Exceedance frequency of appearance of extreme internal waves in the World Ocean

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Abstract. Statistical estimates of internal wave appearance in different regions of the World Ocean are discussed. It is found that the observed exceedance probability of large-amplitude internal waves in most cases can be described by the Poisson curve, which is one of the typical curves of extreme statistics. Detailed analysis is done for the internal waves in the several
10 areas of the World Ocean: tropical part of the Atlantic Ocean, the North-West shelf of Australia, the Mediterranean Sea near the Egyptian Coast and the Yellow Sea.

Keywords: Internal waves, Exceedance frequency, Poisson statistics

1 Introduction

15 Internal waves are observed everywhere in shelf zones of seas. The main source of their generation in the ocean is the semi-diurnal tidal wave, which is initially barotropic and generates the baroclinic tidal wave by the scattering on the continental shelf. As it can be expected, periodic tide generates the regular internal waves each 12.4 hours and this process is well described in literature and modelled numerically, see for instance (Vlasenko et al., 2005). Nevertheless the variability of the magnitude of moon tide and daily temperature and salinity of the sea water lead to random characteristics of the observed
20 internal wave field, see, for example, book by Miropolsky (2001) and review paper by Helfrich and Melville (2006). Popular methods to analyze the random internal wave field are the spectral and correlational methods. As a result, climatic spectra of internal waves have been determined and in particular well-known Garret-Munk climate spectrum (Garret and Munk, 1975), which served as the basis for the regionalization of the World Ocean by the internal wave average parameters. This actually determines the background of the ocean internal waves, over which more intensive processes occur leading to the generation
25 of large (up to extreme values of 500 m) amplitude internal waves (Alford et al., 2015). Data of the large-amplitude internal waves in various areas of the World Ocean are collected in numerous papers (Apel et al., 1985; Salusti et al., 1989; Holloway et al., 1999; Morozov, 2003; Ramp et al., 2004; Sabinin and Serebryany, 2007; Shroyer et al., 2011; Xu and Yin, 2012; Kozlov et al., 2014; Xu et al, 2016). Large-amplitude internal waves have great interest due to an action on offshore platform, submarine and underwater vehicle safety, an effect on phase fluctuations of acoustic signals at large distances

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(Fraser, 1999; Warn-Varnas et al., 2003; Osborn, 2010; Rutenko, 2010; Song et al., 2011; Si et al., 2012;). The special warning systems are developed now in regions of high risk of a pipe and platform damage by the intensive internal waves (Stöber and Moum, 2011).

Internal waves in the ocean can be considered as a continuous random process, and intense large-amplitude waves being are treated as outliers of a given random process are described by the tails of the distribution functions. Consequently, the statistics of these processes is usually different from the Gaussian (normal) distribution. Non-Gaussian character of the observed internal wave field has been mentioned for many areas of the World Ocean (Miropol'sky, 2001; Wang and Gao, 2002). Seasonal and longitudinal statistical analysis of internal wave field has been done recently for the South China Sea (Zheng et al, 2007). It is shown there that the largest number of internal wave packets here is observed at the longitude 116.5ºE and the June 2000 was the most reach on the generation of the internal wave packets in the South China Sea. Special analysis of wave amplitude distribution for the tropical of the western Atlantic Ocean, for the North-West shelf of Australia and the eastern Mediterranean Sea is performed in papers (Ivanov et al., 1993a,b; Pelinovsky et al., 1995), where it is shown that the Poisson law is a good approximation for amplitude distributions of such waves. As it is known Poisson distribution is very popular in the extreme statistics and very often applied in the ocean engineering for description of storm waves (Pelinovsky and Kharif, 2016), tsunamis (Kaistrenko, 2014), rogue waves (Kharif et al., 2009), in geophysics for description of climate anomalies (Dischel, 2017), etc. However, the distribution law for temperature deviations in the tropical part of eastern Atlantic (Mezopoligon-85) is more close to the Gaussan distribution (Morozov et al., 1998).

In the present paper application of methods of extreme statistics to large-amplitude internal waves is briefly reviewed. First, the theoretical approach is revised in Section 2. Then, the results of statistical processing of the internal wave records in various areas of the World Ocean are presented in Section 3. Conclusion is given in Section 4.

