

1 **Ion acceleration at dipolarization fronts associated with**
2 **interchange instability in the magnetotail**

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13

14 **Abstract** It has been confirmed that dipolarization fronts (DFs) can be a
15 result from the existence of interchange instability in the magnetotail. In
16 this paper, we used a Hall MHD model to simulate the evolution of the
17 interchange instability, which produces DFs on the leading edge. A test
18 particle simulation was performed to study the physical phenomenon of
19 ion acceleration on DF. Numerical simulation indicates that particles,
20 with 90-degree pitch angle and initially satisfying the initial power law
21 energy distribution $F \sim (1 + h/\kappa T_0)^{-\kappa-1}$ ($\kappa = 5$, $T_0 = 1.5$ keV and h
22 from 1 keV to 10 keV), move towards the earthward and dawnward and

23 then drift to the tail. The DF-reflected ion population on the duskside
24 appears earlier as a consequence of the asymmetric Hall electric field.
25 Ions, with dawn-dusk asymmetric semicircle behind the DF, may tend to
26 be accelerated to a higher energy ($>6\text{keV}$). These high-energy particles
27 are eventually concentrated in the dawnside. Ions experience effective
28 acceleration by the dawnward electric field E_y while they drift through the
29 dawn flank of the front towards the tail.
30

31 **Introduction**

32 Earthward moving high-speed plasma flows, which are called bursty bulk
33 flows (BBFs), play a vital important role in carrying significant amounts
34 of mass, energy, and magnetic flux from the reconnection region to the
35 near-Earth magnetotail (Angelopoulos et al., 1994). BBFs are often
36 accompanied with a strong (~ 10 nT), abrupt (several seconds), transient
37 enhancement of the magnetic field component B_z in the leading part,
38 known as a dipolarization front (DF) (Nakamura et al., 2009; Sergeev et
39 al., 2009; Fu et al., 2012a). Ahead of the DF, a minor B_z dip usually be
40 observed by THEMIS and MMS (Runov et al., 2009; Schmid et al., 2016),
41 which may be typically interpreted as strong diamagnetic currents caused
42 by a plasma pressure drop over the front or magnetic flux tube or
43 transient reconnection (Kiehas et al., 2009; Ge et al., 2011; Schmid et al.,
44 2011). Simulations have suggested that the magnetic energy would be
45 transferred to plasma on the DF layer in the B_z dip region ahead of
46 trailing fronts (Lu et al., 2017). Many of studies show that the passage of
47 a magnetic island (Ohtani et al., 2004), jet braking (Birn et al., 2011),
48 transient reconnection (Sitnov et al., 2009; Fu et al., 2013), and/or the
49 interchange/ballooning instability (Guzdar et al., 2010; Pritchett and
50 Coroniti, 2013) may account for DF generation. Both Cluster and MMS
51 observed that DFs propagate not only earthward but also tailward, since
52 the fast-moving DFs are compressed and reflected, three quarters of the

53 DFs propagate earthward and about one quarter tailward (Zhou et al.,
54 2011; Nakamura et al., 2013; Huang et al., 2015; Schmid et al., 2016).
55 Spacecraft observations showed that the sudden energy increase in
56 charged particle fluxes at DFs from tens to hundreds of keV in the
57 magnetotail (Runov et al., 2011; Zhou et al., 2010; Fu et al., 2011; Li et
58 al., 2011; Artemyev et al., 2012). A series of studies have been conducted
59 to understand the signatures of DFs and particles, as well as the particle
60 acceleration mechanisms on the DFs. Li et al., (2011) studied the force
61 balance between the Maxwell tension and the total pressure gradient
62 surrounding the DF and found that the imbalance between the curvature
63 force density and the pressure gradient force density would lead to the
64 flux tube acceleration. Ions, essentially nonadiabatic in the magnetotail,
65 can be directly accelerated by the electric field produced by earthward
66 convection of the front, such as due to surfing acceleration or shock drift
67 acceleration (Birn et al., 2012, 2013; Ukhorskiy et al., 2013; Artemyev et
68 al., 2014). Electrons, comparatively adiabatic over most of their orbits,
69 can be accelerated through betatron and Fermi process (Birn et al., 2004,
70 2012). It is noticed that the magnetic field amplitude behind DF is much
71 greater than that ahead of it, Zhou et al. (2011, 2014) obtained that the
72 earthward moving front can reflect and accelerate ions. Ukhorskiy et al.
73 (2013, 2017) took the magnetic field component B_z for different areas
74 and situations into account, revealing a new robust acceleration

75 mechanism enabled by stable trapping of ions. In most cases, ions are
76 energized by combined actions from different acceleration mechanisms.
77 Nevertheless, the physical processes that generate suprathermal particles
78 are not yet fully understood.

79 On the simulation ground, previous two-dimensional simulations just
80 unveil large scale physical process concerning DFs, in their models, the
81 electric field (most of them are derived from $-V \times B$) is assumed to be
82 solely in the y direction behind DFs (Ukhorskiy et al., 2012; Greco et al.,
83 2014; Zhou et al., 2014). It has been found that the spatial scale of DFs in
84 the dawn-dusk direction is about 1-3 R_E and its thickness is on the order
85 of the ion inertial length (Runov et al., 2011; Schmid et al., 2011), which
86 would be between 500 and 1000 km. In the sub-ion scale, there is an
87 electric field directed normal to the DF. The frozen-in condition is broken
88 at the DF and the electric field is mainly attributed by the Hall and
89 electron pressure gradient terms, with the Hall term dominants (Fu et al.,
90 2012b; Lu et al., 2013; Lu et al., 2015). Therefore, the Hall MHD model
91 is necessary to obtain the Hall electric field, which may determine the
92 electric system on DFs.

