

***Interactive comment on* “Competition between Chaotic Advection and Diffusion: Stirring and Mixing in a 3D Eddy Model” by G. J. Brett et al.**

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Author response to reviewer comments on “Competition between Chaotic Advection and Diffusion: Stirring and Mixing in a 3D Eddy Model”

To begin, we would like to thank all reviewers for their close reading and appreciative comments on this paper. It was quite gratifying to receive so many positive remarks. Below, we address the individual comments of each reviewer. Our responses are in italics. Line numbers in our responses refer to the revised paper draft (supplement), while those in the reviewer comments refer to the discussion paper version.

Reviewer 1

1. A sketch of the flow would be helpful when first discussed in detail, showing both

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the rotating flow, the Ekman layers, and the off-center perturbation.

A sketch of the flow was also requested by reviewer 3. A new first figure has been created for this request, which is the first figure attached. It shows the 3D cylinder with the direction of flow and labels indicating Ekman layers. Caption: Sketch of the qualitative velocity field, Eqn.s 7-9. Ekman layers at the top and bottom are where flow has a larger radial component. Ω is the rotation rate of the system. X_0 is the offset between the lid and cylinder rotational centers, as set for the Navier-Stokes simulations.

2. The Batchelor scale is a little difficult to follow when first presented at the beginning of section 3, but then there is an outstanding discussion of this in section 3.1 (on p. 11) with ample references. Perhaps move that discussion a little earlier.

Reviewers 2 and 3 also requested the start of this section be cleaned up. In the revised paper we have re-arranged section 3. We have moved the Batchelor scale discussion forward to the beginning of section 3 (lines 253–283), and we have moved the discussion of dimensionalization from the beginning of section 3 to after Okubo's diffusivity is introduced in section 3.1, which is where it becomes relevant.

3. I will admit that by the time I got halfway through section 5, I was beginning to fade. Although I think that the detail is useful overall, perhaps some trimming of section 5 would be helpful to the readability of the paper. But this isn't critical – it's fine if the authors leave it as is.

Reviewer 3 also commented that section 5 was challenging. This was indeed a difficult section to write and was the target of a number of revisions and reduction prior to submission. We took another look at it and feel that it would be difficult to condense further without sacrificing important content, but we went through and made a number of minor changes intended to make it a little easier to read:

Line 550: X_0 is clarified: "The symmetry-breaking perturbation is created by moving the central axis of the imposed surface lid stress a fraction of the radius X_0 from the

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cylinder axis

Line 565: Figure 9 reference now specifies panels a–c

Line 589: Changed “see Figure 10(h)” to “look ahead to Figure 10(h)”

Line 598 and Fig. 11 caption: We now include the diffusivity, k , in the description of the case we discuss.

Line 641 Changed “ κ_{eff}/k ” to “as measured by κ_{eff}/k ”

We also changed the color scheme of Figs 9-10 (10-11 in the revised version) and improved the quality of these figures to allow more accurate reading of the values.

Reviewer 2

1. Line 69: I would rather talk about important characteristic for the problem considered instead of a “person”. Something like: The terms “important” and “relevant” are somewhat subjective, and a particular aspect, such as the existence of barriers, that is of interest for one scientific question may not be so to another.

Changed to: The terms “important” and “relevant” are somewhat subjective, and a particular aspect, such as the existence of barriers, that is of interest for one scientific question may not be so for another.

2. Line 244: though

Changed, thank you! (Now on line 250)

3. Fig.2/Fig.3: The scale of the upper row of figures looks not equidistant in my viewer. It is also confusing that the lower plots have a scaling range and the upper ones do not. Further it is said in the caption that the simulations are from another work while in the text the simulations are claimed to be done within this study. This is a bit confusing.

The non-equidistant ticks in the top panels of Figs. 3 and 4 were due to problems in changing image format. In the revision, we have used higher-quality images and

removed the ticks.

The difference between the top and bottom panels in Figs 3 and 4 are that the top panels were computed using velocities from a dynamically-consistent numerical model, whereas bottom panels were computed using velocities from our analytic (non-dynamically consistent) model. This is now clarified in the caption and in the text. The purpose of these plots was to show that our analytic model (bottom panels) correctly captures the qualitative features of the dynamically-consistent solution (top panels).

