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Interactive comment

Interactive comment on "Instabilities within Rotating mode-2 Internal Waves" *by* David Deepwell et al.

David Deepwell et al.

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We thank the Reviewers for their comments. We have attempted to respond to all comments. In the case of Reviewer 2, some very insightful comments require computational resources/computation time beyond the one-month revision period and we have taken these as suggestion for future work. Reviewer comments are in bold font, responses are in normal font.

1 Major comments

There is no comparison between the numerical results and field observa-





tions, or attempts to suggests how and where the processes discussed in this manuscripts could be observed in nature. I think is relevant to motivate the readers with some realistic applications of the paper's outcomes. For instance, the authors might compare their numerical experiments in the absence of rotation with the laboratory experiments performed by Carr et al. (2015), since they have collaborated on recent work (Deepwell et al. 2017).

The reviewer is correct that we were not very clear on this point. We have added a paragraph to the introduction that outlines where we see our study in terms of field, experimental and numerical approaches:

"Results on non-rotating mode-2 ISWs, especially with regards to their mass transport capabilities (Deepwell and Stastna (2016), Salloum et al (2012), Brandt and Shipley (2014), Terez and Knio (1998)), are readily available and there is considerable contact between the experimental and numerical modeling literature. This is exemplified by recent progress on quantifying the effects of displacing the pycnocline center from the mid-depth (Carr et al. (2015), Olsthoorn et al. (2013)). In contrast, mode-2 ISWs in a rotating reference frame have been document experimentally by Maxworthy (1983), but no high resolution numerical simulations that provide concrete examples of phenomena future experimental efforts could aim to document exist. We provide such simulations below, with a focus on the overturning induced by the rotation modified ISW (or Kelvin wave, depending on one's choice of terminology) at the focusing boundary.

Our primary qualitative results that could be confirmed in the laboratory concern the fundamentally three dimensional nature of the shear instability at the edges of the mode-2 wave's core, and the the details of the spatial structure of the span-wise kinetic energy flux. The former could be visualized by a PIV system with a light sheet oriented in the span-wise direction, while the latter could be characterized by the more usual along-tank PIV set up. Moreover, the quantitative results of the Kelvin wave-Poincaré wave resonance and the formation of secondary Kelvin waves in our simulation should provide an easier comparison than field oriented simulations such as those of Sanchez-

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Garrido and Vlasenko (2009). In terms of the numerical modeling literature, we are interested in exploring how the Schmidt number (or Prandtl number in thermally stratified systems) affects the localized shear instabilities generated near the Kelvin wave crest. This is important since Schmidt numbers representative of salt stratification ($Sc \approx 700$) are presently intractable for numerical simulations on all but the smallest scales, but realistic results may be obtained by choosing a Schmidt number larger than that for a heat stratified system ($Sc \approx 7$) but much smaller than that of salt. It also implies that while field scale simulations like those of Sanchez-Garrido and Vlasenko (2009) may have a similar Rossby number to an experimental study, they cannot have the same viscosity and diffusivity, implying that experimentalists need to carefully assess what aspects of such simulations they may successfully observe in the laboratory."

The authors do not discuss the implications of the free-slip boundary conditions adopted in their numerical experiments; this is the case of Maxworthy (1983). For instance, how does the growth of shear instabilities near no-slip walls would change the results?

Free slip boundaries are the commonly adopted first choice in numerical studies. No slip boundaries, and the clustered Chebyshev grids necessary to resolve them, would greatly increase the expense of the simulations. We believe that a no-slip boundary condition will have minimal impact on the Kelvin wave and on the shear instabilities near the wall, because the length scales of these instabilities are significantly larger than the boundary layer thickness. We have added a comment to the text, but carrying out no slip simulations is certainly an important future direction.

The authors explore only one background stratification aspect ratio h1=h2, h, with different wave amplitudes. I wonder why they did not explore other background stratification. I would expect that in nature an upper layer thinner than a deep layer, or vice-versa. It might be interesting to explore how the asymmetry in layer thicknesses would change the growth and structure of K-H like instabilities.