93 Lu et al. (2013) have successfully simulated the DF associated with
94 interchange instability in the magnetotail and the trend of simulated
95 physical variables are in good agreement with observations. In this paper,
96 we improve the simulation model in order to study how the Hall electric

97 field on DFs acts on the particle trajectories and ion energizations. Since
98 the DF would be produced by temporal evolution of interchange
99 instability self-consistently through our Hall MHD simulation, it would
100 be meaningful to understand the ion acceleration mechanism associated
101 with the interchange instability in the magnetotail.

102

103 **Theoretical and Numerical Model**

104 Numerical simulations have proved that the existence of interchange
105 instability triggered by the tailward gradient of thermal pressure and the
106 earthward magnetic curvature force is a possible generation mechanism
107 of the DFs in the magnetotail (Guzdar et al., 2010). Based on the Hall
108 MHD model associated with interchange instability (Lu et al., 2013), we
109 conducted test particle simulations to track ion trajectories backward in
110 time by running the simulation with positive time step then check the
111 time history of the trajectories of selected particles.

112 Our simulation was performed by two steps, the first is to establish a
113 more realistic DF to get particle motion background. The other is to place
114 test particles and track their trajectories.

115 The simulation coordinate system is defined with the x-axis pointing
116 away from the Earth, the y-axis pointing from dusk to dawn, and the
117 z-axis pointing northward (Guzdar et al., 2010, Figure 1). The breaking of
118 the earthward flow together with the curvature of the vertical field leads

119 to an effective gravity g away from the earth. Dimensional units are based
 120 on a magnetic field of 10 nT, the Alfvén velocity of 500 km/s, and
 121 reference length of $1 R_E$ leading to a time unit of ~ 13 s, an electric field of
 122 5 mV/m.

123 The dimensionless model with an effective gravity is as follows:

$$\begin{aligned}
 & \frac{\partial}{\partial t} \begin{bmatrix} \rho \\ \rho \mathbf{U} \\ \mathbf{B} \\ \rho e_t \end{bmatrix} + \nabla \cdot \begin{bmatrix} \rho \mathbf{U} \\ \rho \mathbf{U} \mathbf{U} + P \mathbf{I} - \frac{\mathbf{B} \mathbf{B}}{\mu_0} \\ \mathbf{U} \mathbf{B} - \mathbf{B} \mathbf{U} \\ (\rho e_t + P) \mathbf{U} - \frac{\mathbf{B}}{\mu_0} (\mathbf{U} \cdot \mathbf{B}) \end{bmatrix} = \begin{bmatrix} 0 \\ \mathbf{g} \\ 0 \\ \mathbf{g} \cdot \mathbf{U} \end{bmatrix} + \\
 124 & d_i \begin{bmatrix} 0 \\ 0 \\ -\frac{1}{\mu_0} \nabla \times \left(\frac{\nabla \times \mathbf{B} \times \mathbf{B}}{\rho} \right) \\ -\frac{1}{\mu_0^2} \mathbf{B} \cdot \left[\nabla \times \left(\frac{\nabla \times \mathbf{B} \times \mathbf{B}}{\rho} \right) \right] \end{bmatrix} + d_i \begin{bmatrix} 0 \\ 0 \\ -\frac{1}{\mu_0} \nabla \times \left(\frac{\nabla p_e}{\rho} \right) \\ -\frac{1}{\mu_0^2} \mathbf{B} \cdot \left[\nabla \times \left(\frac{\nabla p_e}{\rho} \right) \right] \end{bmatrix} \quad (1)
 \end{aligned}$$

125 Where $P = p + \mathbf{B}^2/2\mu_0$, \mathbf{U} and \mathbf{B} are velocity vector and magnetic
 126 field vector, respectively, $\rho e_t = \rho \mathbf{U}^2/2 + p/(\gamma - 1) + \mathbf{B}^2/2\mu_0$,
 127 $\mathbf{g} = [\beta \rho g_x/2, 0, 0]^T$, β is plasma beta, g_x is the effective
 128 gravitational force in x direction. In equation (1), the second and third
 129 terms on the right-hand side represent the Hall effect and the electron
 130 pressure gradient, respectively. In our present numerical cases, we
 131 postulate that plasma is under isothermal conditions with an isothermal
 132 equation of state $p = \beta \rho/2$ and take the adiabatic exponent $\gamma = 5/3$.
 133 The ion inertial length $d_i = (m_i/\mu_0 e^2 Z^2 L^2 n_i)^{1/2}$, given the reference
 134 length $L = 1 R_E$, the dimensionless ion inertial length is taken as

135 $d_i \approx 0.1$. Electron pressure p_e is taken as $p/6$, because the ion
 136 temperature is 5 times that of electron temperature (Baumjohann et al.,
 137 1989; Artemyev et al., 2011).

138 As for initial conditions, the quasi-stationary equilibrium built by the
 139 plasma pressure and effective gravity g (see equation (2)) (Guzdar et al.
 140 2010 and Lu et al. 2013, 2015) is theoretically reasonable.

$$141 \quad \hat{g} \frac{\beta}{2} \rho = \frac{\partial}{\partial x} \left(\frac{\beta}{2} \rho + \frac{B_z^2}{2} \right) \quad (2)$$

142 It should be noticed that the dawn-dusk and earthward electric field
 143 components averagely, increase to ~ 5 mV/m along with the transient B_z
 144 increase and in some events, the electric field increase exceeded 10
 145 mV/m (Runov et al., 2009, 2011; Schmid, D., et al. 2016). However, the
 146 electric fields calculated by the Hall MHD model in Lu et al. (2013) are
 147 smaller than the observations (see Lu et al., 2013, for a typical
 148 dipolarization event at $x = -10 R_E$ in the equatorial plane, they set $B_0 =$
 149 15 nT, leading to B_z changed from 10.2 nT to 16.8 nT after DF
 150 propagation. The electric field components E_x and E_y are both less than
 151 3 mV/m). So, it is reasonable that we improve the initial conditions to
 152 obtain a realistic electric field, which plays a vital important role in ion
 153 energization.