2 Extreme statistics methods for high amplitude internal waves

Let $\eta(t,/x,y,z)$ describe the vertical displacement of any isopycnal surface at fixed point which, in the first approximation, can be considered as stationary random process. Usually, a few central moments

$$\mu_r = \int_{-\infty}^{\infty} (\eta - \overline{\eta})^r P(\eta) d\eta \qquad (r = 2, 3, 4) \tag{1}$$

are computed for the statistical analysis. Here $P(\eta)$ is the probability density function and $\overline{\eta}$ is the mean value

$\overline{\eta} = \int_{-\infty}^{\infty} \eta P(\eta) d\eta$ (unperturbed position of isopycnal surface). The second moment $\mu_2 = \sigma^2$ determines the intensity of internal

wave oscillations and σ is root mean square height of internal waves. The third and fourth moments determine skewness

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$Sk = \mu_3/\sigma^3$ and kurtosis $Ku = \mu_4/\sigma^4$, which are used to characterize the deviation of the distribution function from the Gaussian curve (note that $Sk = 0$ and $Ku = 3$ for Gaussian distribution). The sign of the skewness on our opinion can be explained by the specific shape in the internal Stokes wave, which is followed from the weakly nonlinear theory of internal waves. In opposite to nonlinear surface waves, which always have narrow and high crests and flat troughs, internal waves

5   on different depths can have either narrow crests and flat troughs or vice-versa depending on the density stratification and modal structure. For more energetic first mode internal waves, the character of the asymmetry of wave profile with respect to the horizontal axis is determined by the coefficient of the quadratic nonlinear term in the Korteweg-de Vries equation, which is strongly variable in the World Ocean (Grimshaw et al., 2007; Kurkina et al., 2011, 2017a,b). Computations of the skewness and kurtosis as well as distribution function of nonlinear internal waves is an interesting problem which is not

10   studied well up to now.

Here we will use the direct method to evaluate the statistics of large-amplitude internal waves. Fixing some value of vertical displacement, we analyze statistics of the exceedance of wave oscillations above this level (outliers of random process). Let us briefly reproduce the well-known approach for calculating the exceedance frequency for continuous processes (Gumbel, 1958; Stuart, 2001) with application to the internal waves.

15   Internal waves have a vertical structure, and the most energetic lowest-mode waves are more intensive in pycnocline. For definiteness, we chose vertical displacement in the pycnocline and denote it $\eta(t)$ omitting coordinates of the pycnocline in this function. For the outlier beyond the level A in the interval Δt both conditions should be satisfied at once

$$\eta(t) < A \quad \text{and} \quad \eta(t + \Delta t) > A. \tag{2}$$

Due to the smallness of Δt we can represent $\eta(t + \Delta t) \approx \eta(t) + w(t)\Delta t$, where $w(t) = d\eta/dt > 0$ is the vertical velocity of

20   particles lying on the isopycnal surface, and rewrite condition (2) as

$$A - w(t)\Delta t < \eta(t) < A. \tag{3}$$

The required probability of finding $\eta(t)$ in the interval (3) is

$$P(A - w\Delta t < \eta < A) = \int_0^\infty dW \int_{A-w\Delta t}^A f(\eta, W; t) d\eta, \tag{4}$$

where $f(\eta, w; t)$ is the two-dimensional probability density of vertical displacement $\eta(t)$ and the vertical velocity $w(t)$ at the

25   same moment of time and the same coordinates. Since Δt is small, we can use the mean-value theorem to calculate the inner integral in (4) and, hence

$$P(\eta - w\Delta t < \eta < A) = \Delta t \int_0^\infty w f(A, w; t) dw. \tag{5}$$

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Probability density function (in time) can be easily found from (5)

$$p(A;t) = \int_0^\infty w f(A, w; t) dw .$$ (6)

Similarly, the probability of crossing the level A from the top down (into the region of small isopycnal value displacement) is

$$p'(A;t) = -\int_{-\infty}^0 w f(A, w; t) dw ,$$ (7)

since this requires $w < 0$. This equation can be used to calculate probability of large troughs in the vertical displacement which can be as danger as large crests. As it is known, large internal waves in the ocean have usually negative polarity and this correlates with negative sign of the quadratic nonlinearity parameter in the weakly nonlinear theory based on the Korteweg-de Vries equation for deepest parts of the World Ocean (Grimshaw et al, 2007).