In this paper we did not re-run the dynamically-consistent NS solver to get the top panels; we simply took these images from P2014. This is now clearly stated in lines 229-230 of the text. Since P2014 only computed Poincare sections but did not compute FTLEs, we have no color images in the top panels. For our analytic model in the bottom panels, however, we have computed both Poincare sections for comparison with the top panels, as well as FTLE fields, whose values we show using the colorbar. These FTLE values will be used in section 3 to compute the Batchelor scales.

The new caption for the first of these figures (3) now reads: "Structures in the kinematic model and dynamical simulation for Ekman numbers of 0.25 (a)(c) and 0.125 (b)(d). Top, (a)(b): Poincare maps from P2014 (their Fig. 10), resulting from a dynamically consistent numerical simulation. Bottom, (c)(d): Poincare maps (black) and largest FTLEs (color) resulting from our non-dynamically consistent kinematic analytic model, with $\epsilon = 0.01$ and x_0 either -0.5 (c) or -0.9 (d); in color, maximum FTLEs calculated for the kinematic model with integration time 400. In (d), red oval approximately separates the resonant and regular layers (inside) from the chaotic sea region (outside), with the blue line segment showing the width of the chaotic sea. The blue diamond shows the width of an island, which is also the width of the resonant layer."

4. Line 252: Maybe I missed it but was the chaotic layer thickness introduced before being used here? I feel like maybe it is necessary to revise the usage of chaotic sea, width of chaotic sea, chaotic layer and chaotic region, see also line 16 in the abstract.

A mere note would help easier reading.

Reviewer 1 also found the start of section 3 to be a bit confusing. Now, near the beginning (lines 260-268), we have: “If δ is larger than the structures in the flow induced by chaos, then diffusion will overcome advection and wipe out these structures. The structures of interest, induced by the deterministic, symmetry-breaking perturbation (see Fig.s 3–4) are the bands of chaos, called resonant layers, surrounding regular island chains (see blue diamond in Fig. 3d), and the chaotic sea region (outside the red oval in Fig. 3d) located near the cylinder perimeter and central axis, which are identified by visual inspection of Poincare sections. When we compare δ to these structures, we define their widths as the difference between distances from the central orbit, $(r,z)=(0.5,0.5)$, to the outermost/innermost part of the structure, measured in Poincare sections like Fig.s 3-4.”

5. Line 264: Should it not be equation (13)?

In fact, it should be equation (9), for the background azimuthal velocity of the kinematic model. This has been changed.

6. Line 273: Does it make sense to talk of a timescale of a non-dimensional timestep? In general I was sometimes confused by the varying usage of non-dimensional units and dimensional ones. Maybe it could be helpful to use only adimensional ones in the text and make a little table for the conversion?

Thank you for your suggestion on making the text more readable. We have added Table 1, figure 2 below, with the correspondence between dimensional and nondimensional values, and removed references to dimensional values of model variables in sections 3-5 (e.g. lines 364,367,461,463).

7. Line 319: Cauchy-Green.

Changed, thank you.

8. Line 341: $\gamma = \sigma$?

Several errors existed in this equation, which is derived in Appendix B. It is now corrected.

9. Line 349: I feel like there is some other reference missing (or not?). Did not Okubo just study up to a scale of 100km in that report?

You are correct, we have updated the upper limit (line 332).

10. Fig.5, caption: Which δ values? (22) or (15)? Even though it becomes clear studying the text it would be easier if it was stated. Just to be curious: What is the result for (15)?

These values are computed with Eqn. 22, which is now indicated in the caption. With Eqn. 15, the Batchelor scale is similar to or larger than the layer widths in all cases.

11. Line 364: Fig. S 2-3

These are in fact referencing figures (plural) 2 and 3, not supplementary figures. This matter has been corrected in the revision (line 363).

12. Line 366: 10-20 rotations <-are those the integration times for the FTLE?

The reviewer is correct. We have clarified the sentence in question as follows: "FTLEs were estimated over an integration time of 400; the range of FTLE magnitudes does not noticeably change when the integration time is decreased by half."

13. Line 377: "rotating can model" is it the standard name for the model used? Why not introduced before? It difficultates understanding using a new name.