154 We take the initial conditions as follows:

$$155 \quad \rho(x) = \frac{1}{2} (\rho_L + \rho_R) - \frac{1}{2} (\rho_L - \rho_R) \tanh \left(\frac{x}{l} \right) \quad (3)$$

$$\begin{cases}
B_Z(x) = 0.28x + 0.7535 & (x \leq -0.38) \\
B_Z(x) = 1.5 + \tanh\left(\frac{x}{0.3}\right) & (-0.38 < x < 0.4) \\
B_Z(x) = 0.14x + 2.314 & (x \geq 0.4)
\end{cases} \quad (4)$$

157 Given the generalized Ohm's law, we use a piecewise function to
158 describe B_Z so as to obtain a strong electric field. In equation (3),
159 $\rho_L = 2$ and $\rho_R = 1$ are the density closer to and away from the Earth,
160 respectively and the characteristic scale $l = 0.2 R_E$. The numbers of grid
161 cells in x and y directions are set 301 and 201, respectively.

162 We solved equation (1) by adopting the second-order upwind total
163 variation diminishing scheme. The simulation box is $4 R_E$ and $1.5 R_E$ in
164 the direction of x and y , respectively. The x boundary is assumed to be
165 zero for all perturbed quantities and the y boundary is to be periodic.

166 As the second simulation step, the control equations for ion motion
167 should be given. Typically, the drift approximation breaks down in
168 terms of ion motion in magnetotail. The dimensionless equations of
169 motion are given by

$$\begin{cases}
\frac{d\mathbf{r}}{dt} = \mathbf{u} \\
\frac{d\mathbf{u}}{dt} = \alpha(\mathbf{E} + \mathbf{V} \times \mathbf{B})
\end{cases} \quad (5)$$

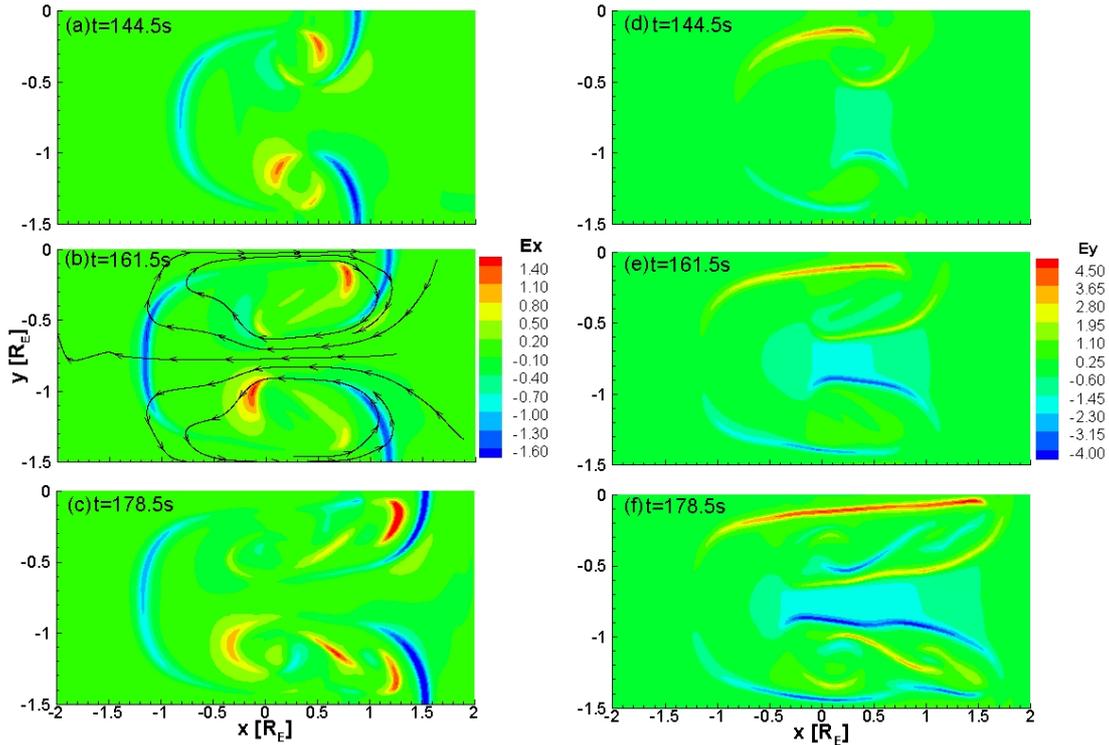
171 where \mathbf{r} is the particle position, \mathbf{u} is the particle velocity, the
172 dimensional parameter $\alpha = \frac{1}{d_i} \approx 10$.