Here we calculate the average number of "positive" outliers (large crests) in wave record. To do so we divide the total time interval into small subintervals Δt_j and introduce a random value N_j equal to 1 for an outlier and 0 outside the outlier. Then the total number of outliers is $N(A) = \sum N_j$ and its mean value is the ensemble average, the probability of this is equal to the probability of crossing the level (6). Moving on to the limit for $\Delta t_j \to 0$, we finally have

$$<N(A)> = \int_0^T \int_0^\infty w f(A, w; t) dw dt .$$ (8)

In the case of a stationary random process the formula (8) is simplified

$$<N(A)> = T \int_0^\infty w f(A, w) dw .$$ (9)

Thus, the average number of outliers is proportional to the time interval and falls with the increase in the outlier level. The same approach can be used to compute average number of "negative" outliers (deepest troughs) in the internal wave field.

Only the average number of outliers was discussed above without considering their probabilistic distribution. A much more difficult problem is to calculate the latter. It should be noted that if outliers are rather rare (which is typical for very large-amplitude internal waves, $A \to \infty$), then their distribution can be regarded as Poisson one. Then the probability of at least one outlier occurred in the time interval t is

$$P = 1 - \exp(-\nu t) ,$$ (10)

where the mean frequency of outliers $\nu = <N>/T$, is found from (9) as

$$\nu(A) = \int_0^\infty w f(A, w) dw.$$ (11)

The average frequency of outliers in the first approximation can be used as an estimate of the internal wave exceedance (cumulative) frequency with the amplitudes greater than the given value of A.

Detail calculations of the outlier characteristics in the internal wave field require the knowledge of two-point (vertical
5   displacement and vertical velocity) distribution functions of isopycnal variation which are usually not measured. If the internal wave random field is assumed to be normal, the density of distribution function is described by a Gaussian curve

$$f(\eta) = \frac{1}{\sqrt{2\pi}\delta} e^{-\frac{(\eta-\bar{\eta})^2}{2\delta^2}},$$ (12)

where δ is the standard deviation (mean amplitude of the internal waves). The distribution function of the vertical displacement and the vertical velocity for the normal process do not correlate, so their two-dimensional probability density
10   splits into a product of two Gaussian curves (12) with naturally different mean-square deviations. Then the average frequency of outliers is

$$\nu(A) = \frac{\delta_w}{2\pi\delta_\eta} \exp(-\frac{A^2}{2\delta_\eta^2}),$$ (13)

where δ_w is the mean-square (standard deviation) value of the vertical velocity in the internal wave and δ_η is the mean-square value of the vertical isopycnic displacement. Thus, the internal wave exceedance frequency depends on the wave amplitude
15   according to the Gaussian curve very quickly fallen with increase in amplitude. We will demonstrate Gaussian character of cumulative frequency for tropical zone of eastern Atlantic Ocean.

It should be remembered that usually internal wave field statistical distributions in the areas of the World Ocean differ from normal distribution as we already pointed in Introduction, see book Miropolsky (2001), so the result will be different from (13) depending on the particular form of the tails of the distribution function in large amplitude range. As shown in
20   (Leadbetter et al., 1983), the intermediate asymptotic exceedance frequency for large outliers has the form of a Poisson curve

$$\nu = \nu_0 \exp\left(-\frac{A}{A_0}\right),$$ (14)

where ν_0 and A_0 are the parameters depending on the specific type of "tails" of the distribution function in the large amplitude range. This expression can be used to compute exceedance (cumulative) frequency of large outliers (positive or negative) in the internal wave field. Obviously, the predicted amplitude values are also random, and here one can speak only

about its evaluation. Its mean value can be calculated only if wave record is long enough, that is usually to measure in the ocean. So, to estimate the predicted amplitude A it is necessary to set the value of the exceedance frequency

$$\nu = 1/T , \tag{15}$$

where T is the prediction time (or the recording time). Expression (14) is used to calculate the design amplitude A of internal wave on prognostic time interval T

$$A_T = A_0 \ln(\nu_0 T) . \tag{16}$$

Characteristic values of A_0 and ν_0 are different for various areas of the World Ocean and will be discussed in next section.