This now reads "kinematic model"; thank you for pointing this out.

14. Line 421: pf→of

This has been changed, thank you.

15. Line 507: Year of citation of Shuckburgh, E. and Haynes, P. should be 2003.

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In this case, we are citing Haynes and Shuckburgh's work on the application of the Nakamura effective diffusivity to the atmosphere, which is described in a pair of papers in JGR in 2000, not the 2003 Shuckburgh and Haynes work on the quantitative applicability of the effective diffusivity in Physics of Fluids in 2003. (The latter is also relevant for our paper and is cited on line 519.)

16. Line 545: The numerical simulations are run using the solver NEK5000...

We have added "the solver", thank you.

17. Fig. 8: X_0 instead of epsilon in caption and in legend the x is small? Further I would find it really helpful for the comparison of the temporal evolution and the peaks of the different cases to have a grid in the background of the plots.

X_0 has replaced ϵ and x_0 , thank you. We have also added a grid.

18. Line 596: After "dye contours" put reference to Fig 10(e)?

We have referenced Fig 10i, thank you for demonstrating how confusing this can be without that reference.

19. Line 599: A caveat is that k_{eff} is a nonlocal property, the value of which at any point in space and time is influenced by processes occurring at all other locations having the same C at a distinct time t (?). This time dependence could also be explicitly noted in equation (25) to clarify. I must admit that I am still a bit confused about the details of the calculations of k_{eff} here. As I understand it the k_{eff} values are calculated at each time step from volumes of equal concentrations (and dC/dV is taken from the cumulative distribution of volumes with concentrations $c \leq C$ as in the reference [Shuckburgh and Haynes, 2003]). One then gets a function $k_{\text{eff}}(C, t)$. The plots of k_{eff} at fixed instances t would thus just be derived by finding the corresponding value of k_{eff} at that $C(t)$? Or is there any such thing as an equivalent latitude used here? I wonder why the two plots of $k_{\text{eff}}(t)$ and $C(t)$ look so different. The k_{eff} looks much more noisy. How does $k_{\text{eff}}(C, t=39)$ look like?

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You are correct about the calculation of k_{eff} . The plots of k_{eff} are noisier than those of C because the function $k_{eff}(C)$ is not very smooth: small variations in C can correspond to larger, non-monotonic changes in k_{eff} . This is now addressed in the text lines 600-604: “A caveat is that k_{eff} is a nonlocal property, so plots show the values $k_{eff}(C)$ mapped onto the locations on the sections with corresponding dye concentrations, C , while they are calculated using the distribution of C over the whole volume at that time. These mappings are noisier than the sections of C because the numerically computed $k_{eff}(C)$ is nonmonotonic and can have large changes with small changes in C .”

20. Line 607-608: Do the results depend on the details of the initial condition? What must be met to ensure that the results are independent?

In our simulations, we see a transition from the large-scale vertical gradient in tracer concentration to approximately toroidal tracer distribution after several overturning cycles. For an initial broad gradient in any direction, we expect the same realignment after the first few overturnings as the tracer is passively advected by the background velocity field. We believe, then, that the tracer distribution that exists at later times is somewhat independent of initial distribution. We have added this idea to the text, lines 615–620, as: “With no disturbance present ($X_0 = 0$) and $k = 10^{-4}$ (Fig. 10(b)), the initially horizontal lines of constant C have been advected by the axially symmetric overturning circulation such that contours of constant C are roughly aligned with the overturning streamfunction. For an initial broad gradient in any direction, we expect the same realignment after the first few overturnings as the tracer is passively advected by the background velocity field. We believe, then, that the tracer distribution that exists at later times is somewhat independent of initial distribution.” It would be interesting to test this, but one would have to do it over a range of tracer distributions. Our paper is quite long already, so this may have to be something to explore in the future.

21. Line 631: Thus the combined effect of smaller diffusivity and finer filaments (i.e., stronger tracer gradients) leads to more rapid mixing across tracer contours. This is my favorite insight of the analysis and it is, at first glance, counterintuitive to me and

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still makes so much sense.

Thank you.

22. Line 667: Here I am confused about the statement: A smaller diffusivity leads to less mixing (X2). Especially when compared to details of Fig. 8.