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It is correct that nature typically has stratifications which consist of a thick deep layer and a thinner upper layer, but this break in the symmetry of layer depth leads to far more complicated behaviour (see Olsthoorn et al. (2013) and Carr et al. (2015)) coupling mode-2 and mode-1 wave generation. We decided, as many authors have in the literature on mode-2 ISWs, to begin with the simple first case of equal layer depths. We have included a comment on this in the article, and mention that unequal layer depths is a possible avenue for further investigation.

The title of the article suggests that the focus of the manuscript is the transition to turbulence driven by second vertical mode internal waves in a rotating environment, but the paper is more general than this title. The paper examines the macro- and micro-scale processes driven by the degeneration of second vertical mode solitary waves in a rotating and bounded stratified flow. I would suggest the authors think of a different title.

The title has been changed to "Multi-scale phenomena of rotation modified mode-2 internal waves".

2 Specific Comments

1. In the introduction, one would also cite the work by Moum et al. (2003) or more recent observations by Zhang and Alford (2015), and for motivations, for instance, Cuypers et al. (2010).

We have added references to these articles in the introduction.

2. On page 2, between 20 and 25, I would mention the results obtained by Melville et al. (1989).

We have done so. This was a necessary inclusion in this article.

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3. How did you estimate that a single turbulent patch has a vertical extent of about 40 cm, where are the 25 points coming from? Vertical grid points? Are the authors making a reference to Ulloa et al. (2015)'s paper?

Yes, we are referencing Ulloa et al. (2015) in measuring their turbulent patch. We estimated that the vertical extent of the patch was 0.04 m. With a vertical grid spacing of 1.55 mm this would give a total of 25 grid points in the region. We have decided to remove the discussion on the resolution of the turbulent patch since it doesn't add anything to the current article and makes sense to revisit in future work.

4. Subsections 1.1 and 1.2: Why equations are not enumerated? Please, enumerate them.

We have done so.

5. Page 3, paragraph 20: It seems obvious, but the authors could write that the domain is Lx x Ly x Lz = 6.4 m x 0.4 m x 0.3 m, or something like that.

We have done so.

6. Table 1: Missing units of z0 and h; both variable should be defined and schematised in Figure 1.

The definition and units of the variables have been included. The schematic has been unchanged since the addition would cause too much clutter to the plot.

7. Page 4, paragraph 10: ' ... we attempt to carry out a Direct Numerical Simulation (DNS) ... '. Concerning this sentence, what is the Kolmogorov scale of the numerical experiments? What is the Ozmidov scale? If authors are solving the Kolmogorov scale, please take the word 'attempt' out of the sentence, otherwise explain further.

The text has been modified to include the following paragraph addressing this issue:

"We have run a series of direct numerical simulations (DNS) in a setup similar to that of

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Maxworthy (1983), who employed a gravity intrusion from a lock release in a rotating, rectangular tank to generate mode-2 waves. Since the flow develops from a state of rest the precise definition of the term "Direct Numerical Simulation" from the turbulence literature, namely that grid spacing must be smaller than the Kolmogorov microscale, cannot be directly translated to the present situation. We define DNS in the sense commonly adopted in the stratified flow modeling literature, with Arthur and Fringer (2016) providing a concrete example. These authors state that DNS is a three-dimensional simulation which has a grid spacing which is "within approximately one order of magnitude of the Kolmogorov length scale". The Kolmogorov scale for transitional flows is defined in an ad hoc manner, usually via the explicit calculation of the viscous dissipation rate. The grid scale of our simulations is comparable to this usage since it is within an order of magnitude of the Kolmogorov scale defined from the maximum local dissigation rate. Moreover, our numerical method is spectral in all directions, and hence formally higher order than that used in Arthur and Fringer (2016). The spectral filter used to control aliasing applies only to the largest 30% of wave numbers and leaves the majority untouched, and no subgrid scale model as in Large Eddy Simulation (LES) is used. Based on these considerations, and in the absence of a better term, DNS will be used throughout."

8. Page 4, paragraph 10: Did Sanchez-Garrido and Vlasenko (2009) define in the same way the Rossby number? It seems that their Rossby number is almost twice smaller than the smaller Ro considered in this work.

