

1 **LABORATORY EXPERIMENTAL INVESTIGATION OF HEAT TRANSPORT IN** 2 **FRACTURED MEDIA**

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9 **Abstract**

10 Low enthalpy geothermal energy is a renewable resource that is still underexploited nowadays, in
11 relation to its potential for development in the society worldwide. Most of its applications have
12 already been investigated, such as: heating and cooling of private and public buildings, roads
13 defrost, cooling of industrial processes, food drying systems or desalination.

14 Geothermal power development is a long, risky and expensive process. It basically consists of
15 successive development stages aimed at locating the resources (exploration), confirming the power
16 generating capacity of the reservoir (confirmation) and building the power plant and associated
17 structures (site development). Different factors intervene in influencing the length, difficulty and
18 materials required for these phases thereby affecting their cost.

19 One of the major limitations related to the installation of low enthalpy geothermal power plants
20 regards the initial development steps which are risky and the upfront capital costs that are huge.

21 Most of the total cost of geothermal power is related to the reimbursement of invested capital and
22 associated returns.

23 In order to increase the optimal efficiency of installations which use groundwater as geothermal
24 resource, flow and heat transport dynamics in aquifers need to be well characterized. Especially in
25 fractured rock aquifers these processes represent critical elements that are not well known.
26 Therefore there is a tendency to oversize geothermal plants.

27 In literature there are very few studies on heat transport especially in fractured media.

28 This study is aimed to deepen the understanding of this topic through heat transport experiments in
29 fractured network and their interpretation.

30 Heat transfer tests have been carried out on the experimental apparatus previously employed to
31 perform flow and tracer transport experiments, which has been modified in order to analyze heat
32 transport dynamics in a network of fractures. In order to model the obtained thermal breakthrough

curves, the Explicit Network Model (ENM) has been used, which is based on an adaptation of a Tang's solution for the transport of the solutes in a semi-infinite single fracture embedded in a porous matrix.

Parameter estimation, time moment analysis, tailing character and other dimensionless parameters have permitted to better understand the dynamics of heat transport and the efficiency of heat exchange between the fractures and matrix. The results have been compared with the previous experimental studies on solute transport.

1 Introduction

An important role in transport of natural resources or contaminant transport through subsurface systems is given by fractured rocks. The interest about the study of dynamics of heat transport in fractured media has grown in recent years because of the development of a wide range of applications, including geothermal energy harvesting (Gisladdottir et al., 2016).

Quantitative geothermal reservoir characterization using tracers is based on different approaches for predicting thermal breakthrough curves in fractured reservoirs (Shook, 2001, Kocabas, 2005, Read et al., 2013).

The characterization and modeling of heat transfer in fractured media is particularly challenging as open and well-connected fractures can induce highly localized pathways which are orders of magnitude more permeable than the rock matrix (Klepikova et al., 2016, Cherubini and Pastore, 2011).

The study of solute transport in fractured media has become recently a widely diffused research topic in hydrogeology (Cherubini, 2008, Cherubini et al., 2008, Cherubini et al., 2009, Cherubini et al., 2013d, Masciopinto et al., 2010), whereas the literature about heat transfer in fractured media is somewhat limited.

Hao et al. (2013) developed a dual continuum model for the representation of discrete fractures and the interaction with surrounding rock matrix in order to give a reliable prediction of the impacts of fracture – matrix interaction on heat transfer in fractured geothermal formations.

Moonen et al. (2011) introduced the concept of cohesive zone which represents a transition zone between the fracture and undamaged material. They proposed a model to adequately represent the influences of fractures or partially damaged material interfaces on heat transfer phenomena.

Geiger and Emmanuel (2010) found that matrix permeability plays an important role on thermal retardations and attenuation of thermal signal. At high matrix permeability, poorly connected fractures can contribute to the heat transport, resulting in heterogeneous heat distributions in the

65 whole matrix block. For lower matrix permeability heat transport occurs mainly through fractures
66 that form a fully connected pathway between the inflow and outflow boundaries, that results in
67 highly non – Fourier behavior, characterized by early breakthrough and long tailing.

68 Numerous field observations (Tsang and Neretnieks, 1998) show that flow in fractures is being
69 organized in channels due to the small scale variations in the fracture aperture. Flow channeling
70 causes dispersion in fractures. Such channels will have a strong influence on the transport
71 characteristics of a fracture, such as, for instance, its thermal exchange area, crucial for geothermal
72 applications (Auradou et al., 2006). Highly channelized flow in fractured geologic systems has been
73 credited with early thermal breakthrough and poor performance of geothermal circulation systems
74 (Hawkins et al., 2012).

75 Lu et. al (2012) conducted experiments of saturated water flow and heat transfer in a regularly
76 fractured granite at meter scale. The experiments indicated that the heat advection due to water flow
77 in vertical fractures nearest to the heat sources played a major role in influencing the spatial
78 distributions and temporal variations of the temperature, impeding heat conduction in transverse
79 direction; such effect increased with larger water fluxes in the fractures and decreased with higher
80 heat source and/or larger distance of the fracture from the heat source.

81 Neuville et al. (2010) showed that fracture – matrix thermal exchange is highly affected by the
82 fracture wall roughness. Natarajan et. al (2010) conducted numerical simulation of thermal transport
83 in a sinusoidal fracture matrix coupled system. They affirmed that this model presents a different
84 behavior respect to the classical parallel plate fracture matrix coupled system. The sinusoidal
85 curvature of the fracture provides high thermal diffusion into the rock matrix.

86 Ouyang (2014) developed a three – equation local thermal non – equilibrium model to predict the
87 effective solid – to – fluid heat transfer coefficient in geothermal system reservoirs. They affirmed
88 that due to the high rock – to – fracture size ratio, the solid thermal resistance effect in the internal
89 rocks cannot be neglected in the effective solid – to fluid heat transfer coefficient. Furthermore the
90 results of this study show that it is not efficient to extract the thermal energy from the rocks if
91 fracture density is not large enough.

92 Analytical and semi-analytical approaches have been developed to describe the dynamics of heat
93 transfer in fractured rocks. Such approaches are amenable to the same mathematical treatment as
94 their counterparts developed for mass transport (Martinez et al., 2014). One of these is the analytical
95 solution derived by Tang et al. (1981).

96 While the equations of solute and thermal transport have the same basic form, the fundamental
97 difference between mass and heat transport is that: 1) solutes are transported through the fractures
98 only, whereas heat is transported through both fractures and matrix, 2) the fracture-matrix exchange
99 is large compared with molecular diffusion. This means that the fracture matrix exchange is more
100 relevant for heat transport than for mass transport. Thus, matrix thermal diffusivity strongly
101 influences the thermal breakthrough curves (BTCs) (Becker and Shapiro, 2003).

102 Contrarily, since the heat capacity of the solids will retard the advance of the thermal front, the
103 advective transport for heat is slower than for solute transport (Rau et al., 2012).

104 The quantification of thermal dispersivity as far as heat transport and its relationship with velocity
105 hasn't been properly addressed experimentally and has got conflicting descriptions in literature (Ma
106 et al., 2012).

107 Most studies neglect the hydrodynamic component of thermal dispersion because of thermal
108 diffusion being more efficient than molecular diffusion by several orders of magnitude (Bear 1972).
109 Analysis of heat transport under natural gradients has commonly neglected hydrodynamic
110 dispersion (e.g., Bredehoeft and Papadopoulos, 1965; Domenico and Palciauskas, 1973; Taniguchi et
111 al., 1999; Reiter, 2001; Ferguson et al., 2006). Dispersive heat transport is often assumed to be
112 represented by thermal conductivity and/or to have little influence in models of relatively large
113 systems and modest fluid flow rates (Bear, 1972, Woodbury and Smith, 1985).

114 Some authors suggest that thermal dispersivity enhances the spreading of thermal energy and
115 should therefore be part of the mathematical description of heat transfer in analogy to solute
116 dispersivity (de Marsily, 1986) and have incorporated this term into their models (e.g., Smith and
117 Chapman, 1983; Hopmans et al., 2002; Niswonger and Prudic, 2003). In the same way, other
118 researchers (e.g., Smith and Chapman, 1983, Ronan et al., 1998, Constanz et al., 2002, Su et al.,
119 2004) have included the thermomechanical dispersion tensor representing mechanical mixing
120 caused by unspecified heterogeneities within the porous medium.

121 On the contrary, some other researchers argue that the enhanced thermal spreading is either
122 negligible or can be described simply by increasing the effective diffusivity, thus the hydrodynamic
123 dispersivity mechanism is inappropriate (Bear, 1972; Bravo et al., 2002, Ingebritsen and Sanford,
124 1998, Keery et al, 2007). Constantz et al. (2003) and Vandenbohede et al. (2009) found that thermal
125 dispersivity was significantly smaller than the solute dispersivity. Others (de Marsily, 1986,
126 Molina-Giraldo et al., 2011) found that thermal and solute dispersivity were on the same order of
127 magnitude.

Tracer tests of both solute and heat were carried out at Bonnaud, Jura, France (deMarsily, 1986) and the thermal dispersivity and solute dispersivity were found of the same order of magnitude.

Bear (1972), Ingebritsen and Sanford (1998), and Hopmans et al. (2002), among others, concluded that the effects of thermal dispersion are negligible compared to conduction and set the former to zero.

However, Hopmans et al (2002) showed that dispersivity is increasingly important at higher flow water velocities, since it is only then that the thermal dispersion term is of the same order of magnitude or larger than the conductive term.

Sauty et al. (1982) suggested that there was a correlation between the apparent thermal conductivity and Darcy velocity thus they included the hydrodynamic dispersion term in the advective-conductive modeling.

Other similar formulations of this concept are present in the literature (e.g., Papadopoulos and Larson, 1978; Smith and Chapman, 1983; Molson et al., 1992). Such treatments have not explicitly distinguished between macrodispersion, which occurs due to variations in permeability over larger scales and the components of hydrodynamic dispersion that occur due to variations in velocity at the pore scale.

One group of authors have utilized a linear relationship to describe the thermal dispersivity and the relationship between thermal dispersivity and fluid velocity (e.g., de Marsily, 1986; Anderson, 2005; Hatch et al., 2006; Keery et al., 2007; Vandenbohede et al., 2009; Vandenbohede and Lebbe, 2010; Rau et al., 2010), while others have identified the possibility of a nonlinear relationship (Green et al., 1964).

The present study is aimed at providing a better understanding of heat transfer mechanisms in fractured rocks. Laboratory experiments on mass and heat transport in a fractured rock sample have been carried out in order to analyze the contribution of thermal dispersion in heat propagation processes, the influence of nonlinear flow dynamics on the enhancement of thermal matrix diffusion and finally the optimal conditions for thermal exchange in a fractured network.

Section 1 shows a short review about mass and heat transport in fractured media highlighting what is still unresolved or contrasting in the literature.

In Section 2 the theoretical background related to non linear flow, solute and heat transport behavior in fractured media has been reported.

158 A better development of the Explicit Network Model (ENM), based on a Tang's solution developed
159 for solute transport in a single semi-infinite fracture inside a porous matrix has been used for the
160 fitting of the thermal BTCs. The ENM model explicitly takes the fracture network geometry into
161 account and therefore permits to understand the physical meaning of mass and heat transfer
162 phenomena and to obtain a more accurate estimation of the related parameters. In analogous way
163 the ENM model has been used in order to fit the observed BTCs obtained from previous
164 experiments on mass transport.

165 Section 3 shows the thermal tracer tests carried out on an artificially created fractured rock sample
166 that has been used in previous studies to analyze nonlinear flow and non Fickian transport dynamics
167 in fractured formations (Cherubini et al., 2012, 2013a, 2013b, 2013c and 2014).

168 In Section 4 have been reported the interpretation of flow and transport experiments together with
169 the fitting of BTCs and interpretation of estimated model parameters. In particular, the obtained
170 thermal BTCs show a more enhanced early arrival and long tailing than solute BTCs.

171 The travel time for solute transport is an order of magnitude lower than for heat transport
172 experiments. Thermal convective velocity is thus more delayed respect to solute transport. The
173 thermal dispersion mechanism dominates heat propagation in the fractured medium in the carried
174 out experiments and thus cannot be neglected.

175 For mass transport the presence of the secondary path and the nonlinear flow regime are the main
176 factors affecting non – Fickian behavior observed in experimental BTCs, whereas for heat transport
177 the non - Fickian nature of the experimental BTCs is governed mainly by the heat exchange
178 mechanism between the fracture network and the surrounding matrix. The presence of a nonlinear
179 flow regime gives rise to a weak growth on heat transfer phenomena.

180 Section 5 reports some practical applications of the knowledges acquired from this study on the
181 convective heat transport in fractured media for exploiting heat recovery and heat dissipation.
182 Furthermore the estimation of the average effective thermal conductivity suggests that there is a
183 solid thermal resistance in the fluid to solid heat transfer processes due to the rock – fracture size
184 ratio. This result matches previous analyses (Pastore et al., 2015) in which a lower heat dissipation
185 respect to the Tang's solution in correspondence of the single fracture surrounded by a matrix with
186 more limited heat capacity has been found.