3 Statistics of internal wave field

3.1. Probability density function in the Yellow Sea

The shallow water (Qingdao offshore area) experimental data from the Yellow Sea are processed in (Wang and Gao, 2002). The thermistor chain was used for measurements. The temporal lengthscale of records is 49 h 49 min with sampling interval 6.4 s. The water depth is 33 m. Rather narrow undisturbed pycnocline lies from 10 m to 16 m with maximum of the Brunt-Vaisala frequency $N_{max} = 0.067$ s^{-1}. Vertical displacements of highpass-filtered 25º - 17.5º (16 levels) isotherms are described and their histograms are plotted. It is found that the standard deviation is slow growing from 0.46 m to 0.56 m from surface to bottom. Skewness is negative for each isotherm and has the maximum 0.5 in absolute value at the depth 15 m with 0.36 at the surface and 0.06 close to bottom. Kurtosis changes from 3.24 close to bottom to 5.05 at the 14 m of depth and 4.12 near the surface. It is shown that the distribution of large internal wave amplitudes is not the Gaussian. The maximum wave height here is not more than 5 m, nevertheless the process differs from the Gaussian law.

We may explain the sign of the computed skewness applying the weakly nonlinear theory of internal waves based on the Korteweg-de Vries equation (Pelinovsky and Shurgalina, 2017). For given area in the Yellow Sea the sign of quadratic nonlinear term in this equation is negative, because the water stratification (see in Wang and Gao, 2002) is practically two-layer with pycnocline situated above the half-depth (Djorjevich and Redekopp, 1978; Kakutani and Yamasaki, 1978). Nonlinear waves as solutions of the extended Korteweg-de Vries equation with negative quadratic nonlinearity have deepest troughs, for instance the internal wave soliton has negative polarity (Grimshaw et al., 2007). This leads to the negative values of the skewness.

3.2 Exceedance frequency of internal waves in the tropical zone of western Atlantic

The exceedance frequency of internal wave is estimated using data obtained during the 39th cruise of the RV "Akademik Vernadsky" in the north-western Atlantic Tropical Zone near the mouth of the Amazon River, 2-15° N, 38-52° W (Ivanov et al., 1993b). Internal waves of average 2.5-10 m amplitudes are observed in this region. To obtain long-term internal wave

recordings the ship echo sounder was used in this study. It allows for studying sound-scattering layer fluctuations at depths up to 100 m. These fluctuations are known to be due to various causes, but in the range up to 3 hour wave periods they are mainly related to internal waves. The wave period also varies over a wide range from 3 min to 30 min on the sonar recordings. Since the measurements were made on the ship moving at a velocity of about $V = 15$ knots and as the maximum

5 of internal wave speed is $c = 3$ knots in order of magnitude, the internal wave pattern can be considered frozen in the first approximation. In this case, the "true" wave period increases in comparison to the observed one with ratio $V/c = 5$. The amplitude of sound-scattering layer fluctuations was everywhere identified with the internal wave amplitude in the pycnocline. The total recording duration was about 218 hours. Wave height (defined as the fluctuation swing between adjacent extremes) and fluctuation duration on the recording were adopted as the main characteristics. Primary echogram

10 processing results by day are presented in the paper (Ivanov et al., 1993b). These data are used to estimate the exceedance (cumulative) frequency. They well agree with the regression line

$$\nu = 9.2\exp(-0.3H) , \tag{17}$$

where H is wave height measured in meters, and ν is in hr^{-1}, except for the heights greater than 25 m, where the total number of wave observations does not exceed six. Formula (17) is used to estimate the predicted wave height versus a forecast time

15 function

$$H = 18 + 3.3\ln T . \tag{18}$$

Predicted values of internal wave heights versus time are summarized in Table 1.

During the time spent at the area, the "true" internal wave recording time (considering the ship movement) was about 45 days. According to the prediction for this period, a wave with a height of more than 31 m should be observed once, with a

20 height of more than 23 m - twice, and more than 27 m – three times. In fact, the level of 31 m is exceeded three times, and the level of 27-28 m - six times, which is quite good within the framework of predictive models.