173

174 **Simulation Results**

175 From 0s to 221s, the simulation experienced a pre-onset phase, during

176 which the DF formed as a consequence of effective gravity g interaction
177 with plasma density gradient. In order to be more realistic, we set up the
178 time interval from 221s to 286s as the acceleration period of the particles.
179 Figure 1 shows the evolution of the electric field in the $z = 0$ plane and
180 black lines indicate streamlines, one can clearly see that the DF moves
181 toward the Earth as time passes by. From Figure 1b it can be seen that the
182 earthward flows coexisted with the tailward flows of the dawn and dusk
183 edges, as a consequence two vortex flow pattern appeared. Figure 1 also
184 shows that the electric field components E_x and E_y are both normal to the
185 front, which is consistent with the observation and simulation (Fu et al.,
186 2012b; Lu et al., 2013). It should be noticed that the total electric field E
187 is asymmetrically distributed on the DF, with a stronger dawnside electric
188 field in Figure 1. This asymmetry can be interpreted as a subsequence of
189 Lorentz force, according to the Hall electric field. Consequently, the
190 Lorentz force along the tangent plane of DF associated with the motions
191 of the decoupled ions leads to the asymmetry of the “mushroom” pattern
192 (Lu et al. 2013).

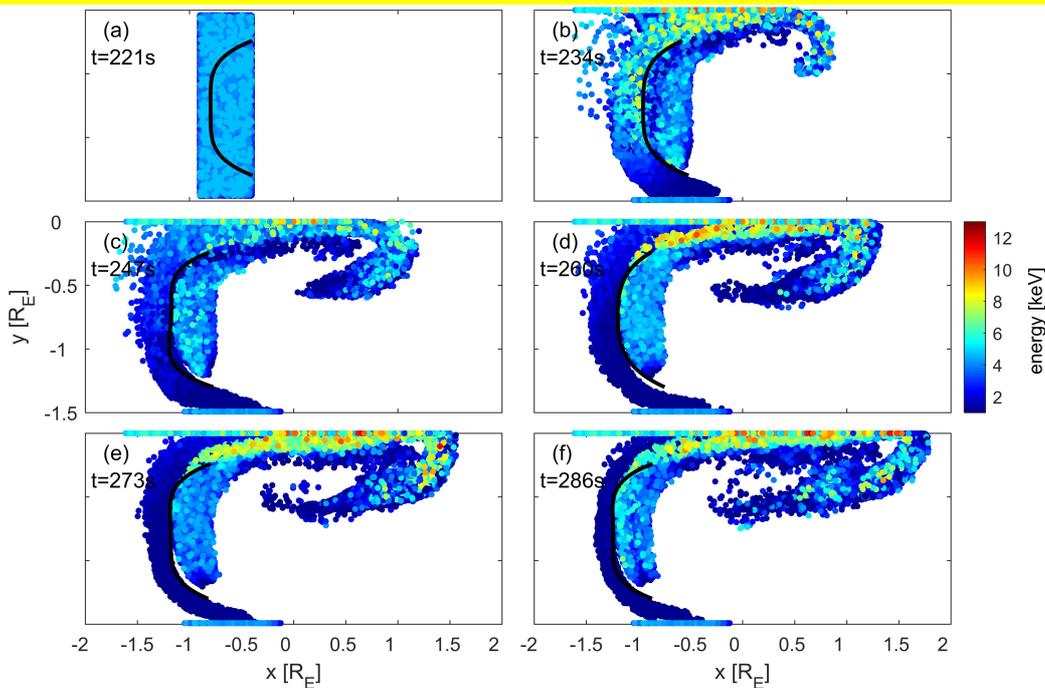


193

194 **Figure 1.** Evolution of the electric field E_x (a-c) and E_y (d-f), black line in
 195 (b) indicate streamlines

196 At $t = 144.5s$, we numerically distribute test particles (80000 ions in total)
 197 around the DF (the launch region with $x = -0.9 R_E \sim -0.4 R_E$, $y = -1.46 R_E$
 198 $\sim -0.04 R_E$) with the initial power law energy distribution $F \sim (1 +$
 199 $h/\kappa T_0)^{-\kappa-1}$ (we take $\kappa = 5$, $T_0 = 1.5 keV$ and h from 1 keV to 10 keV)
 200 (Artemyev et al., 2015). Figure 2 exhibits the spatial distribution of ions
 201 at a given moment. The energy of particles is marked with color and
 202 black lines indicate the position of DFs. As time passes by, the ions
 203 behind the DF accelerate and transport to the dawn flank of the DF,
 204 resulting in the reduction of the ion density behind the DF. It should be
 205 pointed that the ions will remain stationary at the boundary once they
 206 move to the simulated boundary. We investigated the characteristics of

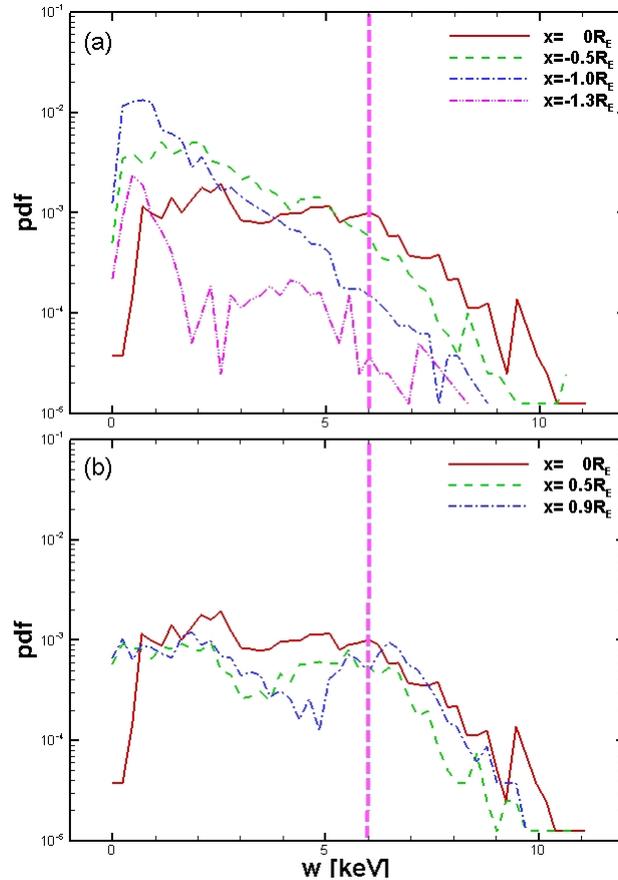
207 ions trajectories and found that the behaviors of ions consist of two parts
 208 (not shown), one is forced by the electric field E_x at the leading edge of
 209 the front, resulting in earthward motion and dawnward drift. Another is
 210 due to the electric field E_y at the dawn flank of the DF, leading to tailward
 211 drift. These results are consistent with observations and simulations
 212 (Nakamura et al., 2002; Greco et al., 2014; Zhou et al., 2011, 2014).
 213 Therefore, the electric field on the DF (Figure 1a), mainly produced by
 214 Hall term and always normal to the front (Fu et al., 2012b; Lu et al.,
 215 2013), makes the particles move in the way described above. Statistical
 216 analysis of the ions energy in Figure 2 indicates that the maximum energy
 217 is about 12 keV. In order to better distinguish particles from different
 218 energy, we assumed that the ions with the final energy greater than 6 keV
 219 are high-energy particles.