187 **2 Theoretical background**

188 **2.1 Nonlinear flow**

189 With few exceptions, any fracture can be envisioned as two rough surfaces in contact. In cross
190 section the solid areas representing asperities might be considered as the grains of porous media.

191 Therefore, in most studies examining hydrodynamic processes in fractured media, the general
192 equations describing flow and transport in porous media are applied, such as Darcy's law, that
193 depicts a linear relationship between the pressure gradient and fluid velocity (Whitaker, 1986;
194 Cherubini and Pastore, 2010)

195 However, this linearity has been demonstrated to be valid at low flow regimes ($Re < 1$). For $Re > 1$
196 a nonlinear flow behavior is likely to occur (Cherubini, 2013d).

197 When $Re \gg 1$, a strong inertial regime develops, that can be described by the Forchheimer equation
198 (Forchheimer, 1901):

$$199 \quad -\frac{dp}{dx} = \frac{\mu}{k} \cdot u_f + \rho\beta \cdot u_f^2 \quad (1)$$

200 Where x (m) is the coordinate parallel to the axis of the single fracture (SF), p ($ML^{-1}T^{-2}$) is the flow
201 pressure, μ ($ML^{-1}T^{-1}$) is the dynamic viscosity, k (L^2) is the permeability, u_f (LT^{-1}) is the convective
202 velocity, ρ (ML^{-3}) is the density and β (L^{-1}) is called the inertial resistance coefficient, or non –
203 Darcy coefficient.

204 It is possible to express Forchheimer law in terms of hydraulic head h (L):

$$205 \quad -\frac{dh}{dx} = a' \cdot u_f + b' \cdot u_f^2 \quad (2)$$

206 The coefficients a' (TL^{-1}) and b' (TL^{-2}) represent the linear and inertial coefficient respectively
207 equal to:

$$208 \quad a' = \frac{\mu}{\rho g k}; \quad b' = \frac{\beta}{g} \quad (3)$$

209 The relationship between hydraulic head gradient and flow rate Q (L^3T^{-1}) can be written as:

$$210 \quad -\frac{dh}{dx} = a \cdot Q + b \cdot Q^2 \quad (4)$$

211 The coefficients a (TL^{-3}) and b (T^2L^{-6}) can be related to a' and b' :

$$212 \quad a = \frac{a'}{\omega_{eq}}; \quad b = \frac{b'}{\omega_{eq}^2} \quad (5)$$

213 Where ω_{eq} (L^2) is the equivalent cross sectional area of SF .

214 **2.2 Heat transfer by water flow in single fractures**

215 Fluid flow and heat transfer in a single fracture (SF) undergo advective, diffusive and dispersive
216 phenomena. Dispersion is caused by small scale fracture aperture variations. Flow channeling is one
217 example of macrodispersion caused by preferred flow paths, in that mass and heat tend to migrate
218 through the portions of a fracture with the largest apertures.

219 In fractured media another process is represented by diffusion into surrounding rock matrix. Matrix
220 diffusion attenuates the mass and heat propagation in the fractures.

221 According to the boundary – layer theory (Fahien, 1983), solute mass transfer q_m (ML^{-2}) per unit
222 area at the fracture-matrix interface (Wu et al., 2010) is given by:

$$223 \quad q_M = \frac{D_m}{\delta} (c_f - c_m) \quad (6)$$

224 Where c_f (ML^{-3}) is the concentration across fractures, c_m (ML^{-3}) is the concentration of the matrix
225 block surfaces, D_m (LT^{-2}) is the molecular diffusion coefficient, and δ (m) is the thickness of
226 boundary layer (Wu et al., 2010). For small fractures, δ may become the aperture w_f (m) of the SF .

227 In analogous manner the specific heat transfer flux q_H (MT^{-3}) at the fracture – matrix interface is
228 given by:

$$229 \quad q_H = \frac{k_m}{\delta} (T_f - T_m) \quad (7)$$

230 Where T_f (K) is the temperature across fractures, T_m (K) is the temperature of the matrix block
231 surfaces, k_m ($MLT^{-3}K^{-1}$) is the thermal conductivity.

232 The continuity conditions at the fracture – matrix interface requires a balance between mass transfer
233 rate and mass diffused into the matrix described as:

$$234 \quad q_M = -D_e \left. \frac{\partial c_m}{\partial z} \right|_{z=w_f/2} \quad (8)$$

235 Where z (m) is the coordinate perpendicular to the fracture axis and w_f is the aperture of the
236 fracture.

237 In the same way the specific heat flux must be balanced by heat diffused into the matrix described
 238 as:

$$239 \quad q_H = -k_e \frac{\partial T_m}{\partial z} \bigg|_{z=w_f/2} \quad (9)$$

240 The effective diffusion coefficient takes into account the fact that diffusion can only take place
 241 through pore and fracture openings because mineral grains block many of the possible pathways.
 242 The effective thermal conductivity of a formation consisting of multiple components depends on the
 243 geometrical configuration of the components as well as on the thermal conductivity of each.

244 The effective terms (D_e instead of D_m and k_e instead of k_m) have been introduced in order to include
 245 the effect of various system parameters such as fluid velocity, porosity, surface area, roughness, that
 246 may enhance mass and heat transfer effect. For instance, when large flow velocity occurs,
 247 convective transport is stronger along the centre of the fracture, enhancing the concentration or
 248 temperature gradient at the fracture matrix interface. As known roughness plays an important role in
 249 increasing mass or heat transfer because of increasing turbulent flow conditions.

250 According to Bodin (2007) the governing equation for the one dimensional advective - dispersive
 251 transport along the axis of a semi-infinite fracture with one – dimensional diffusion in the rock
 252 matrix, in perpendicular direction to the axis of the fracture is:

$$253 \quad \frac{\partial c_f}{\partial t} + u_f \frac{\partial c_f}{\partial x} = \frac{\partial}{\partial x} \left(D_f \frac{\partial c_f}{\partial x} \right) - \frac{D_e}{\delta} \frac{\partial c_m}{\partial z} \bigg|_{z=w_f/2} \quad (10)$$

254 Where D_f (L^2T^{-1}) is the dispersion. The latter mainly depends on two processes: Aris – Taylor
 255 dispersion and geometrical dispersion. Previous experiments (Cherubini et al., 2012, 2013a, 2013b,
 256 2013c and 2014) show that, due to the complex geometrical and topological characteristics of the
 257 fracture network that create tortuous flow paths, Aris – Taylor dispersion may not develop. A linear
 258 relationship has been found between velocity and dispersion so geometrical dispersion is mostly
 259 responsible for the mixing process along the fracture:

$$260 \quad D_f = \alpha_{LM} u_f \quad (11)$$

261 Where α_{LM} (L) is the dispersivity coefficient for mass transport.

262 Assuming that fluid flow velocity in the surrounding rock matrix is equal to zero, the equation for
 263 the conservation of heat in the matrix is given by:

$$\frac{\partial c_m}{\partial t} = D_a \frac{\partial^2 c_m}{\partial z^2} \quad (12)$$

Where D_a is the apparent diffusion coefficient of the solute in the matrix expressed as function of the matrix porosity θ_m , $D_a = D_e / \theta_m$ (Bodin et al., 2007).

Tang et al. (1981) presented an analytical solution for solute transport in semi – infinite single fracture embedded in a porous rock matrix with a constant concentration at the fracture inlet ($x = 0$) equal to c_0 (ML^{-3}) and with an initial concentration equal to zero. The solute concentration in the fracture \bar{c}_f and in the matrix \bar{c}_m has been given as function of time in Laplace space as follows:

$$\bar{c}_f = \frac{c_0}{s} \exp(\nu L) \exp \left[-\nu L \left\{ 1 + \beta^2 \left(\frac{s^{1/2}}{A} + s \right) \right\}^{1/2} \right] \quad (13)$$

$$\bar{c}_m = \bar{c}_f \exp \left[-Bs^{1/2} (z - w_f / 2) \right] \quad (14)$$

Where s is the integral variable of the Laplace transform, L (L) is the length of SF , the ν , A , β^2 and B coefficients are expressed as follows: $\nu = \frac{u_f}{2D_f}$ (15)

$$A = \frac{\delta}{\sqrt{\theta_m D_e}} \quad (16)$$

$$\beta^2 = \frac{4D_f}{u_f^2} \quad (17)$$

$$B = \frac{1}{\sqrt{D_e}} \quad (18)$$

Whereas the gradient of \bar{c}_m at the interface $z = w_f/2$ is:

$$\left. \frac{d\bar{c}_m}{dx} \right|_{x=w_f/2} = -\bar{c}_f B s^{1/2} \quad (19)$$

Defined the residence time as the average amount of time that the solute spends in the system, on the basis of these analytical solutions the probability density function (*PDF*) of the solute residence time in the single fracture in the Laplace space can be expressed as:

$$\bar{\Gamma}(s) = \exp(\nu L) \exp \left[-\nu L \left\{ 1 + \beta^2 \left(\frac{s^{1/2}}{A} + s \right) \right\}^{1/2} \right] \quad (20)$$

Assuming that density and heat capacity are constant in time, the heat transport conservation equation in SF can be expressed as follows:

$$\frac{\partial T_f}{\partial t} + u_f \frac{\partial T_f}{\partial x} = \frac{\partial}{\partial x} \left(D_{fH} \frac{\partial T_f}{\partial x} \right) - \frac{k_e}{\rho_w C_w \delta} \frac{\partial T_m}{\partial z} \Big|_{z=w_f/2} \quad (21)$$

Where ρ_w (ML^{-3}), C_w ($\text{L}^2\text{T}^2\text{K}^{-1}$) represent the density, the specific heat capacity of the fluid within SF respectively. D_f for heat transport assumes the following expression:

$$D_{fH} = \frac{\lambda_L}{\rho_w C_w} \quad (22)$$

Where λ_L is the thermodynamic dispersion coefficient ($\text{MLT}^{-3}\text{K}^{-1}$). Sauty et al. (1982) and de Marsily (1986) proposed an expression for the thermal dispersion coefficient where the thermal dispersion term varies linearly with velocity and depends on the heterogeneity of the medium, as for solute transport:

$$\lambda_L = k_0 + \alpha_{LH} \rho_w C_w u_f \quad (23)$$

Where k_0 is the bulk thermal conductivity ($\text{MLT}^{-3}\text{K}^{-1}$) and α_{LH} (L) is the longitudinal thermal dispersivity.

The heat transport conservation equation in the matrix is expressed as follows:

$$\rho_m C_m \frac{\partial T_m}{\partial t} = k_e \frac{\partial^2 T_m}{\partial z^2} \quad (24)$$

Note that the governing equations of heat and mass transport highlight similarities between the two processes, thus Tang's solution can be used also for heat transport.

In terms of heat transport, the coefficients ν , A , β^2 and B are expressed as follows:

$$\nu = \frac{u_f}{2D_{fH}} \quad (25)$$

$$A = \frac{\delta}{\sqrt{\theta D_e}} \quad (26)$$

where $\theta = \rho_m C_m / \rho_w C_w$ and $D_e = k_e / \rho_w C_w$.

$$\beta^2 = \frac{4D_f}{u_f^2} \quad (27)$$

$$B = \frac{1}{\sqrt{D_e}} \quad (28)$$

Three characteristic time scales can be defined:

$$t_u = \frac{L}{u_f}; \quad t_d = \frac{L^2}{D_f}; \quad t_e = \frac{\delta^2}{D_e} \quad (29)$$

Where L (L) is the characteristic length, t_u (T), t_d (T) and t_e (T) represent the characteristics time scales of convective transport, dispersive transport and loss of the mass or heat into the surrounding matrix.

The relative effect of dispersion, convection and matrix diffusion on mass or heat propagation in the fracture can be evaluated by comparing the corresponding time scale.

Peclet number Pe is defined as the ratio between dispersive (t_d) to convective (t_u) transport times:

$$Pe = \frac{t_d}{t_u} = \frac{u_f L}{D_f} \quad (30)$$

At high Peclet numbers transport processes are mainly governed by convection, whereas at low Peclet numbers it is mainly dispersion that dominates.

Another useful dimensionless number, generally applied in chemical engineering, is the Damköhler number that can be used in order to evaluate the influence of matrix diffusion on convection phenomena. Da relates the convection time scale to the exchange time scale.

$$Da = \frac{t_u}{t_e} = \frac{\alpha L}{u_f} \quad (31)$$

Where α (T^{-1}) is the exchange rate coefficient corresponding to:

$$\alpha = \frac{D_e}{\delta^2} \quad (32)$$

Note that the inverse of t_e has the same meaning of the exchange rate coefficient α (T^{-1}).

When t_e values are of the same order of magnitude as the transport time t_u ($Da \approx 1$), diffusive processes in the matrix are more relevant. In this case concentration or temperature distribution profiles are characterized by a long tail.

When $t_e \gg t_u$ ($Da \ll 1$) the fracture – matrix exchange is very slow and it does not influence mass or heat propagation. On the contrary when $t_e \ll t_u$ ($Da \gg 1$) the fracture matrix exchange is rapid, there is instantaneous equilibrium between fracture and matrix and they have the same concentration or temperature. These two circumstances close the standard advective – dispersive transport equation.