Sanchez-Garrido and Vlasenko (2009) do not define a Rossby number or Rossby radius of deformation. An estimate based on the latitude, wave speed, and channel width does give a smaller Rossby number than the one we present, however, we are not attempting to make a direct comparison to a specific geographic region. Comparison to experiments such as those carried out by Grimshaw et al. (2013) gives similar Rossby numbers.

9. Table 2 is referenced in page 4; so far there is no clear explanation about

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how cw and aw were estimated. The authors explained these parameters were parametrised on the wall, y = 0 m, and the amplitude was defined before the formation of instabilities. Was the emergence of interfacial instabilities defined by visual inspection of the isopycnals? How was then estimated the phase speed, cw? This matter requires a bit of further explanation.

The initial discussion of these parameters was fairly terse, and we have now expanded their discussion and included a reference to a schematic in a previous paper. The main points (as they are now in the paper) are: a_w is measured as the average maximum displacement from the upstream value of the isopycnal $\rho(z_0 \pm h)$. c_w is the speed of the location of this maximum displacement. Yes, the instabilities were visually inspected from the density field.

10. Subsection 1.2: I would suggest rewriting the description of the governing equations. I would suggest something like 'our numerical model solve the Boussinesq equations of motion on an f-plane ...'. 'stratified Navier-Stokes equations' sounds a bit unusual.

We have done so.

11. Page 5, paragraph 15: Is SPINS the acronym given to the numerical solver or is a general pseudo-spectral method?

SPINS is the acronym for the numerical solver. We have fixed the typo in calling it a method as it is actually a particular solver.

12. Page 6, paragraph 5: What type of computational resources were used to perform the numerical experiments (machine, number of cores, computational time)?

A typical run completed in approximately 3 days on 64 processors on Compute Canada resources (SHARCNET). The higher resolution cases required significantly more resources, approximately two weeks using a combination of 64 and 128 processors

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(either number was used on a restart). Data analysis requiring a day or two added additional computation time. The supercomputer cluster is mentioned in the Acknowl-edgments.

13. Page 6, paragraph 5: How many vertical grid points does the numerical experiment use to solve the peaks of the square of the buoyancy frequency, N2, on the initial solitary wave? I would include this information to show that the density transitions are well solved. For instance, the vertical length-scale of the pycnocline thickness in the wavefront, h, is solved by around 17 and 36 grid points each vertical grid resolution, respectively.

Yes, we should have discussed the resolution of the stratification. We have added the following sentences to clarify this: "For the resolution listed in table 3, the strongly stratified region of the background stratification contains approximately, $2h/\Delta z \approx 33$ points. The entire stratification has approximately 140 points, and is thus well resolved."

14. Section 2. The authors start refereeing the work of Maxworthy (1983). Similarly to ?, I would compute the relationship between wave amplitude, Aw, phase celerity, cw, and the dependence with the controlling parameter, the Rossby number (and later with the Schmidt number). These results can be discussed along with Figure 3.

Based on the information in table 2 we have added the following discussion: "The wave speed, measured as the speed of the location of the maximum displacement, is independent of the rotation rate and has a value larger than the linear long wave speed due to the large amplitude nature of these waves. The amplitude is only weakly dependent on the rotation rate or Rossby number."

15. Equation 1. The definition of ξ does not allow a quantitative comparison between the numerical experiments. I would recommend using a scaling that allows comparison.

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We are concerned with comparing the geometric structure of the waves between different simulations, thus the maximum-scaled KE is the best choice. We have included the maximum unscaled values in the caption for comparison.

16. Page 6, paragraph 25. Where does the shear reach its maximum? at $\widetilde{y} = 0$?

Yes, the shear reaches its maximum at y=0. This has been made clearer in the article.

17. Figure 3: I would include the Rossby number for each experiment to show the background rotation environment along with the resulting wave dynamics.

The Rossby numbers have been added to the figure caption.

18. Section 2 (Page 7, paragraph 5) How did the authors compute the energy partition between Kelvin and Poincaré waves? The authors may compute spatial spectra as a function of time to quantify the energy contained in the spanwise and streamwise axes.