3.3 Internal wave temperature at Mesopolygon-85 in the Atlantic Ocean

The wave process in the open ocean can be expected closer to normal, which makes it possible to use the theory of normal random process and estimate the limits of its applicability in internal wave practice. In the given paper is undertaken the

25 exceedance frequency analysis for internal wave records obtained from buoys at the area in the eastern Atlantic Ocean in 1985 (Mesopolygon-85; the detailed description of the experiment is given in Kort, 1988). It should be mentioned that there 49 buoy records are processed, and it is unique possibility to estimate the horizontal variability of the internal wave amplitude distribution function. The area was located at the juncture of the Canary Deep and the Green Cape Deep (19-21°N and 36-38°E). The buoy stations operated approximately two months from April to May. The meters were placed on four

30 horizons, but the most representative measurements were made at the horizon of 200 m. The total size of the area was approximately 80 to 80 miles.

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Temperature variation recordings in Celsius at various points of the area were used to calculate the average frequency of outliers (temperature variation exceeding of the set value ΔT). 49 cases (out of 54) are very well described by a Gaussian distribution

$$\nu = (0.79 \pm 0.17) \exp\left(-(10.61 \pm 4.5)(\Delta T)^2\right), \tag{19}$$

where the parameters vary from station to station. Here ν again has the dimension of hour^{-1} and ΔT is degree centigrade. It should be noted that the deviation in ν_0 consists of 21% and 42% in the exponent, on the area about 48000 km^2 in the tropical part of eastern Atlantic. More details of the experiment data are given in (Morozov et al., 1998). Unfortunately, we could not able to convert equation (19) in similar equation for vertical displacement because the vertical structure of internal waves was not measured.

3.4 Internal wave heights in the Mediterranean Sea

Let us discuss internal wave appearance in tideless seas where one can expect the statistical characteristics universalization over a short period of time without being tied to the phases of the moon. The reasons of internal wave generation here may be storms and upwelling as well as the effect of river flow in mouth. Internal wave observations for one of the Mediterranean regions (Levant Sea) obtained during the 27th cruise of the RV "Professor Kolesnikov" (July-August 1991) are used in the paper. These old data briefly presented in Ivanov et al. (1993a) are now revised. During the period from 27 to 29 July, 1991 a special experiment to record internal waves was performed at the area near the Egyptian shelf. The measurements were carried out in a thermocline. The basin depth at the area is varied from 200 to 1100 m. The vertical profile of the Brunt-Vaisala frequency contains the pycnocline presence at a depth of about 25 m at a frequency of 17 cycle/hour. Below the pycnocline the mean value of the Brunt-Vaisala frequency is 4 cycle/hour. The wave regime in the eastern Mediterranean is relatively poor, since the tide is very small. The wave height distribution function is calculated from these data. The vessel speed was approximately $V = 5$ knots, which significantly exceeds the internal wave propagation speed in this region ($c = 2$ knots). Therefore, in the first approximation, the internal wave field can be considered as frozen. This means that the "true" time recording can be increased by $V/c = 2.5$ times. The applicability of Poisson law for the exceedance (cumulative) frequency, as can be seen from Fig. 1, is well applied for the observed data: they are approximated by the formula

$$\nu = 4\exp(-1.79A), \tag{20}$$

where A is a wave amplitude measured in meters, and ν is in hr^{-1}. The obtained distribution (20) can be used for the prediction of large amplitude waves. The predicted values of internal wave amplitudes calculated using formula (20) that can occur in the Mediterranean Sea near the Egyptian shelf over different time periods, are summarized in Table 2.

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It should be noted that the observed internal waves at this region have much smaller amplitudes than in the ocean, where 100-meter waves are recorded (Ramp et al., 2004). This fact is well known for the tideless seas and is reflected in the large value of the return period for internal wave of 5 m amplitude in this part of the Mediterranean Sea.