The product between Pe and Da represents another dimensionless group which is a measure of transport processes:

$$Pe \times Da = \frac{t_d}{t_e} = \frac{\alpha L^2}{D_f} \quad (33)$$

When $Pe \times Da$ increases t_e decreases more rapidly than t_d , and subsequently the mass or heat diffusion into the matrix may be dominant on the longitudinal dispersion.

2.3 Explicit network model (ENM)

The 2D Explicit Network Model (ENM) depicts the fractures as 1D pipe elements forming a 2D – pipe network and therefore expressly takes the fracture network geometry into account. The ENM model permits to understand the physical meaning of flow and transport phenomena and therefore to obtain a more accurate estimation of flow and transport parameters.

With the assumption that a j^{th} SF can be schematized by a 1D – pipe element, the Forchheimer model can be used to write the relationship between head loss Δh_j (L) and flow rate Q_j ($L^3 T^{-1}$) in finite terms:

$$\frac{\Delta h_j}{L_j} = a Q_j + b Q_j^2 \Rightarrow \Delta h_j = \left[L_j (a + b Q_j) \right] Q_j \quad (34)$$

Where L_j (L) is the length of j^{th} SF, a (TL^{-3}) and b (T^2L^{-6}) represent the Forchheimer parameters written in finite terms. The term in the square brackets constitutes the resistance to flow $R_j(Q_j)$ (TL^{-2}) of j^{th} SF.

In case of steady – state conditions and for a simple 2D fracture network geometry, a straightforward manner can be applied to obtain the solution of flow field by applying the first and second Kirchhoff's laws.

In a 2D fracture network, fractures can be arranged in series and/or in parallel. Specifically, in a network in which fractures are set in a chain, the total resistance to flow is calculated by simply adding up the resistance values of each single fracture. The flow in a parallel fracture network breaks up, with some flowing along each parallel branch and re – combining when the branches meet again. In order to estimate the total resistance to flow the reciprocals of the resistance values have to be added up and then the reciprocal of the total has to be calculated. The flow rate Q_j across the generic fracture j of the parallel network can be calculated as (Cherubini et al., 2014):

$$Q_j = \sum_{i=1}^n Q_i \left[\frac{1}{R_j} \left(\sum_{i=1}^n \frac{1}{R_i} \right)^{-1} \right] \quad (35)$$

Where $\sum_{i=1}^n Q_i$ (LT^{-3}) is the sum of the mass flow rates at fracture intersections in correspondence of the inlet bond of j fracture, whereas the term in square brackets represents the probability of water distribution of j fracture $P_{Q,j}$.

Once known the flow field in the fracture network, to obtain the *PDF* at a generic node the *PDFs* of each elementary path that reaches the node have to be summed up. They can be calculated as the convolution product of the *PDFs* of each single fracture composing the elementary path.

Definitely the BTC describing the concentration in the fracture as function of time at the generic node, using the convolution theorem, can be obtained as follows:

$$c_f(t) = c_0 + c_{inj}(t) * L^{-1} \left[\sum_{i=1}^{N_p} \prod_{j=1}^{n_{f,i}} P_{M,j} \bar{\Gamma}_j(s) \right] \quad (36)$$

Where c_0 (ML^{-3}) is the initial concentration and c_{inj} (ML^{-3}) is the concentration injection function, $*$ is the convolution operator, L^{-1} represents the inverse Laplace transform operator, N_p is the number of the paths reaching the node, $n_{f,i}$ is the number of the SF belonging to the elementary path i^{th} , $P_{M,j}$

373 and $\bar{\Gamma}(s)$ are the mass distribution probability and the *PDF* in the Laplace space of the generic j^{th}
 374 *SF* respectively. Inverse Laplace transform L^{-1} can be solved numerically using Abate et al. (2006)
 375 algorithm.

376 At the same way the BTC T_f which describes the temperature in the fracture as function of time at
 377 the generic node can be written as:

$$378 \quad T_f(t) = T_0 + T_{inj}(t) * L^{-1} \left[\sum_{i=1}^{N_p} \prod_{j=1}^{n_{f,i}} P_{H,j} \bar{\Gamma}_j(s) \right] \quad (37)$$

379 Where T_0 (K) is the initial temperature, T_{inj} (K) is the temperature injection function and $P_{H,j}$ is the
 380 heat distribution probability.

381 $P_{M,j}$ and $P_{H,j}$ can be estimated as the probabilities of the mass and heat distribution at the inlet bond
 382 of each individual *SF* respectively. The mass and heat distribution is proportional to the
 383 correspondent flow rates:

$$384 \quad P_{M,j} = P_{H,j} = \frac{Q_j}{\sum_{i=1}^n Q_i} \quad (38)$$

385 Note that if Equation 38 is valid, the probability of water distribution is equal to the probabilities of
 386 mass and heat distribution (term in square brackets in Equation 34). Definitely the ENM model
 387 regarding each *SF* can be described by four parameters ($u_{f,j}$, $D_{f,j}$, α_j , $P_{Q,j}$).

388 **3 Material and methods**

389 **3.1 Description of the experimental apparatus**

390 The heat transfer tests have been carried out on the experimental apparatus previously employed to
 391 perform flow and tracer transport experiments at bench scale (Cherubini et al. 2012, 2013a, 2013b,
 392 2013c and 2014). However, the apparatus has been modified in order to analyze heat transport
 393 dynamics. Two thermocouples have been placed at the inlet and the outlet of a selected fracture
 394 path of the limestone block with parallelepiped shape ($0.6 \times 0.4 \times 0.08 \text{ m}^3$) described in previous
 395 studies. A TC – 08 Thermocouple Data Logger (pico Technology) with a sampling rate of 1 second
 396 has been connected to the thermocouples. An extruded polystyrene panel with thermal conductivity
 397 equal to $0.034 \text{ Wm}^{-1}\text{K}^{-1}$ and thickness 0.05 m has been used to thermally insulate the limestone
 398 block which has then been connected to a hydraulic circuit. The head loss between the upstream

399 tank connected to the inlet port and the downstream tank connected to the outlet port drives flow of
 400 water through the fractured block. An ultrasonic velocimeter (DOP3000 by Signal Processing) has
 401 been adopted to measure the instantaneous flow rate that flows across the block. An electric boiler
 402 with a volume of 10^{-2} m^3 has been used to heat the water. In a flow cell located in correspondence
 403 of the outlet port a multiparametric probe is positioned for the instantaneous measurement of
 404 pressure (dbar), temperature ($^{\circ}\text{C}$) and electric conductivity ($\mu\text{S cm}^{-1}$). Figure 1a shows the fractured
 405 block sealed with epoxy resin, Figure 1b shows the thermal insulated fractured block connected to
 406 the hydraulic circuit, whereas the schematic diagram of the experimental apparatus is shown in
 407 Figure 2.

408 3.2 Flow experiments.

409 The average flow rate through the selected path can be evaluated as:

$$410 \quad \bar{Q} = \frac{S_I}{t_1 - t_0} (h_1 - h_0) \quad (39)$$

411 Where $S_I \text{ (L}^2\text{)}$ is the cross section area of the flow cell, $\Delta t = t_1 - t_0$ is the time for the flow cell to be
 412 filled from $h_0 \text{ (L)}$ and $h_1 \text{ (L)}$. To calculate the head loss between the upstream tank and the flow cell
 413 the following expression is adopted:

$$414 \quad \Delta h = h_c - \frac{h_0 + h_1}{2} \quad (40)$$

415 Where h_c is the hydraulic head measured in the upstream tank. Several tests have been carried out
 416 varying the control head, and in correspondence of each value of the average flow rate and head
 417 loss the average resistance to flow has been determined as:

$$418 \quad \bar{R}(\bar{Q}) = \left[\frac{S_I}{t_1 - t_0} \ln \left(\frac{h_0 - h_c}{h_1 - h_c} \right) \right]^{-1} \quad (41)$$

419 3.3 Solute and temperature tracer tests

420 Solute and temperature tracer tests have been conducted through the following steps.

421 As initial condition, a specific value of hydraulic head difference between the upstream tank and
 422 downstream tank has been assigned. At $t = 0$ the valve a is closed so as the hydrostatic head inside
 423 the block assumes the same value to the one in the downstream tank. At $t = 10 \text{ s}$ the valve a is
 424 opened.

425 For solute tracer test at time $t = 60$ s by means of a syringe, a mass of 5×10^{-4} kg sodium chloride is
 426 injected into the inlet port. Due to the very short source release time, the instantaneous source
 427 assumption can be adopted which assumes the source of solute as an instantaneous injection (pulse).
 428 The multiparametric probe located within the flow cell measures the solute BTC.

429 As concerns thermal tracer tests at the time $t = 60$ s the valve d is opened while the valve c is
 430 closed. In such a way a step temperature function in correspondence of the inlet port $T_{inj}(t)$ is
 431 imposed and measured by the first thermocouple. The other thermocouple located inside the outlet
 432 port is used to measure the thermal BTC.

433 The ultrasonic velocimeter is used in order to measure the instantaneous flow rate, whereas a
 434 multiparametric probe located at the outlet port measures the pressure and the electric conductivity.

435 **4 Results and discussion**

436 **4.1 Flow characteristics**

437 The Kirchhoff laws have been used in order to estimate the flow rates flowing in each single
 438 fracture. In Figure 3 a sketch of the 2D pipe conceptualization of the fracture network is reported.

439 The resistance to flow of each SF can be evaluated as the square bracket in Equation (34). For
 440 simplicity the linear and non linear terms have been considered constant and equal for each SF .

441 The resistance to flow for the whole fracture network $\bar{R}(\bar{Q})$ can be evaluated as the sum of the
 442 resistance to flow of each SF arranged in chain and the total resistance of the parallel branches
 443 equal to the reciprocal of the sum of the reciprocal of the resistance to flow of each parallel branch:

$$444 \quad \bar{R}(\bar{Q}) = R_1(Q_0) + R_2(Q_0) + \left(\frac{1}{R_6(Q_1)} + \frac{1}{R_3(Q_2) + R_4(Q_2) + R_5(Q_2)} \right)^{-1} + \quad (42)$$

$$+ R_7(Q_0) + R_8(Q_0) + R_9(Q_0)$$

445 Where R_j with $j = 1 - 9$ represents the resistance to flow of each SF , Q_0 is the injection flow rate,
 446 Q_1 and Q_2 are the flow rates flowing in the parallel branch 6 and 3 – 4 – 5 respectively.

447 The flow rate Q_1 is determined in iterative manner using the following iterative equation derived by
 448 the Equation (35) at the node 3:

$$Q_1^{k+1} = Q_0 \left[\frac{1}{R_6(Q_1^k)} \left(\frac{1}{R_3(Q_0 - Q_1^k) + R_4(Q_0 - Q_1^k) + R_5(Q_0 - Q_1^k)} + \frac{1}{R_6(Q_1^k)} \right)^{-1} \right] \quad (43)$$

Whereas the flow rate Q_2 is determined merely as:

$$Q_2 = Q_0 - Q_1 \quad (44)$$

The linear and nonlinear terms representative of the whole fracture network have been estimated matching the average experimental resistance to flow resulting from Equation (41) with resistance to flow estimated from Equation (42).

The linear and nonlinear term are equal respectively to $a = 7.345 \times 10^4 \text{ sm}^{-3}$ and $b = 11.65 \times 10^9 \text{ s}^2 \text{ m}^{-6}$. Inertial forces dominate viscous ones when the Forchheimer number (Fo) is higher than one. Fo can be evaluated as the ratio between the non linear loss (bQ^2) and the linear loss (aQ). The critical flow rate Q_{crit} which represents the value of flow rate for which $Fo = 1$ is derived as the ratio between a and b resulting $Q_{crit} = 6.30 \times 10^{-6} \text{ m}^3 \text{ s}^{-1}$.

Because of the nonlinearity of flow, varying the inlet flow rate Q_0 the ratio between the flow rates Q_1 and Q_2 flowing respectively in the branches 6 and 3 – 5 is not constant. When Q_0 increases Q_2 increases faster than Q_1 . The probability of water distribution of the branch 6 $P_{Q,6}$ is evaluated as the ratio between Q_0 and Q_1 , whereas the probability of water distribution of the branch 3 – 5 is equal to $P_{Q,3-5} = 1 - P_{Q,6}$.

4.2 Fitting of breakthrough curves and interpretation of estimated model parameters

The behavior of mass and heat transport has been compared varying the injection flow rates. In particular 21 tests in the range $1.83 \times 10^{-6} - 1.26 \times 10^{-5} \text{ m}^3 \text{ s}^{-1}$ (Re in the range 17.5 – 78.71) for heat transport have been made and compared with the 55 tests in the range $1.32 \times 10^{-6} - 8.34 \times 10^{-6} \text{ m}^3 \text{ s}^{-1}$ (Re in the range 8.2 – 52.1) for solute transport presented in previous studies.

The observed heat and mass BTCs for different flow rates have been individually fitted using the ENM approach presented in section 2.3. For simplicity the transport parameters u_f , D_f and α are assumed equal for all branches of the fracture network. The probability of mass and heat distribution are assumed equal to the probability of water distribution.