We agree with the reviewer that the wording of this sentence was indeed ambiguous. We have rewritten the sentence in question as follows (lines 680–681): “A smaller diffusivity leads to more filamentation (higher²) and highly elevated enhancement (much larger κ_{eff}).”

23. Line 681: I feel that pros and cons is a bit colloquial and would suggest advantages and disadvantages (or so). But that is just my personal opinion.

We have changed this line, thank you for marking it.

24. General comment 1: As a general remark to the Figures and their descriptions, there is quite some mixed usage of either left-middle-right-bottom-top and a,b,c,d,... Maybe it would become easier to read just using a,b,c,d,... Especially Fig.'s 8/9/10.

In the text we have replaced references by location to references by panel letters. In the actual captions of figures, we use positions of rows and columns in order to indicate the pattern of the panels- rows and columns generally have the same type of data or data from the same simulation shown. However, we now also note the panel letters to avoid confusion.

25. General comment 2: On a similar vein I also find the usages of the word turbulence, turbulent diffusivity, diffusion, eddy diffusion and similar expressions confusing too. I would try to avoid using these concepts interchangeably and only use those expressions that were defined before.

We have tried to clean up our lexicon. Both terms “eddy diffusion” and “eddy diffusivity” have been eliminated. We now consistently use terms “chaotic advection” and “turbu-

lent diffusion" to refer to the two dominant processes that influence tracer evolution. For example, the new abstract now reads:

"The importance of chaotic advection relative to turbulent diffusion is investigated in an idealized model of a 3D swirling and overturning ocean eddy. . . Turbulent diffusion is alternatively represented by: 1) an explicit, observation-based, scale-dependent diffusivity, 2) stochastic noise, added to a deterministic velocity field, or 3) explicit and implicit diffusion in a spectral numerical model of Navier–Stokes equations."

Reviewer 3

General comment 1: The methods are really well described but I believed some of the sections are too long. I would like the authors to focus on results and maybe relayed some of the methodology details to Appendix. For example, sec. 3-3.1 and add details to the results section in 3.2. Section 5 is also a bit hard to follow as the reader is asked to compare two figures, maybe a reorganization of the figures could improve the readability.

Reviewer 1 agreed that the structure of section 3 was not optimal and that section 5 was challenging. We have re-structured and streamlined section 3. Specifically, we have moved the Batchelor scale discussion forward to the beginning of section 3, and the discussion of dimensionalization from the beginning of section 3 to after Okubo's diffusivity is introduced in section 3.1.

Section 5 was indeed difficult to write and was the target of a number of revisions and reduction prior to submission. We took another look at it and feel that it would be difficult to condense further without sacrificing important content, but we went through and made a number of minor changes intended to make it a little easier to read:

Line 550: X_0 is clarified: "The symmetry-breaking perturbation is created by moving the central axis of the imposed surface lid stress a fraction of the radius X_0 from the cylinder axis."

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Line 565: Figure 9 reference now specifies panels (a)–(c)

Line 589: Changed “see Figure 10(h)” to “look ahead to Figure 10(h)”

Line 598 and Fig. 11 caption: We now include the diffusivity, k , in the description of the case we discuss.

Line 641 Changed “ κ_{eff}/k ” to “as measured by κ_{eff}/k ”

We also changed the color scheme of Figs 9-10 (10-11 in the revised version) and improved the quality of these figures to allow more accurate reading of the values. Finally, we now consistently refer to the subpanels in the multi-panel figures by their letters (a,b, . . .) instead of their location (middle, left, etc.).

2: Lines 55-60: the authors should take a look at “Material barriers to diffusive and stochastic transport” by G. Haller, D. Karrasch and F. Kogelbauer, which seeks transport barriers with no diffusion of tracers across it. Those structures could help extract the different regions analyzed in figure 11.

We thank the reviewer for the reference to a relevant paper and for the suggestion regarding figure 11. While we agree that it would be interesting to try re-doing the calculations presented for the slightly different regular region identified via this other technique, the resolution of the tracer field in our existing simulations is too low to allow for a precise calculation of K_{eff} within that exact island. Note that we only use Poincare sections as guidance for picking red and blue regions with qualitatively different behavior. We have added the following sentence to address this issue near the end of section 5, line 667: “While we used Poincare sections as guidance for defining regular and chaotic regions, other methods (for example, Haller et al., 2018) could be used instead for the more precise delineation of the phase space.”