220

221 **Figure 2.** Test particle simulations of ion energization at the DF, particle

222 energy is indicated with color and black line represents the position of the
 223 DF

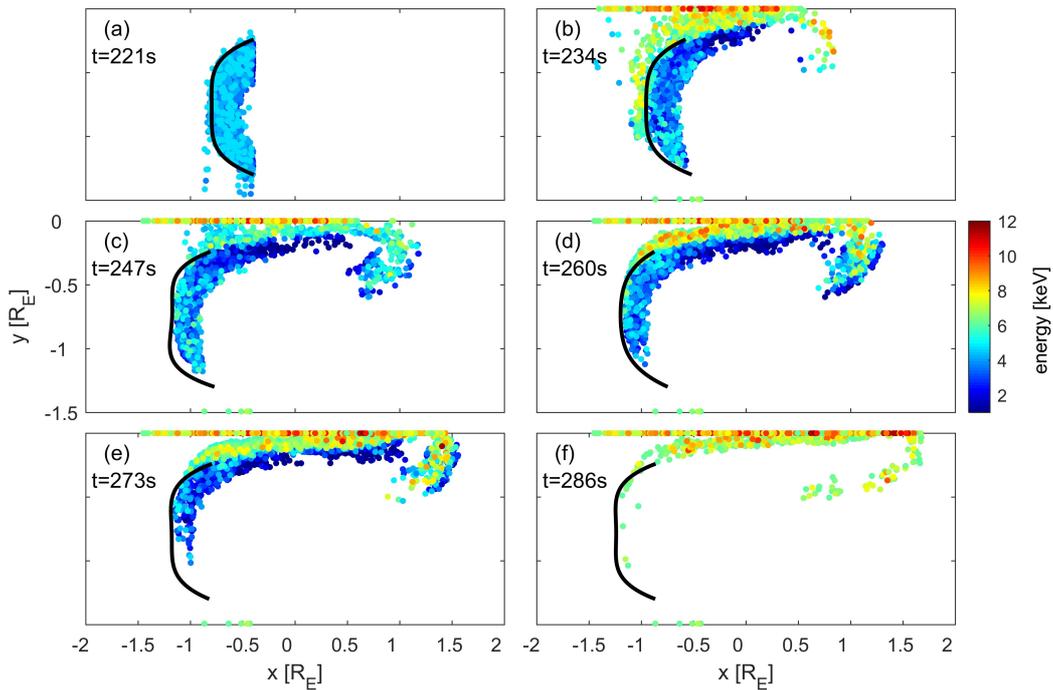


224
 225 **Figure 3.** PDFs of particle energy computed at the region of (a) $x < 0 R_E$
 226 and (b) $x > 0 R_E$. The red dotted line mark the high energy demarcation
 227 line 6 keV.

228 Figure 3 gives the probability density function (PDF) of particle energy at
 229 different x positions at final time. In order to better distinguish the curves
 230 of different x distances, we show the results in two figures according to
 231 different region in x direction. It can be seen from Figure 3b that the
 232 high-energy particles are assembled in the region of $x > -0.5 R_E$ whereas
 233 Figure 3a shows that the low energy ($\sim 2\text{keV}$) ions are concentrated in the

234 region of $x < -0.5 R_E$. At $x = 0 R_E$, ion energy is evenly distributed
 235 between 1 keV and 6 keV practically. In combination with Figure 2, we
 236 can further obtain that almost all the high-energy particles gathered in the
 237 dawnside of $x > -0.5 R_E$ region. It implies that ion acceleration is more
 238 effective at the dawnside of DF.

239 To have a statistical description of high-energy ions, we picked out
 240 high-energy particles from the total number. The simulation results are
 241 shown in Figure 4 with ions energy marked with different color. It
 242 appears that high energy particles, accounting for 7.45 percent, mainly
 243 gathering at the dawnside of the DF.