3.5 Exceedance frequency in the current velocity from the data of buoy stations (the north-western shelf of Australia)

5 Relatively long internal wave recordings were obtained at buoy stations on the northeastern shelf of Australia (Pelinovsky et al., 1995). The water depth is approximately 123 m. Flow velocities in the internal wave range, recorded at a horizon of 3 m above the ocean bottom, will be analyzed in the given paper. Measurements were taken every 2 minutes for 10 days. Only the flow component, which contains the strongest wave fluctuations, was analyzed in the transverse to the isobaths direction (45^0 north - east). The time series is passed through a high-frequency filter to remove the tidal component. Each recording is

10 divided into equal intervals of 4000 minutes. Primary time series processing results are given by Pelinovsky et al. (1995). The calculated values of exceedance frequency for different amplitudes are approximated by the expression

$$\nu = 1.33 \exp(-0.071 U) , \tag{21}$$

where ν has the dimension of hr^{-1} and amplitude of horizontal velocity variation U is in cm/sec.

The regression formulae obtained above can be used for calculation of exceedance probability of large-amplitude internal

15 waves as function of wave flow amplitude and time duration. Result of calculation for the North West Shelf of Australia is represented on Fig. 2.

4 Conclusions

Here we consider statistical characteristics of the internal wave field in several areas of World Ocean: the tropical part of the western Atlantic Ocean near the Amazonian mouth, the part of the eastern Atlantic, the west part of Mediterranean Sea, the

20 North West shelf of Australia and the Yellow Sea shelf (Fig. 3).

It is difficult directly to compare the results of exceedance frequency calculations for various regions of the World Ocean. The main difficulty of the comparison is that different characteristics were measured. In particular, in the tropical zone of the Atlantic, the vertical displacement of the sound-scattering layers was measured, in the Mediterranean Sea it was the amplitude of displacement of the thermocline, while on the Australian shelf the records of flow velocity fluctuations were

25 analyzed, and at the Mesopolygon-85 it was the temperature fluctuations on a given level. The internal mode structures were never analyzed for these measurements, and we cannot confirm that the observations are done in the mode maximum. So, we may predict the internal wave amplitude only for the level of measurements. Also for three analyzed areas the Poisson law is valid for internal wave amplitude distribution, but for Mezopolygon - 85 we get the Gauss distribution what is more appropriate for very small amplitudes. Nevertheless, the internal waves in the eastern Mediterranean Sea have amplitudes not

30 more than 2 m but the amplitude distribution function closes to the Poisson law. It seems, all mentioned above is the subject

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for following investigations. Meanwhile, the value of v_0 has universal character and should be not depended from the measured characteristics of internal waves. For the Australian shelf $v_0 = 1.3$ hr^{-1}, for the tropical zone of the Atlantic $v_0 = 9.2$ hr^{-1}, for Mesopolygon-85 $v_0 = 0.8$ hr^{-1} and for the Mediterranean (Levant Sea) $v_0 = 4$ hr^{-1}. These values turned out to be very heterogeneous. It should be the feature of the ocean region. We may connect this value with capacity the region to

5 generating of internal waves. So, the area near the mouth of the Amazon River is famous of large amplitude internal waves, which are generated by fresh water intrusion into ocean salted one and plus the tide events. Low amplitude but often-generated internal waves are performed near the Nile River mouth. Internal waves generated mainly by tide propagate cross the Australian shelf. We may propose due to $v_0 = 0.8$ hr^{-1}, that internal waves in the Mezoppoligon-85 are not too often generated.

10 Now the numerical methods to predict internal wave field characteristics in different areas of the World Ocean is actively applied. They demonstrate that such characteristics are very sensitive to the density stratification of the ocean. Water stratification is varied in night and day during months and the moon tidal wave is varied also. The influence of variation of water stratification on the internal wave dynamics can be illustrated by the seasoning maps of kinematic parameters of internal waves (Kurkina et al., 2001, 2017a,b). Computing many scenario of the internal wave developing for various

15 hydrological conditions, some statistical estimates can be done. We do this work within the Euler equations for stratified water for the Barents Sea (Kurkina and Talipova, 2011; Talipova et al., 2014), the Sea of Okhotsk (Kurkina et al., 2017b) etc.

Data availability. The data used by this study are extracted from the GDEM database.

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Competing interests. The authors declare that they have no conflict of interest.