3: Lines 575-580: is there a difference between x_0 and X_0 , and later in the caption of Fig.8 there is also an epsilon?

Yes, there is a difference. As noted in the first paragraph of section 2.2 (l215-220), x_0

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is a parameter for the offset in the perturbation for the kinematic model, while X_0 is the offset in the NS simulation. Epsilon is the strength of the perturbation for the kinematic model. In the caption of figure 8 the epsilon should be X_0 ; this has been corrected. We have also labeled X_0 in the new figure (now Figure 1) requested by the first reviewer.

4: Lines 771-774: 3D dye released and tracking seem almost like an impossible task, especially when the tracers have to be followed for multiple days. Right now, none of those methods can be calculated with observation data. Is there any plan for the applications of such analysis to 3D model outputs (ECCO, HYCOM, etc.) that assimilate data from floats, drifters, CTD casts, etc.? An analysis performed for example on a Loop Current or Agulhas Current eddy would be interesting.

We thank the reviewer for the comment and suggestion. We agree that any application to the ocean in 3D is extraordinarily challenging for any of our measures. It would be quite interesting to apply our analysis to data-assimilative models, but that is outside the scope of our work. There is also the question of whether any of the cited models can reproduce the vertical velocity field correctly. Often, a certain degree of horizontal averaging is needed to get a vertical velocity that looks sensible.

5. Line 140: the streamfunction is not intuitive at all, I believed a sketch of the flow in section two could improve the readability.

To better relate the streamfunction to the velocities, we have added at its introduction (line 145) "The streamfunction relates to the velocities by the negative z-derivative of Ψ being the radial velocity and the radial derivative being the vertical velocity." A sketch of the flow was also requested by reviewer 1 and is now presented as the first figure- it is included in the response there, the first one in this document.

6. Line 299: for a for a

Now one for a, thank you.

7. Line 319: Cauchy-Green

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Cauchy, thank you.

8. Line 421: move out pf

Of, thank you.

9. Line 445: a scale with square root of time could be included in the left panels of figure 7

The square root of time curve has been added to panel (a).

10. Equation 20: I believe it should be σ instead of γ ?

Several errors existed in this equation, which is derived in Appendix B. It is now corrected.

Reviewer 4

Here we paraphrase the comments in order to shorten them and address each individually.

1. The kinematic model assumes 1) there is a separation of scales between the background flow and the turbulent perturbation; 2) the background flow is steady; and 3) the turbulence can be parameterized as a diffusive process (in the simulations of this model there is no actual turbulent flow). It is my view that the validity of almost all of the conclusions/inferences presented in the paper is limited to flows for which assumptions 1) and 2) (again, maybe also 3)) apply. None of these assumptions apply to the NS simulations. Indeed, there is no guarantee that those simulations approach anything resembling a quasi-steady flow. Assumption 2) is both especially important and especially restrictive, and this should be stated clearly by the authors. It is assumption 2) – together with incompressibility – that leads to the underlying structure of a 2 dof autonomous Hamiltonian system.

You are correct that a separation in spatial and temporal scales between the background flow and the turbulent perturbation is necessary for the analysis we perform.

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This is explicitly stated in the introduction (lines 58–68): “The relevance of chaotic advection for the stirring of material within geophysical flows would appear to rest on several criteria. The first is that the flow field contain persistent, long-lived (on the time-scale of interest) features such as gyres, eddies and jets, that by themselves generate regions of elevated stirring as well as separating barriers. Secondly, the stirring within these regions should be at least as important as that due to smaller scale, intermittent features (i.e. small scale turbulence). Third, the barriers that exist in the absence of small-scale turbulence should retain meaning as suppressors of exchange between the rapidly-stirred regions in the presence of the small-scale turbulence. For the flow considered in this paper the first aspect has been investigated and shown to be true (citations); this work concentrates on investigating the second and third aspects.”