474 The experimental BTCs are fitted using Equation (36) and Equation (37) for mass and heat
475 transport respectively. Note that for mass transport $c_{inj}(t)$ supposing the instantaneous injection
476 condition becomes a Dirac delta function.

477 The determination coefficient (r^2) and the root mean square error ($RMSE$) have been used in order
478 to evaluate the goodness of fit.

479 Tables 1 and 2 show the values of transport parameters, the $RMSE$ and r^2 for mass and heat
480 transport respectively. Furthermore Figure 4 and Figure 5 show the fitting results of BTCs for some
481 values of Q_0 .

482 The results presented in Tables 1 and 2 highlight that: the estimated convective velocities u_f for heat
483 transport are lower than for mass transport. Whereas the estimated dispersion D_f for heat transport is
484 higher than for mass transport. Regarding the transfer rate coefficient α , it assumes very low values
485 for mass transport relatively to the convective velocity. Instead for heat transport the exchange rate
486 coefficient is of the same order of magnitude of the convective velocity and, considering a
487 characteristic length equal to $L = 0.601$ m corresponding to the length of the main path of the
488 fracture network, the effect of dual – porosity is very strong and cannot be neglected relatively to
489 the investigated injection flow range. Both mass and heat transport show a satisfactory fitting. In
490 particular manner, $RMSE$ varies in the range 0.0015 – 0.0180 for mass transport and in the range
491 0.0030 – 0.236 for heat transport, whereas r^2 varies in the range 0.9863 – 0.9987 for mass transport
492 and in the range 0.0963 – 0.9998 for heat transport.

493 In order to investigate the different behavior between mass and heat transport, the relationships
494 between injection flow rate and the transport parameters have been analyzed. In Figure 6 the
495 relationship between u_f and Q_0 is reported. Whereas in Figures 7 and 8 are reported the dispersion
496 coefficient D_f and the exchange term α as function of u_f respectively. The figures show a very
497 different behavior between mass and heat transport.

498 Regarding mass transport experiments according to previous studies (Cherubini at al., 2013a,
499 2013b, 2013c and 2014) the figure 5 shows that for values of Q_0 higher than $4 \times 10^{-6} \text{ m}^3 \text{ s}^{-1}$ u_f
500 increases less rapidly. This behavior was due to the presence of inertial forces that gave rise to a
501 retardation effect on solute transport.

502 Instead Figure 7 shows a linear relationship between u_f and D_f suggesting that inertial forces did not
503 exert any effect on dispersion and that geometrical dispersion dominates the Aris – Taylor
504 dispersion.

505 In the same way as for mass transport, for heat transfer a linear relationship is evident between
 506 dispersion and convective velocity. Even if heat convective velocity is lower than solute advective
 507 velocity, the longitudinal thermal dispersivity assumes higher values than the longitudinal solute
 508 dispersivity. Also for heat transport experiments a linear relationship between u_f and D_f has been
 509 found.

510 Figure 8 shows the exchange rate coefficient α as function of the convective velocity u_f for both
 511 mass and heat transport.

512 Regarding the mass transport, the estimated exchange rate coefficient α is much lower than the
 513 convective velocity. These results suggest that in the case study fracture – matrix exchange is very
 514 slow and it may not influence mass transport. Non Fickian behavior observed in the experimental
 515 BTCs is therefore dominated mainly by the presence of inertial forces and the parallel branches.

516 A very different behavior is observed for heat transport. Heat convective velocity does not seem to
 517 be influenced by the presence of the inertial force whereas u_f is influenced by fracture matrix
 518 exchange phenomena resulting in a significant retardation effect. Once the model parameters for
 519 each flow rate have been determined, the unit response function (f_{URF}), corresponding to the *PDF*
 520 obtained from impulsive injection of both solute and temperature tracers, is obtained. The unit
 521 response function can be characterized using the time moments and tail character analysis.

522 The mean residence time t_m assumes the following expression:

$$523 \quad t_m = \frac{\int_0^{\infty} t f_{URF}(t) dt}{\int_0^{\infty} f_{URF}(t) dt} \quad (45)$$

524 Whereas the n^{th} normalized central moment of distribution of the f_{URF} versus time can be written as:

$$525 \quad \mu_n = \frac{\int_0^{\infty} (t - t_m)^n f_{URF}(t) dt}{\int_0^{\infty} f_{URF}(t) dt} \quad (46)$$

526 The second moment μ_2 can be used in order to evaluate the dispersion relative to t_m , whereas the
 527 skewness is a measure of the degree of asymmetry and it is defined as follows:

$$528 \quad S = \mu_3 / \mu_2^{3/2} \quad (47)$$

529 The tailing character t_c can be described as:

$$t_c = \frac{\Delta t_{fall}}{\Delta t_{rise}} \quad (48)$$

Where Δt_{fall} denotes the duration of the falling limb defined as the time interval from the peak to the tail cutoff which is the time when the falling limb first reaches a value that is 0.05 times the peak value. Δt_{rise} is defined as the time interval from the first arrival to the peak. This quantity provides a measure of the asymmetry between the rising and falling limbs. A value of t_c significantly higher than 1 indicates an elongated tail compared to the rising limb (Cherubini et al., 2010).

In Figure 9 is reported the residence time versus the injection flow rates. The figure highlights that t_m for heat transport is about 3 times higher than for mass transport. In particular way t_m varies in the range 40.3 - 237.1 s for mass transport and in the range 147.8 – 506.9 s for heat transport. This result still highlights that heat transport is more delayed than mass transport.

In same way the skewness S (Figure 10) and tailing character t_c (Figure 11) are reported as function of Q_0 .

A different behavior for heat and mass transport is observed for the skewness coefficient. For heat transfer the skewness shows a growth trend which seems to decrease after $Q_0 = 3 \times 10^{-6} \text{ m}^3 \text{ s}^{-1}$. Its mean value is equal to 2.714. For solute transport the S does not show a trend, and assumes a mean value equal to 2.018.

The tailing character does not exhibit a trend for both mass and heat transport. In either cases t_c is significantly higher than 1, specifically 7.70 and 30.99 for mass and heat transport respectively.

In order to explain the transport dynamics, the trends of dimensionless numbers Pe and Da varying the injection flow rate have been investigated. The Figure 12 shows the Pe as function of Q_0 for both mass and heat experiments. As concerns mass experiments Pe increases as Q_0 increases, assuming a constant value for high values ($Pe = 7.5$) of Q_0 . For heat transport a different behavior is observed, Pe showing a constant trend and being always lower than one. Even if the injection flow rate is relatively high, thermal dispersion is the dominating mechanism in heat transfer.

Figure 12 reports Da as function of Q_0 . For mass transport Da assumes very low values, of the order of magnitude of 10^{-4} .

The convective transport scale is very low respect to the exchange transport scale, thus the mass transport in each single fracture can be represented with the classical advection dispersion model.

As regards heat transport Da assumes values around the unit showing a downward trend as injection flow rate increases switching from higher to lower values than the unit. As injection flow rate increases the convective transport time scale reduces more rapidly than the exchange time scale.

These arguments can be explained because the relationships between Q_0 and u_f show a change of slope when Da becomes lower than the unit. In other words when Da is higher than the unit the exchange between fracture and matrix dominates on the convective transport giving rise to a more enhanced delay on heat transport, conversely when Da is lower than one convective transport dominates on fracture- matrix interactions and the delay effect is reduced.

Furthermore this effect is evident also on the trend observed in the graph $S - Q_0$ (Figure 10). For values of Da lower than the unit a change of slope is evident, the skewness coefficient increases more slowly. Thus for $Da > 1$ the early arrival and the tail effect of BTC increase more rapidly than for $Da < 1$.

Note that even if Da presents a downward trend as Q_0 increases, when the latter exceeds Q_{crit} a weak growth trend for Da is detected, that however assumes values lower than the unit.

The Figure 14 shows the dimensionless group $Pe \times Da$ varying the injection flow rate. Regarding mass transport $Pe \times Da$ is of the order of magnitude of 10^{-3} confirming the fact that the fracture – matrix interaction can be neglected relatively to the investigated range of injection flow rates. For heat transport $Pe \times Da$ assumes values just below the unit, with a downward trend as Q_0 increases. t_d and t_e have the same order of magnitude.

In order to find the optimal conditions for heat transfer in the analyzed fractured medium the thermal power exchanged per unit temperature difference \dot{Q} ($ML^2T^{-1}K^{-1}$) for each injection flow rate in quasi steady state conditions can be estimated. The thermal power exchanged can be written as:

$$\dot{Q} = \rho C_w Q_0 (T_{inj} - T_{out}) \quad (49)$$

The outlet temperature T_{out} can be evaluated as function of the f_{URF} using the following expression:

$$T_{out} = T_0 + (T_{inj} - T_0) \int_0^\infty f_{URF}(t) dt \quad (50)$$

Substituting the Equation (50) in the Equation (49) the thermal power exchanged per unit temperature difference is:

$$\frac{\dot{Q}}{(T_{inj} - T_0)} = \left(1 - \int_0^\infty f_{URF}(t) dt\right) \rho C_w Q_0 \quad (51)$$

Figure 15 shows the similarities between the relationship $\dot{Q}/(T_{inj} - T_0) - Q_0$ (Figure 15a) and $Da - Q_0$ (Figure 14b). Higher Da values correspond to higher values of $\dot{Q}/(T_{inj} - T_0)$. The thermal power exchanged increases as the Damköhler number increases as shown in Figure 15c. These results highlight that for the observed case study the optimal condition for thermal exchange in the fractured medium is obtained when the exchange time scale is lower than the convective transport scale or rather when the dynamics of fracture – matrix exchange are dominant on the convective ones.

Moreover in a similar way to Da , $\dot{Q}/(T_{inj} - T_0)$ shows a weak growth trend when Q_0 exceeds Q_{crit} . This means that the nonlinear flow regime improves the fracture – matrix thermal exchange, however at high values of injection flow rates convective and dispersion time scales are less than the exchange time scale. Nevertheless these results have been observed in a small range of Da numbers close to the unit. In order to generalize these results a larger range of Da numbers should be investigated.

In order to estimate the effective thermal conductivity coefficient k_e , the principle of conservation of heat energy can be applied to the whole fractured medium. Neglecting the heat stored in the fractures, the difference between the heat measured at the inlet and at the outlet must be equal to the heat diffused into the matrix:

$$\rho C_w Q_0 (T_{inj} - T_{out}) = \int_{A_f} k_e \frac{dT_m}{dz} \Big|_{z=wf/2} dA_f \quad (52)$$

where A_f is the whole surface area of the whole active fracture network and the gradient of T_m can be evaluated according to Equation (19) using temperature instead of concentration as variable.

Then the average effective thermal conductivity \bar{k}_e can be obtained as:

$$\bar{k}_e = \frac{\rho_w C_w Q_0 (T_{inj} - T_{out})}{\int_{A_f} \frac{dT}{dz} \Big|_{z=wf/2} dA_f} \quad (53)$$

609 The average effective thermal conductivity has been estimated for each injection flow rate (Figure
610 16) and assumes a mean value equal to $\bar{k}_e = 0.1183 \text{ Wm}^{-1}\text{K}^{-1}$. The estimated \bar{k}_e is one order of
611 magnitude lower than the thermal conductivity coefficient reported in the literature (Robertson,
612 1988). Fractured media have a lower capacity for diffusion as opposed to the Tang's model which
613 has unlimited capacity. There is a solid thermal resistance in the fluid to solid heat transfer
614 processes which depends on the rock – fracture size ratio.

615 This result is coherent with previous analyses on heat transfer carried out on the same rock sample
616 (Pastore et al., 2015). In this study Pastore et al. (2015) found that the ENM model failed to model
617 the behavior of heat transport in correspondence of parallel branches where the hypothesis of
618 Tang's solution of single fracture embedded in a porous medium having unlimited capacity cannot
619 be considered valid. In parallel branches the observed BTCs are characterized by less retardation of
620 heat propagation as opposed to the simulated BTCs.

621 **5 Conclusions**

622 Aquifers offer a possibility of exploiting geothermal energy by withdrawing the heat from
623 groundwater by means of a heat pump and subsequently supplying the water back into the aquifer
624 through an injection well. In order to optimize the efficiency of the heat transfer system and
625 minimize the environmental impacts, it is necessary to study the behavior of convective heat
626 transport especially in fractured media, where flow and heat transport processes are not well known.

627 Laboratory experiments on the observation of mass and heat transport in a fractured rock sample
628 have been carried out in order to analyse the contribution of thermal dispersion in heat propagation
629 processes, the contribution of nonlinear flow dynamics on the enhancement of thermal matrix
630 diffusion and finally the optimal heat recovery and heat dissipation strategies.

631 The parameters that control mass and heat transport have been estimated using the ENM model
632 based on Tang's solution.

633 Heat transport shows a very different behavior compared to mass transport. The estimated transport
634 parameters show differences of several orders of magnitude. Convective thermal velocity is lower
635 than solute velocity, whereas thermal dispersion is higher than solute dispersion, mass transfer rate
636 assumes a very low value suggesting that fracture – matrix mass exchange can be neglected. Non -
637 fickian behavior of observed solute BTCs is mainly due to the presence of the secondary path and
638 nonlinear flow regime. Contrarily heat transfer rate is comparable with convective thermal velocity
639 giving rise to a retardation effect on heat propagation in the fracture network.