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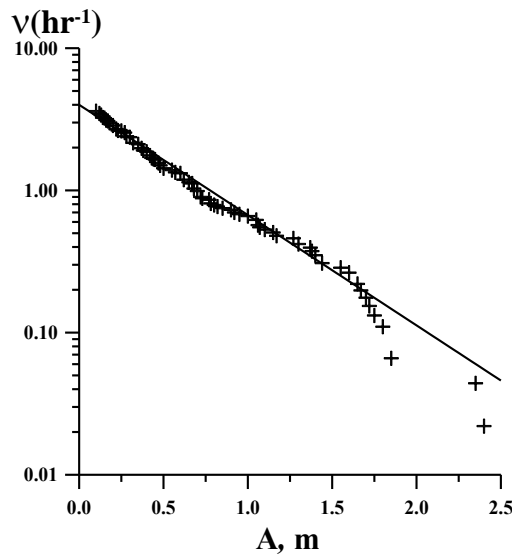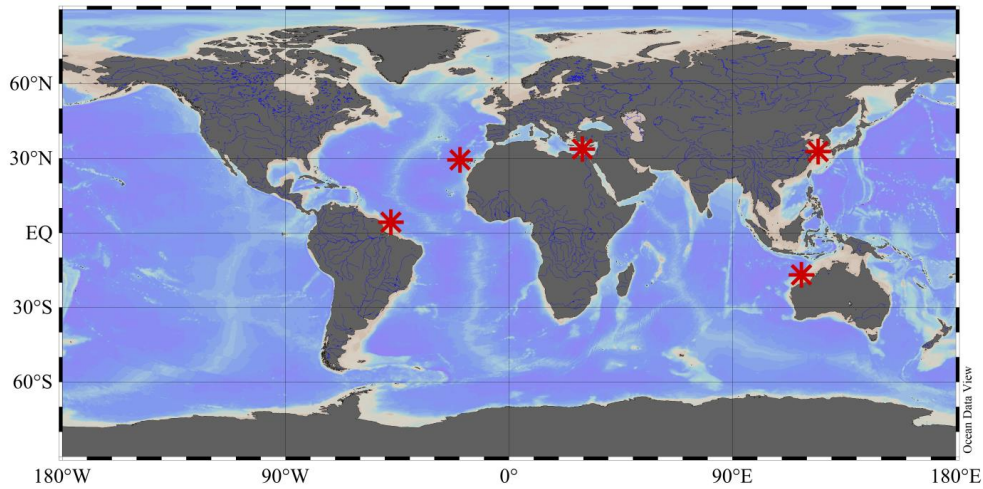
15√ **Figure 1: The exceedance frequency of internal wave amplitudes in the eastern part of the Mediterranean Sea.**

Not a good phrase; should be rephrased.

of a certain amplitudes?
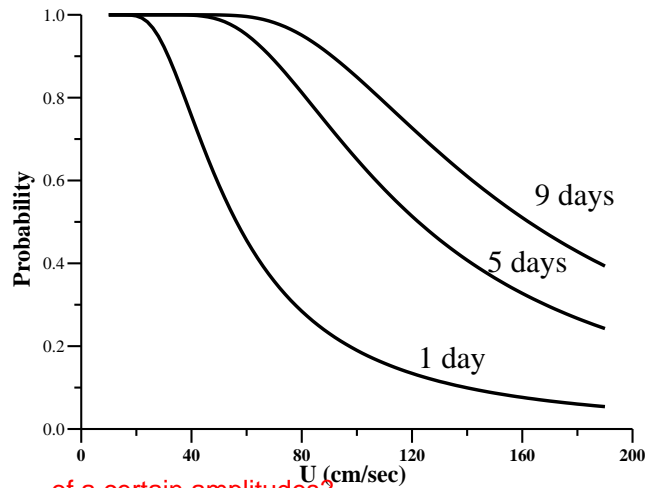
√ **Figure 2: Probability of occurrence of internal waves at the North West Australian shelf.**

√ **Figure 3: Areas, where we consider statistical characteristics of internal waves.**

Not good grammatically; should be rephrased.

5

√ **Table 1: Wave height prediction for the Atlantic tropical zone.**

time	1 day	10 days	1 month	3 months	6 month	1 year
H(m)	18	26	29	33	35	38

This sounds much better

Table 2: Predicted internal wave heights in the Mediterranean Sea.

Time period	1 day	1 week	1 month	3 months
A(m)	2.6	3.6	4.5	5.1

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