We agree that the sentence, as written, was confusing. We have replaced it with: "Overall, the spatial distribution of kinetic energy is dominated by the Kelvin wave front and two secondary features near the focusing wall." This re-write is based on the observations made in figure 3. We note that because of the curvature of the Kelvin wave front, a spanwise spectrum will not provide an accurate representation of the energy.

19. Page 8, paragraph 10. How is this Kelvin-Poincaré wave resonance compared with the one studied by Melville et al. (1989), and the observed by Renouard et al. (1993). It seems that the train of solitary waves obtained by Ulloa et al. (2015) also converges to azimuthal secondary Kelvin waves.

In Renouard et al. (1993) the Poincare waves were resonantly generated as the ISW turned at a right-angled corner. We have added the following sentences:

"Renouard et al. (1986), however, matches our results of Poincare waves being resonantly generated along the side wall. Melville et al. (1989) also clearly shows that the

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curvature of the wave front is due to the combination of a Poincare and Kelvin wave. Our results are in agreement with both of these results, but now applying to mode-2 ISWs."

20. Page 9, paragraph 10: Is there any experimental evidence that a secondary Kelvin wave becomes more energetic and overtakes the leading Kelvin wave? What is the relevance of this phenomenon? This might be possible to show, for instance, by using a circular basin such as those used by Wake et al. (2005) and Ulloa et al. (2014). However, this would be a different problem. I think the authors should emphasize the relevance and implications of having secondary Kelvin waves in the system.

We are unaware of any experimental evidence showing secondary waves surpassing the leading Kelvin wave. For rectangular geometry, this is likely to remain the case as it takes considerable time for the transfer of energy to occur. Circular basins are a different problem with additional effects due to the curvature of the side walls. We have added this point into the article.

21. Page 12, paragraph 5: Is there any relationship between the internal Rossby radius of deformation and the length-scale where shear instabilities were found in the spanwise direction? The authors state that this region is confined to a quarter of the transversal length-scale, Lz. However, did they observe any change in terms of the Rossby radii?

Yes, the Rossby number does play a role in determining the length-scale of the instabilities. We've added a discussion on this result.

22. Page 12, paragraph 10: Why did the oscillatory K-H like billows disappear once the vertical resolution was increased? Any further thought? What was the most critical wavenumber in both cases, when nz = 256, and nz = 512. The authors could perform a stability analysis to understand the nature of the instabilities and the growth rate.

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For clarity, we note that the billows do not "disappear", but that small details of their evolution change. We have begun a more systematic study of even higher resolution simulations of this, and a number of other, studies in order to unravel some of the subtle ways in which hydrodynamic instability and numerical viscosity interact. Since such simulations take a long time we have cut down some of the discussion in the present manuscript. The suggestions given by the reviewer here will be taken into account in the future study. The background state is quite complex (i.e. it is not a parallel shear flow, see figure demonstrating non-negligible vertical velocity (in m/s) at focusing wall in case 10_1 below), and hence a detailed stability analysis, while a good idea, is really a separate study. (figure 1 here).

23. Page 12, paragraph 10: Regarding the von-Karman like vortices. I would think that this kind of instabilities is possible to have a physical sense. There is a localised solitary wave propagating through a mid-layer in an initially quiescent stratified fluid. If we move on the leading solitary wave on the near-wall zone, the solitary wave feels there is a streamwise flow in the opposite direction. This scenario leads to a shear flow that could be similar than the one observed in the generation of von-Karman street vortices. Could you please give a look at the vertical velocity profile along the core of the leading wave?

We have added the following: "These K-H billows can also be considered analogous to a von Karman vortex street. In a reference frame moving with the wave, the background flow is directed around the wave, much like it is around a cylinder in von Karman's classical experiment. The analogy is somewhat limited since the Kelvin wave core is not a solid, and due to the rotation the core bends backward away from the wall (and hence isn't a cylinder). Moreover, the instability is a shear instability, as opposed to a boundary layer separation." We have looked at the velocity, but have not included this figure in the manuscript since the density figures makes the vortices quite apparent. (Figure 2 here)

24. Page 13, paragraph 5: Is there any clue of baroclinic-like instabilities? Have

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the authors observed the vorticity field in the x -y plane?