640 The discrepancies detected in transport parameters are moreover observable through the time
641 moment and tail character analysis which demonstrate that the dual porosity behavior is more
642 evident in the thermal BTCs than in the solute BTCs.

643 The dimensionless analysis carried out on the transport parameters proves that as the injection flow
644 rate increases thermal convection time scale decreases more rapidly than the thermal exchange time
645 scale, explaining the reason why the relationship $Q_0 - u_f$ shows a change of slope for Da lower than
646 the unit.

647 Thermal dispersion dominates heat transport dynamics, the Peclet number and the product between
648 Peclet number and Damköhler number is almost always less than the unit.

649 The optimal conditions for thermal exchange in a fracture network have been investigated. The
650 power exchanged increases in a potential way as Da increases in the observed range.

651 The Explicit Network Model is an efficient computation methodology to represent flow, mass and
652 heat transport in fractured media, as 2D and/or 3D problems are reduced to resolve a network of 1D
653 pipe elements. Unfortunately in field case studies it is difficult to obtain the full knowledge of the
654 geometry and parameters such as the orientations and aperture distributions of the fractures needed
655 by the ENM even by means of field investigation methods. However in real case studies the ENM
656 can be coupled with continuum models in order to represent greater discontinuities respect to the
657 scale of study that generally give rise to preferential pathways for flow, mass and heat transport.

658 A method to represent the topology of the fracture network is represented by multi fractal analysis
659 analysis as discussed in Tijera at al. (2009) and Tarquis at al. 2014.

660 This study has permitted to detect the key parameters to design devices for heat recovery and heat
661 dissipation that exploit the convective heat transport in fractured media.

662 Heat storage and transfer in fractured geological systems is affected by the spatial layout of the
663 discontinuities.

664 Specifically, the rock – fracture size ratio which determines the matrix block size is a crucial
665 element in determining matrix diffusion on fracture – matrix surface.

666 The estimation of the average effective thermal conductivity coefficient shows that it is not efficient
667 to store thermal energy in rocks with high fracture density because the fractures are surrounded by a
668 matrix with more limited capacity for diffusion giving rise to an increase in solid thermal resistance.

669 In fact, if the fractures in the reservoir have a high density and are well connected, such that the
670 matrix blocks are small, the optimal conditions for thermal exchange are not reached as the matrix
671 blocks have a limited capability to store heat.

672 On the other hand, isolated permeable fractures will tend to lead to the more distribution of heat
 673 throughout the matrix.

674 Therefore, subsurface reservoir formations with large porous matrix blocks will be the optimal
 675 geological formations to be exploited for geothermal power development.

676 The study could help to improve the efficiency and optimization of industrial and environmental
 677 systems, and may provide a better understanding of geological processes involving transient heat
 678 transfer in the subsurface.

679 Future developments of the current study will be carrying out investigations and experiments aimed
 680 at further deepening the quantitative understanding of how fracture arrangement and matrix
 681 interactions affect the efficiency of storing and dissipation thermal energy in aquifers. This could be
 682 achieved by means of using different formations with different fracture density and matrix porosity.

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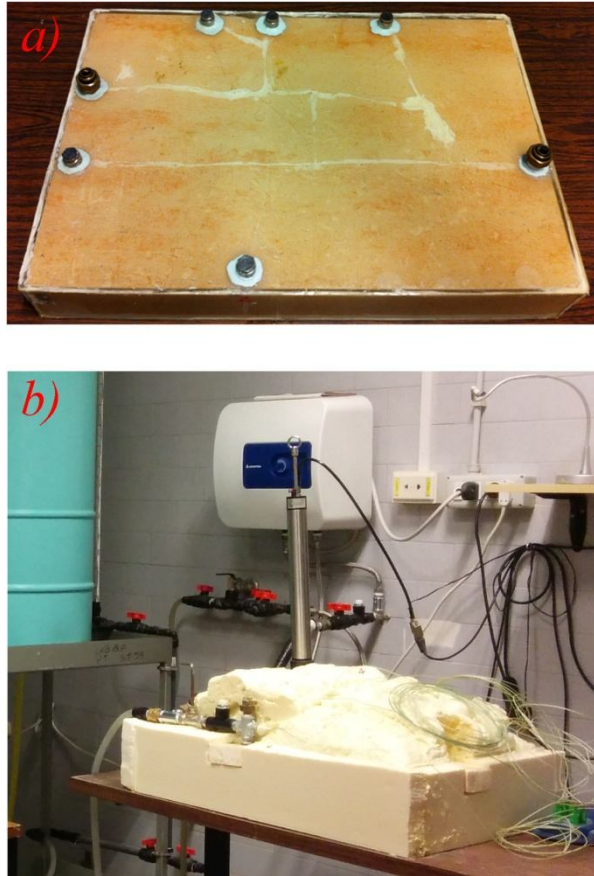
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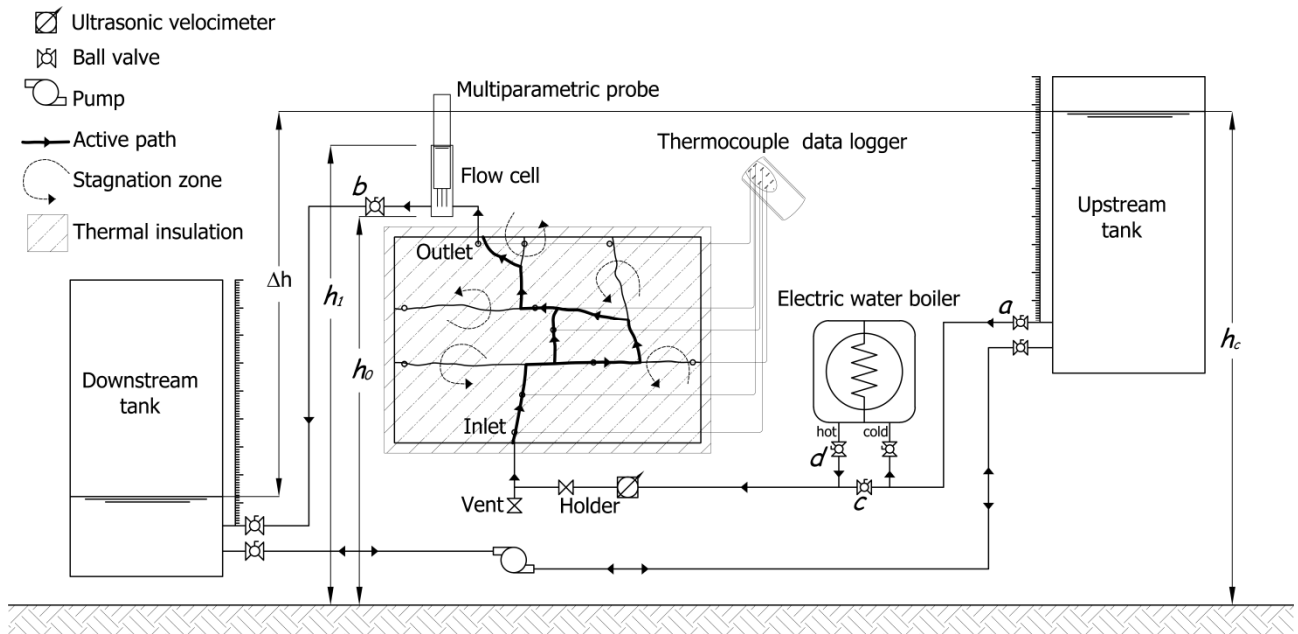
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862 **Figure 1. a) fractured block sealed with epoxy resin. b) thermal insulated fracture block connected to the hydraulic circuit.**



863

864 **Figure 2. Schematic diagram of the experimental setup.**

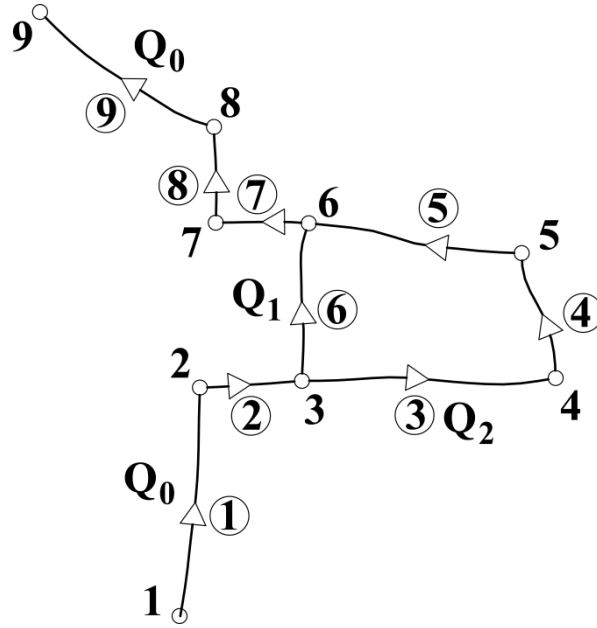


Figure 3. Two dimensional pipe network conceptualization of the fracture network of the fractured rock block in Figure1. Q_0 is the injection flow rate, Q_1 and Q_2 are the flow rates that flowing in the parallel branch 6 and 3-4-5 respectively.

Injection flow rate $Q_0 \text{ (m}^3\text{s}^{-1}) \times 10^{-6}$	Convective velocity $u_f \text{ (ms}^{-1}) \times 10^{-3}$	Dispersion $D_f \text{ (ms}^{-2}) \times 10^{-3}$	Exchange rate coefficient $\alpha \text{ (s}^{-1}) \times 10^{-6}$	RMSE	r^2
1.319	4.38 ÷ 4.47	0.68 ÷ 0.70	4.80 ÷ 5.06	0.0053	0.9863
1.843	6.21 ÷ 6.28	0.57 ÷ 0.58	2.86 ÷ 3.01	0.0026	0.9954
2.234	6.54 ÷ 6.59	0.66 ÷ 0.67	3.09 ÷ 3.13	0.0017	0.9976
2.402	7.64 ÷ 7.68	0.67 ÷ 0.67	2.65 ÷ 2.68	0.0015	0.9983
2.598	9.88 ÷ 9.94	0.80 ÷ 0.82	2.76 ÷ 2.84	0.0015	0.9987
2.731	8.27 ÷ 8.35	0.75 ÷ 0.76	2.80 ÷ 2.91	0.0018	0.9977
2.766	8.35 ÷ 8.41	0.84 ÷ 0.85	2.65 ÷ 2.69	0.0021	0.9978
3.076	11.33 ÷ 11.43	0.89 ÷ 0.91	2.53 ÷ 2.59	0.0029	0.9982
3.084	10.86 ÷ 10.95	0.87 ÷ 0.89	3.11 ÷ 3.18	0.0022	0.9982
4.074	15.88 ÷ 16.02	1.19 ÷ 1.21	2.89 ÷ 2.94	0.0048	0.9979
4.087	15.07 ÷ 15.20	1.11 ÷ 1.13	3.75 ÷ 3.83	0.0045	0.9976
4.132	14.71 ÷ 14.82	1.08 ÷ 1.09	2.93 ÷ 2.98	0.0028	0.9985
4.354	15.63 ÷ 15.77	1.14 ÷ 1.16	3.24 ÷ 3.30	0.0052	0.9979
4.529	17.05 ÷ 17.21	1.30 ÷ 1.32	2.88 ÷ 2.94	0.0055	0.9978
5.852	19.26 ÷ 19.38	1.44 ÷ 1.46	4.21 ÷ 4.25	0.0042	0.9983
5.895	19.38 ÷ 19.54	1.37 ÷ 1.39	3.77 ÷ 3.82	0.0058	0.9981
6.168	18.98 ÷ 19.17	1.36 ÷ 1.39	2.87 ÷ 2.92	0.0091	0.9973
7.076	20.64 ÷ 20.86	1.36 ÷ 1.39	3.33 ÷ 3.39	0.0123	0.9963

7.620	20.47 ÷ 20.75	1.52 ÷ 1.55	2.33 ÷ 2.39	0.0180	0.9951
7.983	21.33 ÷ 21.58	1.61 ÷ 1.64	2.92 ÷ 2.98	0.0137	0.9965
8.345	21.71 ÷ 21.97	1.65 ÷ 1.68	2.81 ÷ 2.86	0.0136	0.9964

872 **Table 1. Estimated values of parameters, RMSE, and determination coefficient r^2 for ENM with Tang's solution at different**
873 **injection flow rates for mass transport.**