As for the NS simulations, they do reach a nearly steady flow, as have laboratory experiments with similar setups (e.g. Fountain et al. 2001). In our work, NS simulations produced a circulation that was observed to be steady over hundreds of azimuthal cycling times, as evidenced by the replication of periodic orbits in the stroboscopic sections in the top panels (labelled a,c) of our figs. 3 and 4 (previously 2 and 3). Please also see Pratt et al., 2014 for more examples of NS-based Poincare sections over a wide range of parameters.

We have added to the conclusion (lines 792-794) “Although the focus of this current paper is on the behavior of a steady 3D eddy flow subject to a turbulent diffusion, similar results are expected to hold for 3D eddy flows with time-periodic and time-quasiperiodic behavior.” To expand on that idea, note that treatment of a time-periodic 3D eddy flow (but without the focus on advection vs diffusion) is described in Rypina et al. (2015), who used theoretical arguments, analytic kinematic model and NS simulations to study Lagrangian transport and transport barriers arising in a time-dependent 3d idealized eddy. We could have carried out the same suite of experiments for that time-dependent flow as here, invoking the same assumptions of time scale separation and parameterization of turbulence as a diffusive process. So one does not lose the

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features induced by chaotic advection just because of time dependence. Our hope is to analyze time-dependent and otherwise more complex flows in the future using the presented set of tools, and to inspire others to consider our measures of the relative impacts of chaotic advection and turbulence or diffusion in other flows. Note also that a flow that varies on a significantly longer timescale than more intermittent perturbations could be amenable to analysis similar to the steady case.

2. In many cases throughout the text the authors make statements about exponential stretching, exponential growth, positive Lyapunov exponents, etc. The authors should be a bit more careful about saying that these behaviors are average behaviors for long times.

We agree with the reviewer and in the revised paper we now avoid such non-rigorous statements. Instead, we use terms akin to “fast chaotic-advection-induced separation/stretching” (lines 445, 482, for example) and phrases like “average exponential growth, as measured by FTLEs” (lines 256, 286, 440, 745). We have also rewritten the sentence introducing FTLEs as follows (lines 292-293): “The FTLE quantifies the average exponential separation rate between a trajectory and its close neighbors over a finite time interval.”

3. For the trajectory integrations in the kinematic model with added stochasticity, the algorithm that the authors use to integrate the stochastic differential equation, Eq 23, is quite crude; there are simple explicit integration schemes for stochastic differential equations (SDEs). (Does the mystery factor of 1/3 described on lines 405-407 somehow account for the fact that a Runge-Kutta algorithm is trying to mimic a real SDE integrator?)

Yes, we used a very simple method for integrating a stochastic process. Other integration schemes might provide a more accurate solution. However, we carefully tested that its mean and standard deviation behaved properly over time without a background velocity before applying it. The stochastic perturbations are added to the deterministic

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velocity at each full timestep. The 1/3 factor is due to the fourth-order integration function, which estimates the next point using the weighted sum of estimates of the velocity at the current position (v_1 , weight 1/6), the halfway point estimated from the current position (v_2 , weight 1/3), the halfway point estimated using v_2 (v_3 , weight 1/3), and the final point estimated using v_3 (v_4 , weight 1/6). Only v_1 and v_4 include stochastic additions, leading to the 1/3 factor. We have added the following at lines 393–408 to clarify: “Using the described stochastic perturbation, although it is quite simple, with $U_{bi} = 0$ or a constant, the variance of a set of trajectories grows linearly in time, while the standard deviation grows linearly with the square root of time, as expected for diffusion. . . This diffusivity requires a certain step size s for the stochastic perturbation, which relates to the distribution of u' by $s = \sigma \Delta t / 3$, with σ the standard deviation of u' , Δt the numerical timestep (0.01), and the factor of 3 due to the details of a fourth-order Runge–Kutta integration. The next position, using this method, is estimated using the weighted sum of estimates of the velocity at the current position (v_1 , weight 1/6), the halfway point estimated from the current position (v_2 , weight 1/3), the halfway point estimated using v_2 (v_3 , weight 1/3), and the final point estimated using v_3 (v_4 , weight 1/6). Only v_1 and v_4 include stochastic additions, leading to the 1/3 factor.”