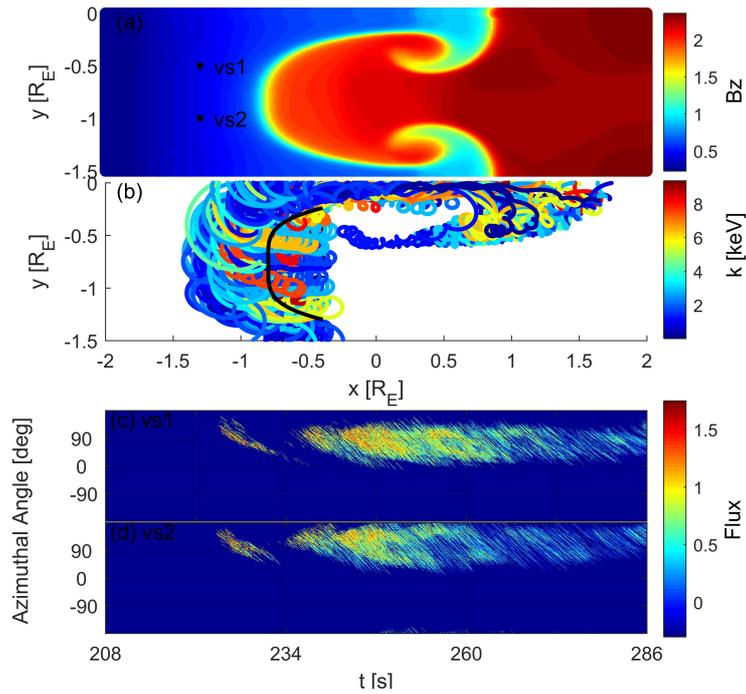
244

245 **Figure 4.** Snapshots of high-energy ions at specific moment of the
 246 simulation, black line represents the pre-region position of the DF
 247 Figure 4a shows that the initial position of high-energy particles is
 248 roughly an asymmetric semicircle whereas the dawnside area is wider

249 than the duskside, which means that more ions are accelerated in the
250 dawnside than in the duskside. Compared with Figure 2, however, we can
251 intuitively infer that ions with initial positions ahead of or behind and
252 away from the front would not obtain great energization. The ions with
253 initial positions ahead of the front are forced by the E_x of pre-DF region
254 and they move earthward and dawnward with a larger gyration radius due
255 to smaller ambient magnetic B_z , thus can't be accelerated by the
256 dawnside electric field E_y . The ions with initial positions behind the front
257 move with it and always stay behind the DF during the whole evolution
258 period of DF. As a result, there exist no strong fields to energized ions.
259 That is to say, only particles which diverted to the dawnside region closer
260 to the front can be effectively accelerated.

261 In a previous paper, Zhou et al. (2014) inferred that the more energized
262 DF-reflected ions originating from the duskside of the DF would be able
263 to reach farther into the ambient. In their model the ions would have been
264 accelerated more significantly in the DF duskside than in its dawnside
265 which is due to the y displacements behind the convex DF (Zhou et al.,
266 2014 Figure 3). However, observations and numerical simulations
267 indicate that the convective electric field behind the front is smaller than
268 the Hall term on the DF on the spatial scale of ion inertial length (Fu et al.,
269 2012b). Therefore, the explanation based on the convective electric field
270 E_y was inappropriate in our model. Figure 4 has already illustrated that

271 the ion acceleration process is on the dawnside. In addition, statistical
 272 analysis of 5961 high-energy ions indicates that 2004 ions were traced to
 273 the duskside of the DF, about 34 % of the total high-energy particles. The
 274 source area of ions reaches closer to the Earth, as shown in Figure5.



275
 276 **Figure 5.** Simulation results of ion differential energy fluxes in the 1-20
 277 keV energy range at different location. (a) Positions of virtual satellites.
 278 (b) Ions with initial positions on different y locations moving with the
 279 dipolarization front, the DF at $t = 221$ s was marked with black solid line.
 280 Kinetic energy at final moment is marked with color. (c and d)
 281 Differential energy fluxes at dawnside (vs1) and duskside (vs2),
 282 respectively, as the functions of equatorial azimuthal angle and time.
 283 The dark spots in Figure 5a mark the locations of the virtual satellites.
 284 Figure 5c and 5d show the distribution of differential energy flux as the
 285 function of equatorial azimuthal angle and time at the duskside and

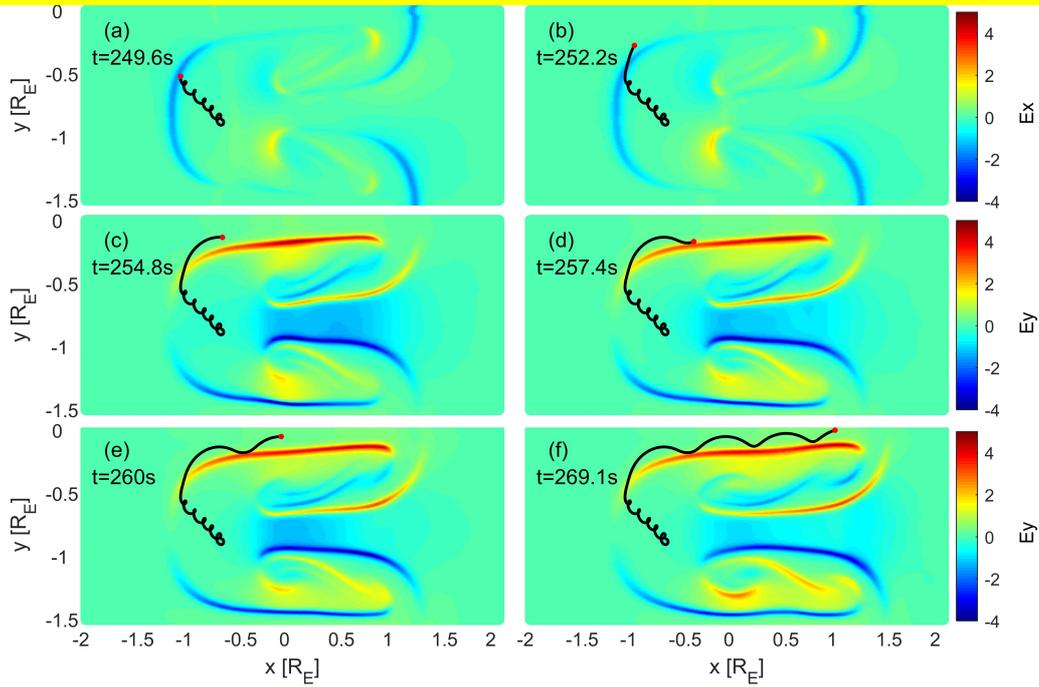
286 dawnside of the DF respectively. Ion trajectories with initial positions
287 along different y locations in Figure 5c and 5d are plotted in Figure 5b
288 where the DF at $t = 221$ s is set as baseline and marked with black solid
289 line. Kinetic energy at final moment is indicated with color.