874

Injection flow rate Q_0 ($m^3 s^{-1}$) $\times 10^{-6}$	Convective velocity u_f (ms^{-1}) $\times 10^{-3}$	Dispersion D_f (ms^{-2}) $\times 10^{-3}$	Exchange rate coefficient α (s^{-1}) $\times 10^{-3}$	RMSE	r^2
1.835	2.20 ÷ 2.91	1.91 ÷ 1.95	6.27 ÷ 6.59	0.0065	0.9997
2.325	1.74 ÷ 2.73	1.82 ÷ 1.91	5.39 ÷ 9.26	0.0098	0.9992
2.462	0.35 ÷ 0.52	2.42 ÷ 2.57	2.25 ÷ 2.33	0.0138	0.9984
2.605	0.44 ÷ 0.54	2.33 ÷ 2.40	0.74 ÷ 0.77	0.0073	0.9995
2.680	2.18 ÷ 2.95	1.77 ÷ 1.83	5.68 ÷ 8.31	0.0030	0.9998
2.800	0.36 ÷ 0.79	2.53 ÷ 2.68	3.54 ÷ 3.72	0.0213	0.9982
2.847	1.73 ÷ 3.16	1.98 ÷ 2.06	4.95 ÷ 13.45	0.0283	0.9978
3.003	2.34 ÷ 2.87	2.24 ÷ 2.32	5.33 ÷ 6.55	0.0033	0.9998
3.998	2.56 ÷ 2.75	6.63 ÷ 6.80	2.05 ÷ 2.11	0.0150	0.9993
4.030	2.60 ÷ 2.83	7.18 ÷ 7.36	1.42 ÷ 1.52	0.0147	0.9993
4.217	3.85 ÷ 4.56	8.92 ÷ 9.29	4.86 ÷ 5.77	0.0228	0.9945
4.225	2.43 ÷ 2.64	7.53 ÷ 7.84	1.64 ÷ 1.80	0.0251	0.9987
4.471	2.30 ÷ 3.13	9.18 ÷ 9.50	1.06 ÷ 1.33	0.1115	0.9957
5.837	3.51 ÷ 4.13	4.95 ÷ 5.36	0.61 ÷ 0.79	0.2360	0.9872
5.880	2.71 ÷ 3.10	4.23 ÷ 4.60	0.04 ÷ 0.05	0.1997	0.9926
6.445	4.71 ÷ 5.12	6.18 ÷ 6.81	1.49 ÷ 1.54	0.2156	0.9863
7.056	8.15 ÷ 8.46	10.05 ÷ 10.74	5.63 ÷ 6.00	0.0694	0.9951
7.959	9.64 ÷ 10.11	18.40 ÷ 19.47	10.92 ÷ 11.55	0.0662	0.9971
8.971	13.40 ÷ 13.79	24.57 ÷ 25.82	15.35 ÷ 15.85	0.0303	0.9985
12.364	11.01 ÷ 11.67	21.97 ÷ 22.63	5.23 ÷ 5.25	0.0631	0.9939
12.595	13.71 ÷ 14.26	26.65 ÷ 27.61	9.26 ÷ 9.41	0.0426	0.9955

875 **Table 2. Estimated values of parameters, RMSE, and determination coefficient r^2 for ENM with Tang's solution at different**
876 **injection flow rates for heat transport.**

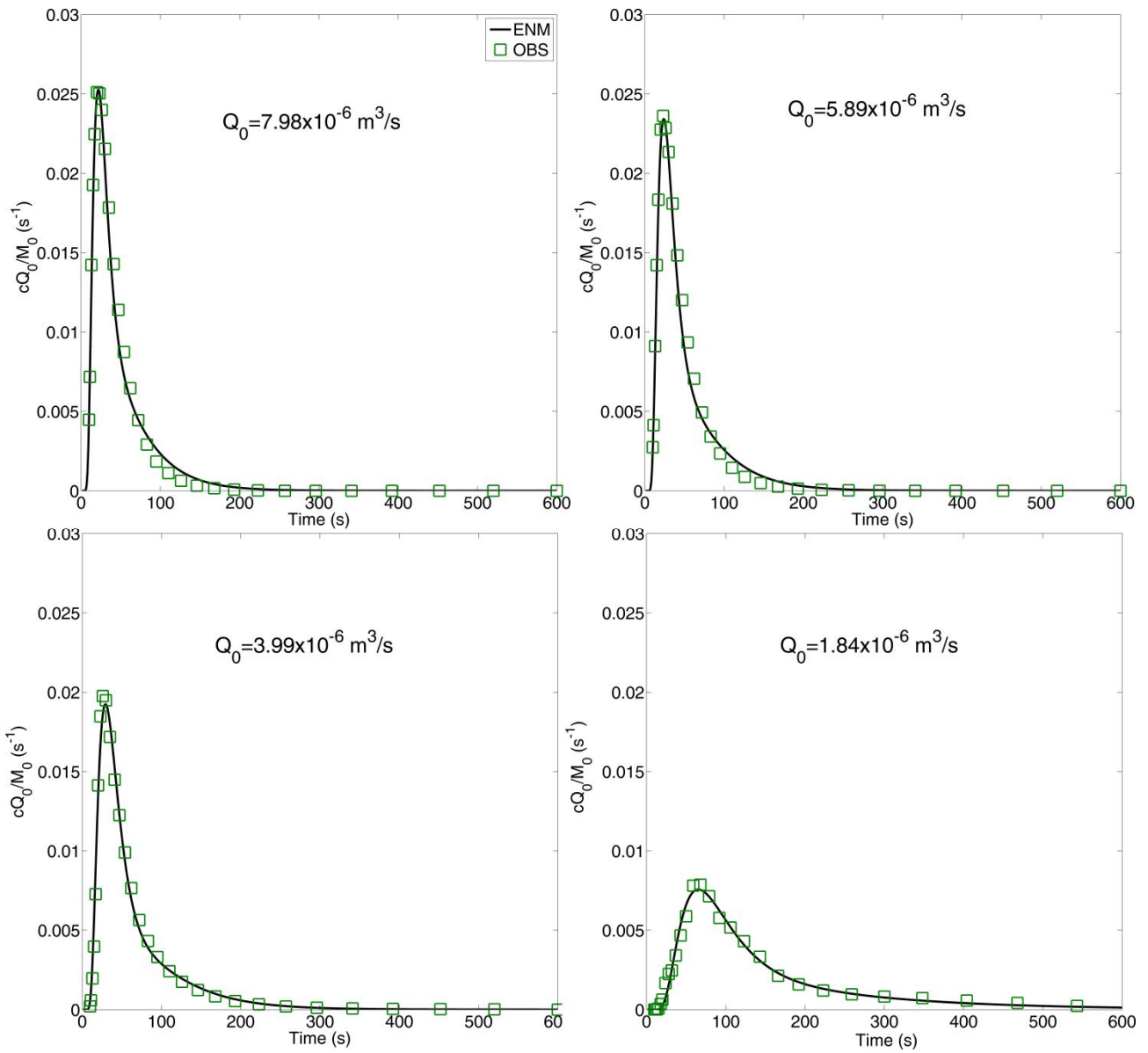


Figure 4. Fitting of BTCs at different injection flow rates using ENM with Tang's solution for mass transport. Green square curve is the observed specific mass flux at the outlet port, continuous black line is the simulated specific mass flux.

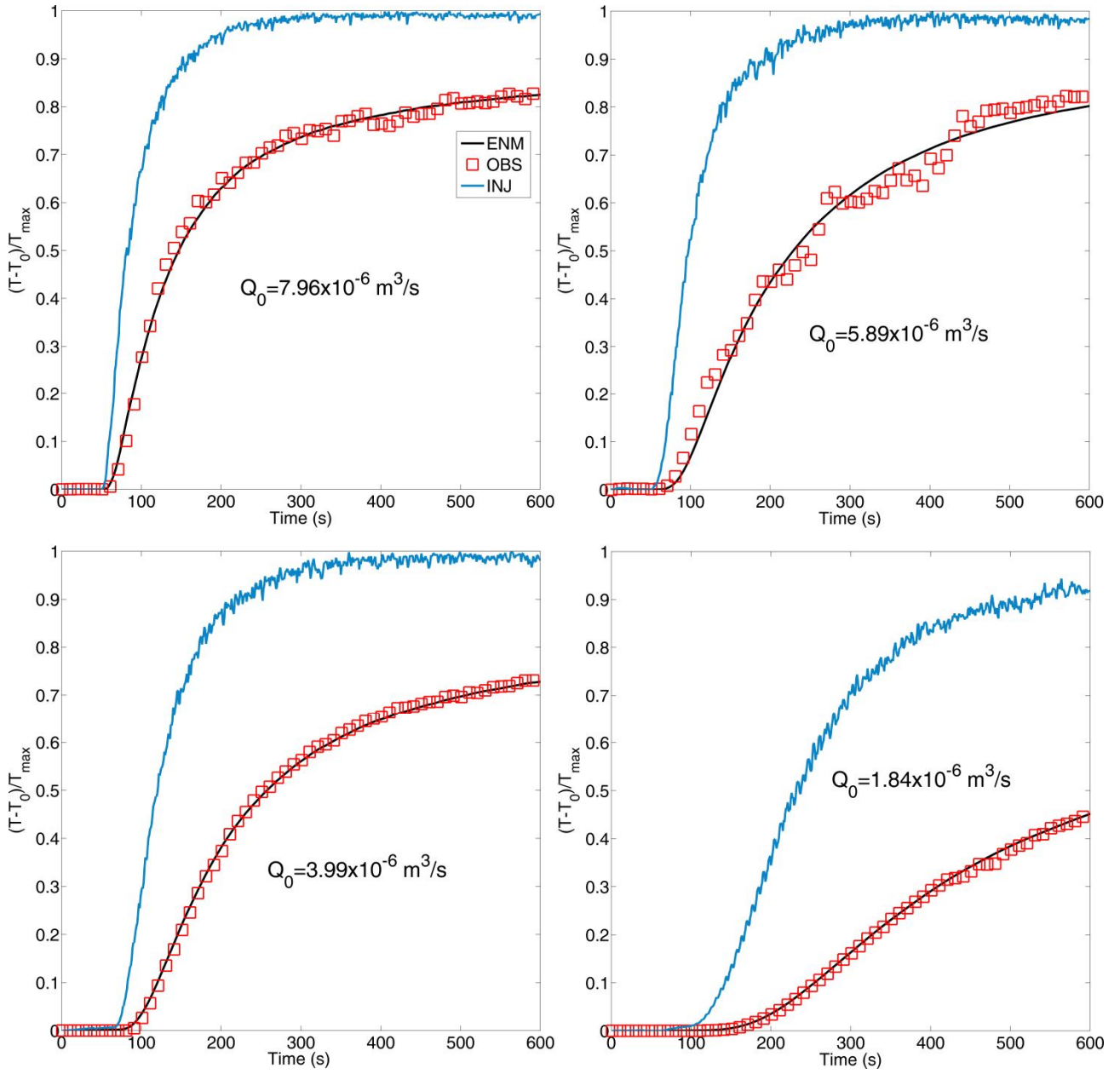
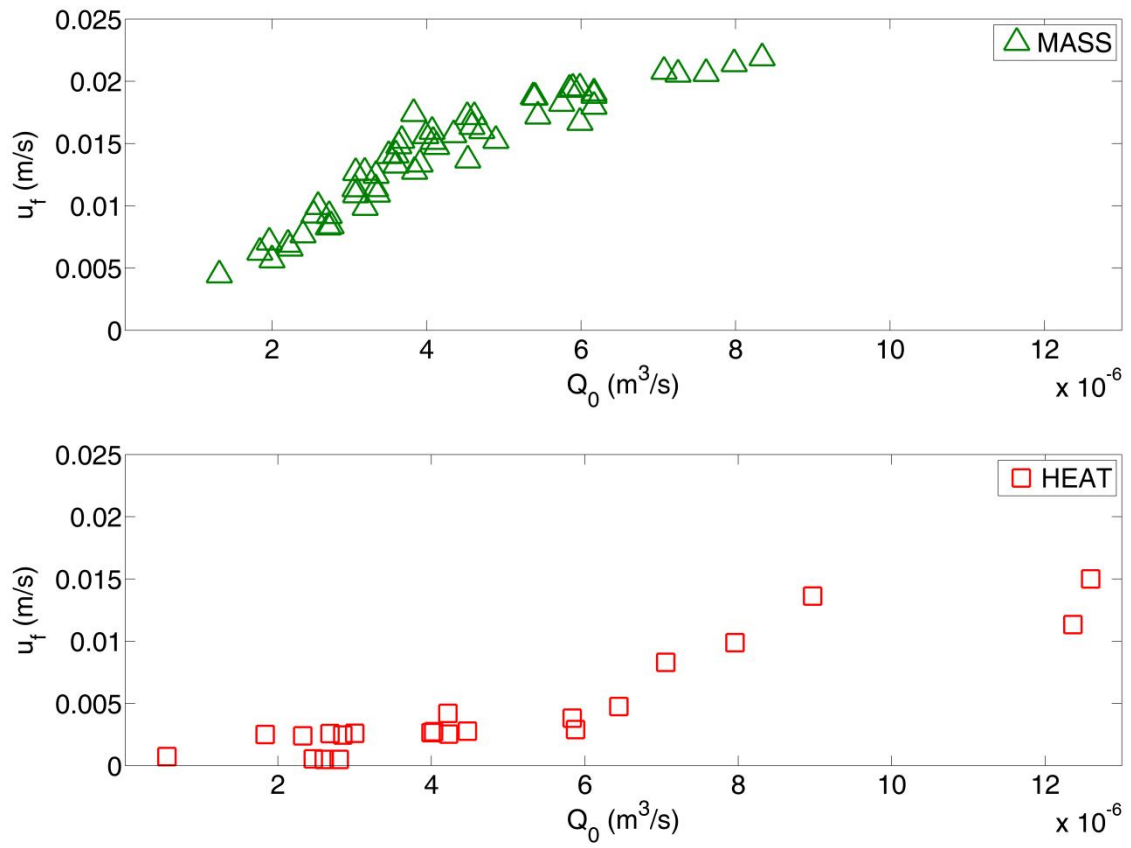


Figure 5. Fitting of BTCs at different injection flow rates using ENM with Tang's solution for heat transport. The blue curve is the temperature observed at the inlet port used as the temperature injection function, the red square curve is the observed temperature at the outlet port, the black continuous curve is the simulated temperature at the outlet port.

