We tried our best to improve the manuscript and made some changes in the manuscript. These changes will not influence the content and framework of the paper. And here we did not list the changes but marked in red in revised paper. We appreciate for Editors/Reviewers' warm work earnestly, and hope that the correction will meet with approval.

Once again, thank you very much for your comments and suggestions.

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Interactive comment on Nonlin. Processes Geophys. Discuss., <https://doi.org/10.5194/npg-2019-36>, 2019.

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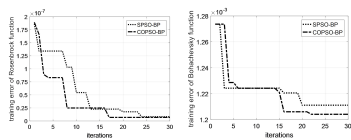


Fig. 1 Training error curves of SPSO-BP and COPSO-BP algorithms

Fig. 1.