Please also note the supplement to this comment:

<https://www.nonlin-processes-geophys-discuss.net/npg-2018-54/npg-2018-54-AC1-supplement.pdf>

Interactive comment on Nonlin. Processes Geophys. Discuss., <https://doi.org/10.5194/npg-2018-54>, 2018.

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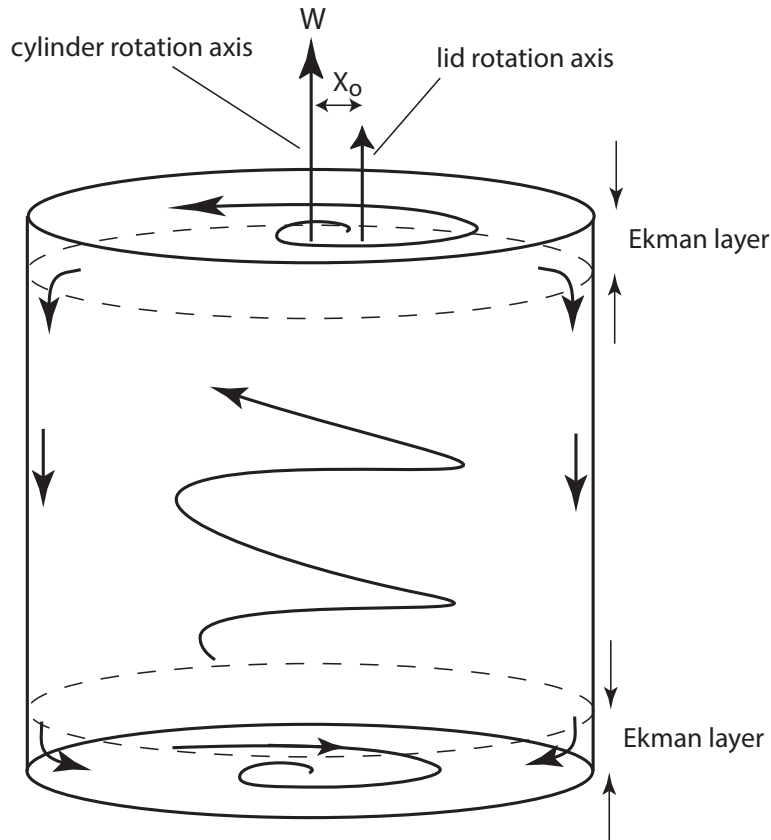


Fig. 1. Sketch of the qualitative velocity field, Eqn.s 7-9. Ekman layers at the top and bottom are where flow has a larger radial component. Ω is the rotation rate of the system. X_0 is the offset between the

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Variable	Nondimensional Value	Scaling factor	Dimensional value, E=0.25			
			E=0.25	E=0.125	E=0.02	E=0.0005
δ_E	a/\sqrt{E}	40m	40m	40m	40m	
H	1	$a\delta_E/\sqrt{E}$	80m	113m	283m	1789m
u	0.01–0.1	1m/s	0.01–0.1m/s	0.01–0.1m/s	0.01–0.1m/s	0.01–0.1m/s
w	$2 \cdot 10^{-4}$ –0.05	1m/s	0.005–0.05m/s	0.003–0.04m/s	0.001–0.014m/s	$2 \cdot 10^{-4}$ – $2 \cdot 10^{-3}$ m/s
timestep	1 (1000)	$H/1\text{ms}^{-1}$	84s (23h)	113s (31h)	283s (3.3d)	1789s (20.7d)
winding time	20–200	time	28min–4.6hr	39min–6.6hr	1.5–16.5hr	3.3–33hr
overturning time	30–400	time	42min–9h	1–12h	2–31h	15h–8d
κ	e.g. 10^{-5}	$H\text{m}^2\text{s}^{-1}$	$8 \cdot 10^{-4}\text{m}^2\text{s}^{-1}$	$1.1 \cdot 10^{-3}\text{m}^2\text{s}^{-1}$	$2.8 \cdot 10^{-3}\text{m}^2\text{s}^{-1}$	$1.8 \cdot 10^{-2}\text{m}^2\text{s}^{-1}$

Table 1. Nondimensional variables, their scale factors, and their dimensional equivalents.

Fig. 2. Nondimensional variables, their scale factors, and their dimensional equivalents.

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