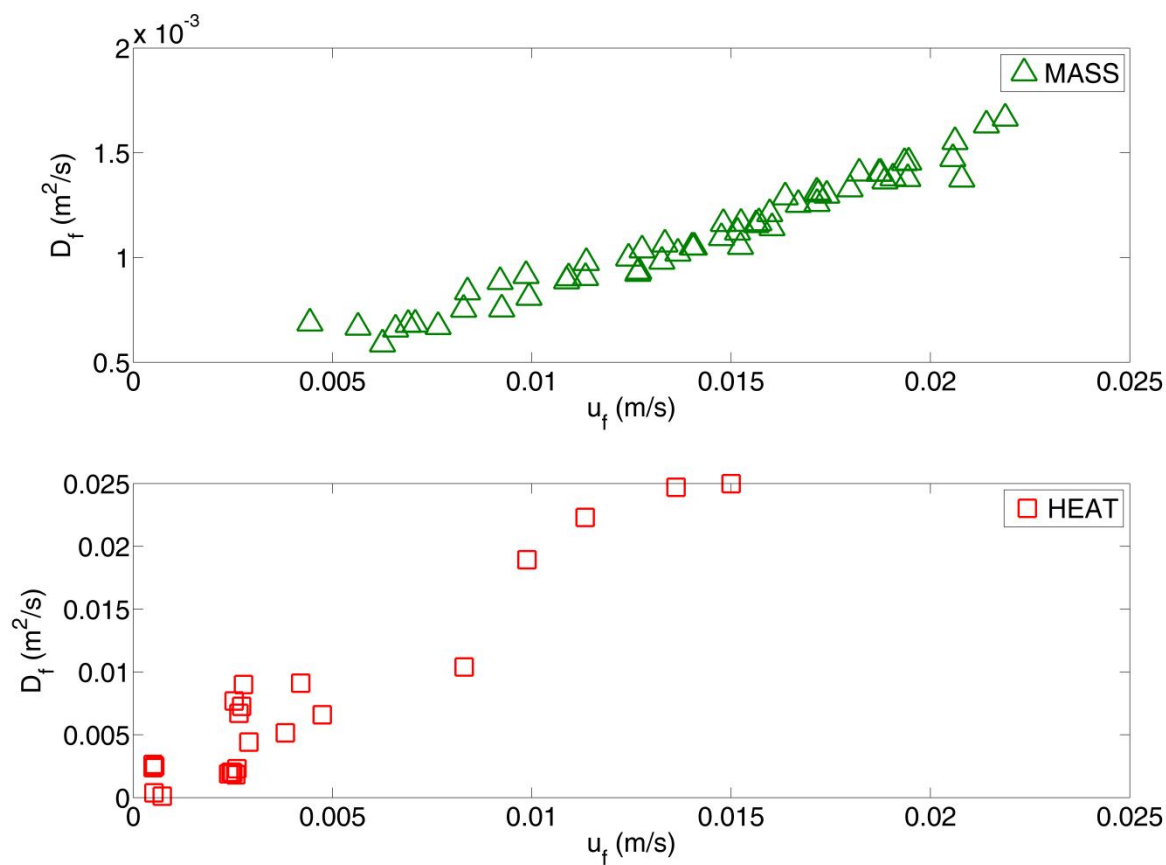


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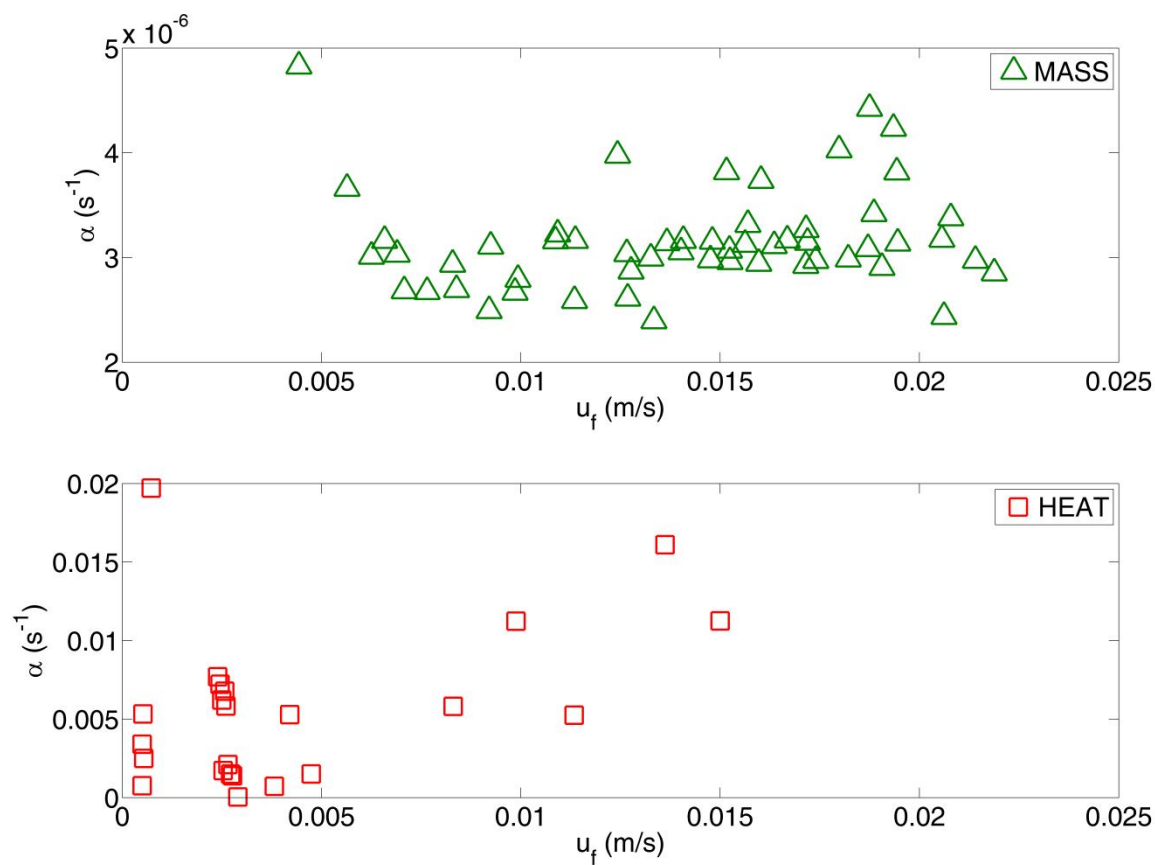
Figure 6. Velocity u_f ($\text{m}\cdot\text{s}^{-1}$) as function of the injection flow rate Q_0 (m^3s^{-1}) for ENM with Tang's solution for both mass and heat transport.



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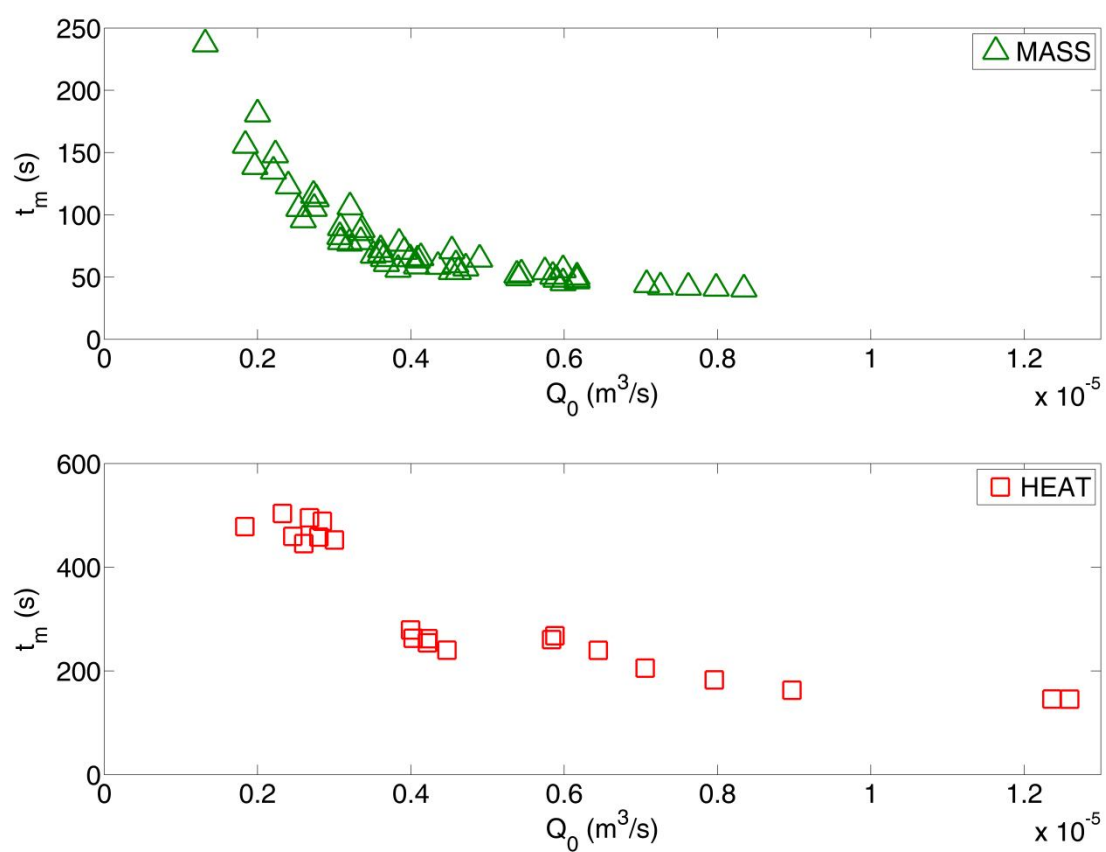
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Figure 7. Dispersion D_f ($\text{m}\cdot\text{s}^{-2}$) as function of velocity u_f ($\text{m}\cdot\text{s}^{-1}$) for ENM with Tang's solution for both mass and heat transport.



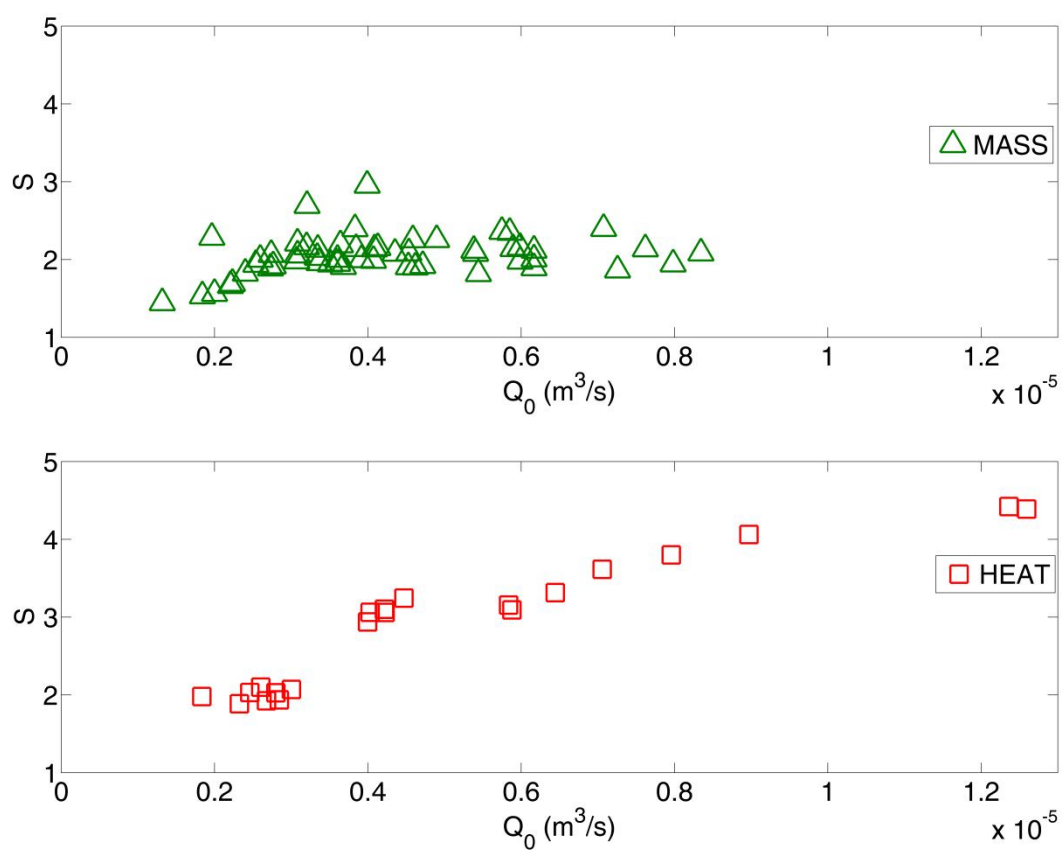
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891 **Figure 8. Transfer coefficient α (s⁻¹) as function of velocity u_f (m·s⁻¹) for both mass and heat transport.**