290 It is obviously seen in Figure 5 that the duskside ions tend to move to
291 dawn at the front (Figure 5d, $90^\circ < \theta < 180^\circ$), while the dawnside ones
292 divert toward tailward (Figure 5c, $0^\circ < \theta < 90^\circ$). This finding is similar
293 to the fluxes of 78-300 keV ions in Birn et al. (2015). At about $t = 221$ s
294 ~ 153 s, the particles with higher initial energy ahead of the front have
295 large radius of gyration and those particles are minor affected by the
296 smaller initial electric field, therefore they are almost simultaneously
297 observed (Figure 5b and 5d). While at $t > 234$ s ions with the initial
298 position at duskside would be able to reach farther into the ambient,
299 which is consistent with the results of Zhou et al. (2014) and Birn et al.
300 (2015). On the other hand, the earlier observed ions are not the most
301 energized ions compared with high-energy counterparts in our model,
302 which is opposite to Zhou's conclusion. It can be easily understood by
303 considering the Hall electric field. The small electric field near the
304 duskside of the front allows particles to drift toward earthward and
305 dawnward for a long time, whereas the high one close to dawnside forces
306 ions to drift tailward quickly during the period that particles obtain most
307 energy (Figure 4).

308 In order to study how the Hall field E_y on the dawnside of DF accelerate
309 ions, we choose one typical ion to track its trajectory, which is initiated at
310 $x = -0.7 R_E$, $y = -0.86 R_E$ behind the DF with an azimuth angle of 14.58°
311 and initial kinetic energy of 1 keV. Its final kinetic energy is 12 keV, as
312 shown in Figure 6. Figure 7 demonstrates the evolution of ion positions
313 and energy and Figure 8 shows the local B_z , E_x , E_y seen by this particle.
314 During the beginning period from 221s to 247s, the ion moves earthward
315 together with the front and meanwhile downward in the frame of the
316 moving front. During this period, the ion gains very little energy. Even
317 though the E_x component of electric field accelerates the ion along its
318 earthward motion, the deceleration by the E_y component keeps the ion
319 energy almost unchanged. When $t = 249.6$ s, the ion arrives at the
320 dawnside of the DF, where the Hall electric field is very strong. After a
321 sharp energization for about 5 seconds, the ion kinetic energy increase to
322 ~ 5 keV (Figure 7b and 7c, the weaker E_x works to reduce the energy by
323 about 3.7 keV and the stronger E_y increases the energy by about 9 keV).
324 As shown in Figure 6 and 7, when $t > 253.8$ s, the ion kinetic energy
325 gradually increases, which can be interpreted based on the fact that the
326 y-displacement δy^+ (corresponding to the energy increase) is larger than
327 δy^- (corresponding to the energy reduction) in the case where E_y
328 component is almost constant. Since the ions arrive at the ambient of
329 dawnward DF, the magnitude of magnetic field is increase, which results

330

in a high δy^+ . Figure 8 shows the time history of the local B_z , E_x , E_y .



331

332

Figure 6. Orbits of an ion with the initial energy 1 keV and final energy

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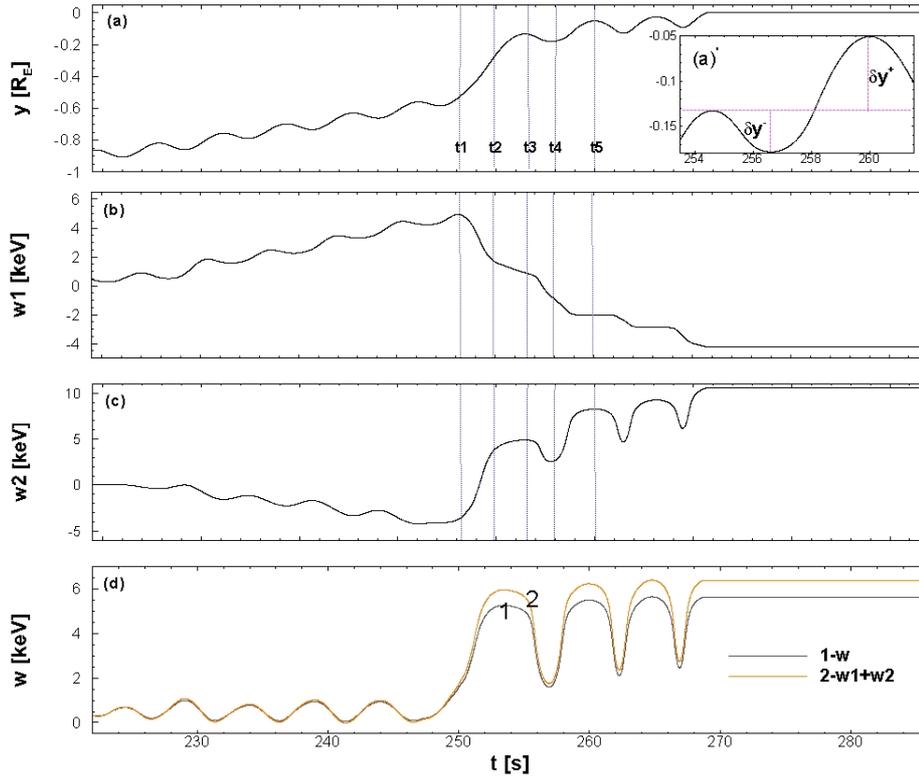
5.54 keV, traced from $x = -0.7 R_E$, $y = -0.86 R_E$ at different moments. The

334

locations of ion are shown as red dots superposed on snapshots of the

335

background Hall electric field E_x (a-b) and E_y (c-f).