We have looked at the vorticity field and find no evidence of baroclinic-like instabilities. We have also done a back-of-the-envelope calculation for the fastest growing baroclinic mode and find that the scale of the waves in the manuscript is smaller than typical baroclinic disturbances by more than an order of magnitude.

25. Page 14, paragraph 10: Did the authors compute the local gradient Richardson numbers on the leading solitary wave zone?

Yes, we did. We have added the following sentence: "Though the Richardson number is not applicable in the upper and lower layers where there is no vertical density variation, within the wave core the Richardson number drops below 1/4 around the edge of the mode-2 bulge while the K-H billows form."

26. Page 16, paragraph 10: Do the authors think that the channel width plays any role in the train of solitary-type waves structure and the shear instabilities growth? If so, please comment.

For the instability of the leading Kelvin wave, the highest rotation rate case shows that the instability occurs within 10 cm of the focusing wall (approximately a quarter of the channel width used). Thus in fact a narrower tank would give similar results. Since the trailing Poincare and Kelvin waves are a result of the leading wave we expect them to have no impact on the shear instabilities of the leading wave. The width of the channel will, however, adjust the reflection of the Poincare waves and thus the resonance of the secondary Kelvin wave. This last point has been included.

27. Page 17, paragraph 10: What grid resolution would be required to solve the Batchelor scale in a numerical experiment with Sc=700? How far are we to solve this problem?

Our Kolmogorov scale (as defined from the maximum local dissipation rate) is approximately 2.5e-4 m. The Batchelor scale is therefore approximately 1e-5 m for Sc=700.

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For our domain size $(6.4 \times 0.4 \times 0.3)$ this would require about 7.5e14 total points. At our highest resolution we use about 5e8 total points. Hence, we are still a very long way from resolving the Sc=700 case.

28. Page 18, paragraph 10: 'Since the stratification has broadened in this case, the Richardson number has increased leaving the unstable region for shear instabilities to form.' Please, explain better this sentence.

The meaning in this was certainly unclear. We have changed it to read: "The higher diffusivity in the Sc = 1 case acts to hinder the production of shear instabilities by quickly diffusing them as they form."

29. Results: Schmidt number dependence. What is the message from this section? In a thermally stratified fluid (Pr=7) we could expect dynamics such as those shown in Figure 14(a,b).

We were not as clear as we could have been in the purpose of the Schmidt number dependence section. The following sentences have been included in the introduction to motivate this better.

"In terms of the numerical modeling literature, we are interested in exploring how the Schmidt number (or Prandtl number in thermally stratified systems) affects the localized shear instabilities generated near the Kelvin wave crest. This is important since Schmidt numbers representative of salt stratification (Sc \approx 700) are presently intractable for numerical simulations on all but the smallest scales, but realistic results may be obtained by choosing a Schmidt number larger than that for a heat stratified system (Sc \approx 7) but much smaller than that of salt. It also implies that while field scale simulations like those of Sanchez-Garrido and Vlasenko (2009) may have a similar Rossby number to an experimental study, they cannot have the same viscosity and diffusivity, implying that experimentalists need to carefully assess what aspects of such simulations they may successfully observe in the laboratory."

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30. There is a problem with the references, the doi link is duplicated.

Unfortunately this is a problem with the Copernicus bibliography style. We have done what we can to fix it.

31. Abstract: I do not understand what does the last sentence mean: 'Comparisons of equivalent cases with different Schmidt numbers indicate that while low Schmidt number results in the correct general characteristics of the modified ISWs, it does not correctly predict the trailing Poincaré wave field or the intensity and duration of the K-H instabilities'. What is not possible to predict at low Schmidt number (guessing the authors refer to Sc = 1)? How are the authors predicting the trailing Poincaré wave field and the intensity and duration of K-H instabilities?

We have re-written the abstract to clarify this point. We had unwisely used the word 'predict' when 'model' would have been a better choice. By this we mean that a low Schmidt number does not accurately model what we have observed in the higher Schmidt number cases.

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Fig. 1. Velocity along location of maximum amplitude on the focusing wall (x=1.05m in sec-

ondary figure)

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Fig. 2. Vertical velocity along focusing wall during K-H billow formation. Contours are select isopycnals.