336

337 **Figure 7.** Physical quantities of ion as the function of time with blue
 338 dotted lines index specific moment. (a), (a') Y position and its partial
 339 enlarged detail, red dotted line is the reference line. (b, c) Energization
 340 produced by E_x and E_y , respectively. (d) Kinetic energy and numerical
 341 summation of w_1 and w_2 display with orange and black line, respectively.
 342 The label of t_1 to t_5 correspond to 249.6s, 252.2s, 254.8s, 256.9s and
 343 260s respectively.

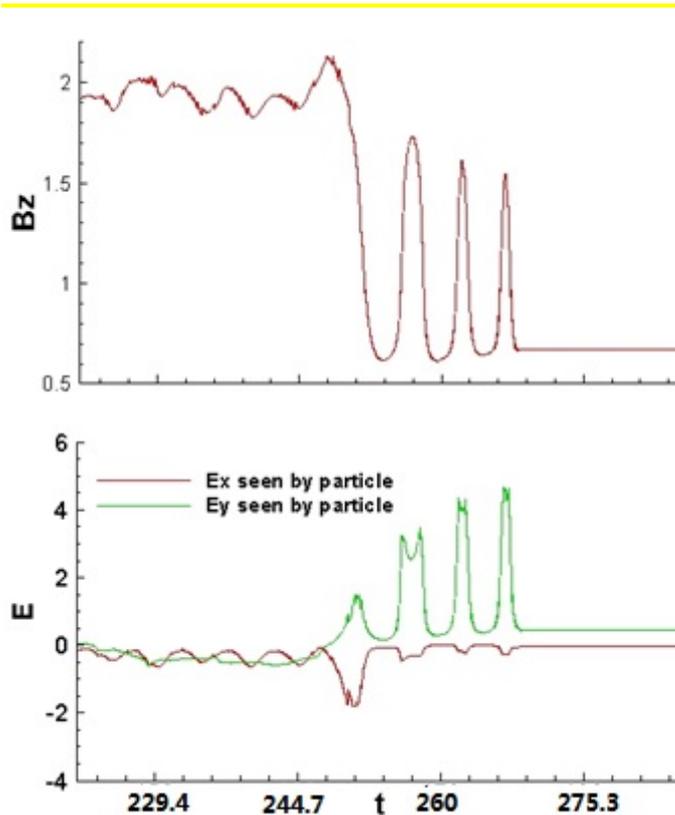


Figure 8. The time history of the local B_z , E_x , E_y

344

345

346 Summary and Discussion

347 In this paper, we used a test particle simulation to investigate ion
 348 acceleration at dipolarization fronts (DFs) produced by interchange
 349 instability in the magnetotail. The Hall MHD model was improved by
 350 applying the realistic initial conditions to obtain the fields which are
 351 better consistent with observation.

352 It should be noticed that our test particle is 2D without the motion in the z
 353 direction along the field line. So we only study the ions with 90-degree
 354 pitch angle. Test particles were settled in both the pre-DF and post-DF
 355 region, most of them exhibited earthward and dawnward drift and then
 356 diverted tailward. It is found that ions with the initial position at duskside

357 would be able to reach farther into the ambient plasma, which has been
358 also proofed by Zhou et al. (2014) and Birn et al. (2015). Statistical
359 analysis shows that the high-energy particles are mainly assembled in the
360 dawnside of $x > -0.5 R_E$ region, which suggests the dawnside region of
361 the DF is the main area for particle acceleration.

362 Numerical simulation results indicate that the ions initially settled behind
363 the front may obtain higher energization. In order to explain how the Hall
364 electric field influence ions, we tracked the trajectory of particular ions in
365 the ion-scale electric field. As expected, the E_y component at the dawn
366 flank of DF plays an important role in the acceleration of ion. Although
367 the E_x component in the pre-DF region constitutes a potential drop of ~ 1
368 keV across the DF as reported by Fu et al., (2012b), the energy
369 enhancement would be offset on their way out toward the magnetotail
370 due to the E_y component. The spatial and temporal properties of E_y
371 component are critical factors for particle acceleration (Greco et al., 2014;
372 Birn et al., 2013, 2015; Artemyev et al., 2015; Ukhorskiy et al., 2017). In
373 contrast to the results from other MHD model, it makes sense in our
374 self-consistent Hall MHD simulation that the accelerating electric field is
375 the E_y component of the Hall electric field on the dawnside of the front
376 instead of the convection electric field E_y behind the front in their model.

377 Our test particle simulation can well reproduce the direct acceleration
378 process generated by the Hall field. Nevertheless, it should be pointed out

379 that the ion acceleration mechanisms such as Fermi acceleration and
380 resonance acceleration can also provide powerful ion energization with
381 tens of keV to hundreds of keV (Fu et al.,2011; Artemyev et al., 2012),
382 which is not discussed in this paper. Still, there is no doubt that our study
383 suggests that the dawn flank dusk-dawn electric field plays an essential
384 role in ions energization.

385

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394

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