892

893 **Figure 9. Mean travel time t_m (s) as function of injection flow rate for both mass and heat transport.**



894

895 **Figure 10. Skewness as function of injection flow rate for both mass and heat transport.**

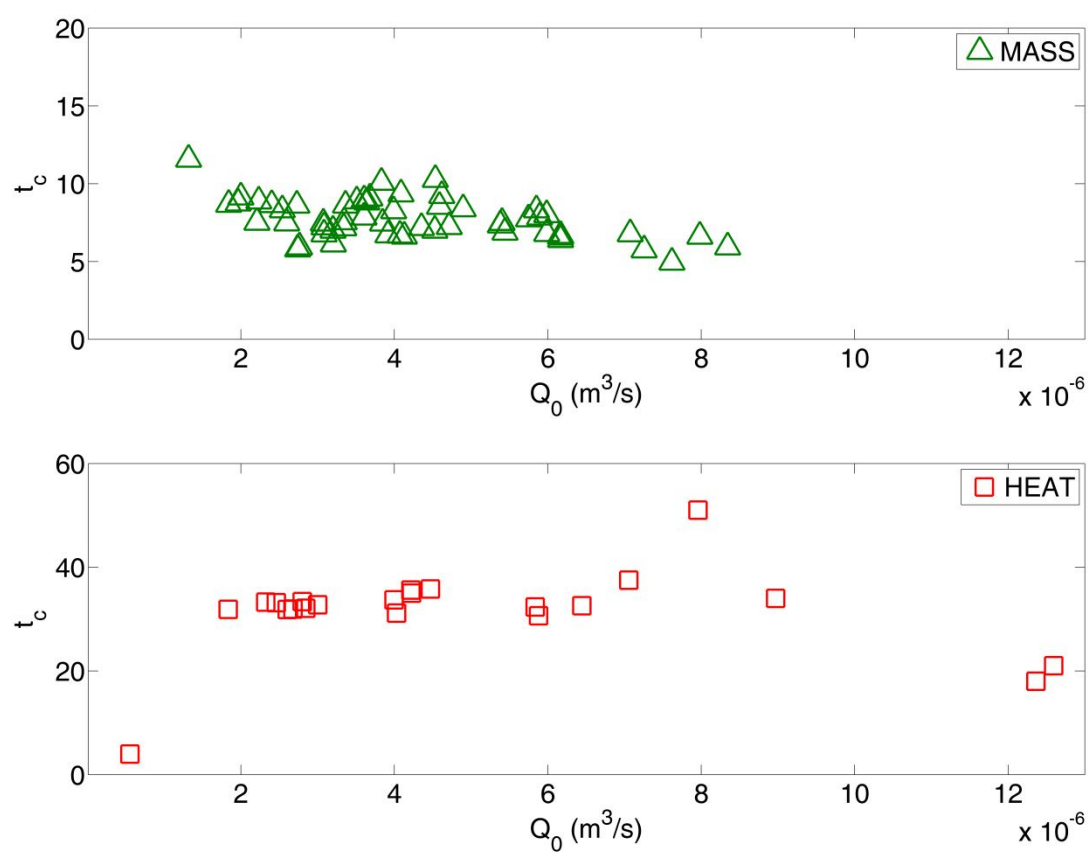
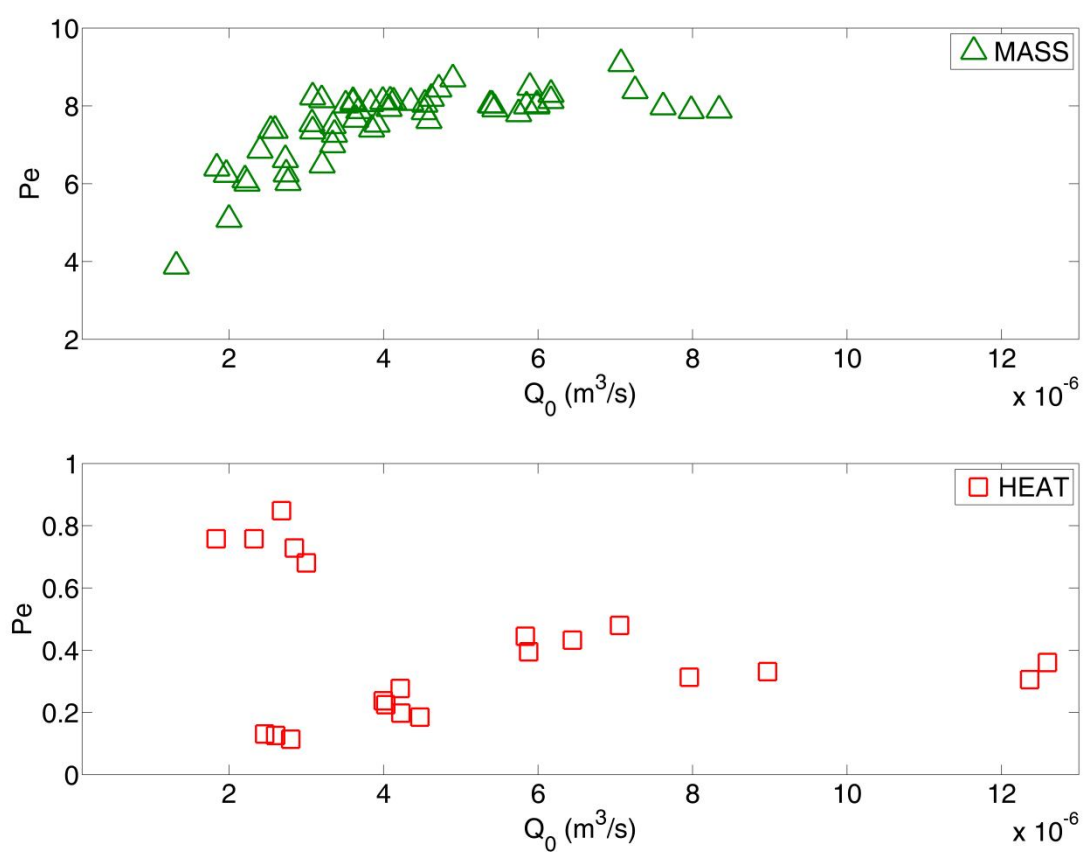
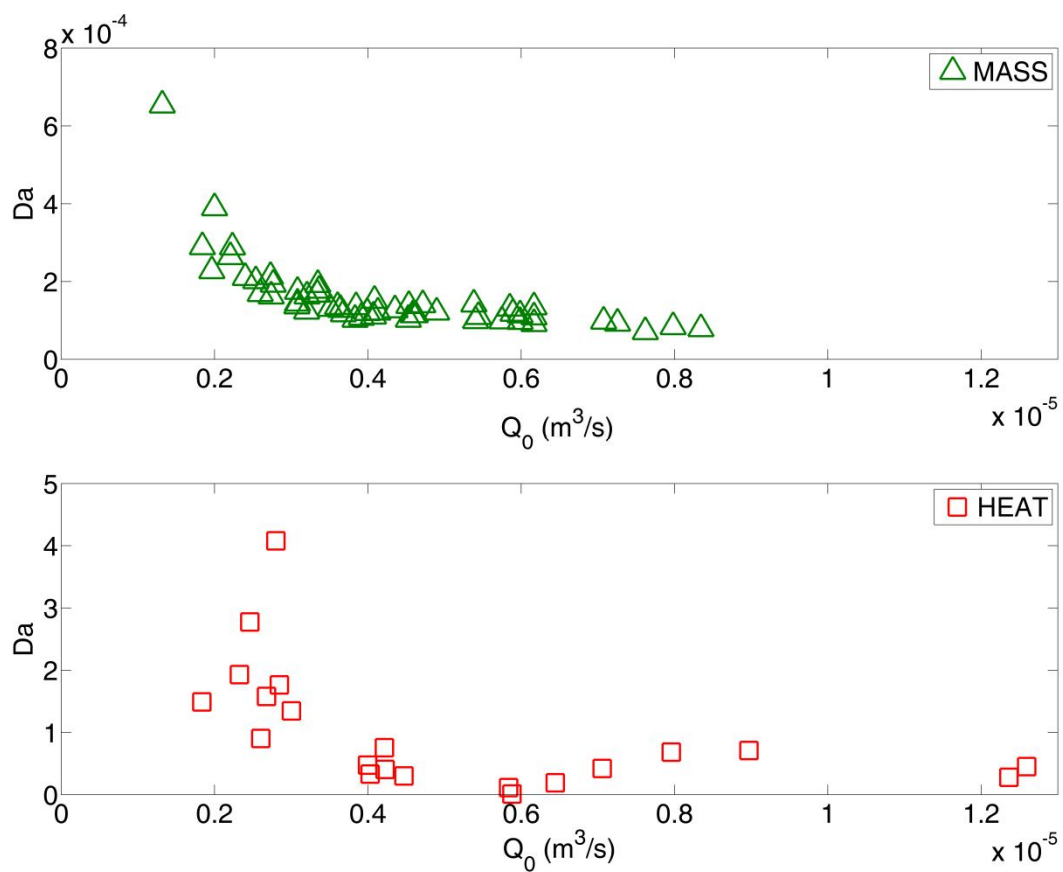


Figure 11. Tailing character t_c as function of injection flow rate for both mass and heat transport.



899

900 **Figure 12. Peclet number as function of injection flow rate Q_0 (m³s⁻¹) for both mass and heat transport.**



901

902 **Figure 13. Da number as function of injection flow rate Q_0 (m^3s^{-1}) for both mass and heat transport.**

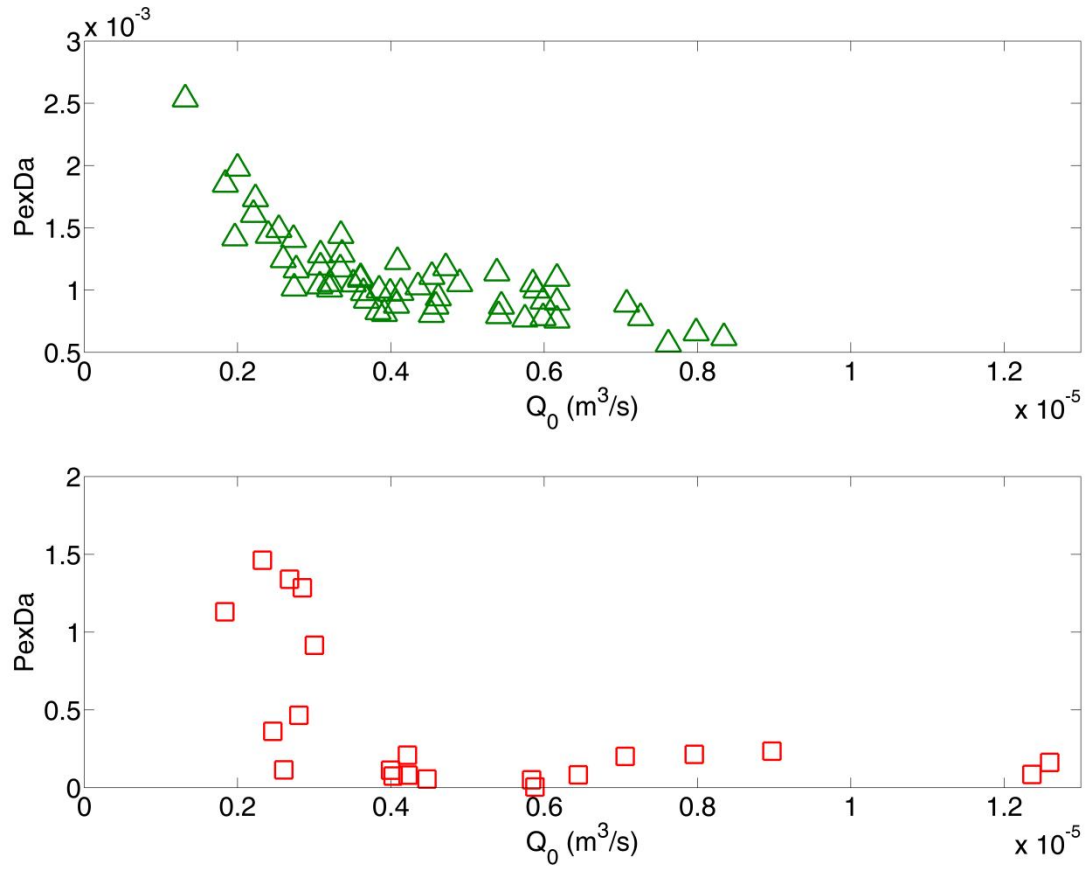


Figure 14. $\text{Pe} \times \text{Da}$ number as function of injection flow rate Q_0 ($\text{m}^3 \text{s}^{-1}$) for both mass and heat transport.

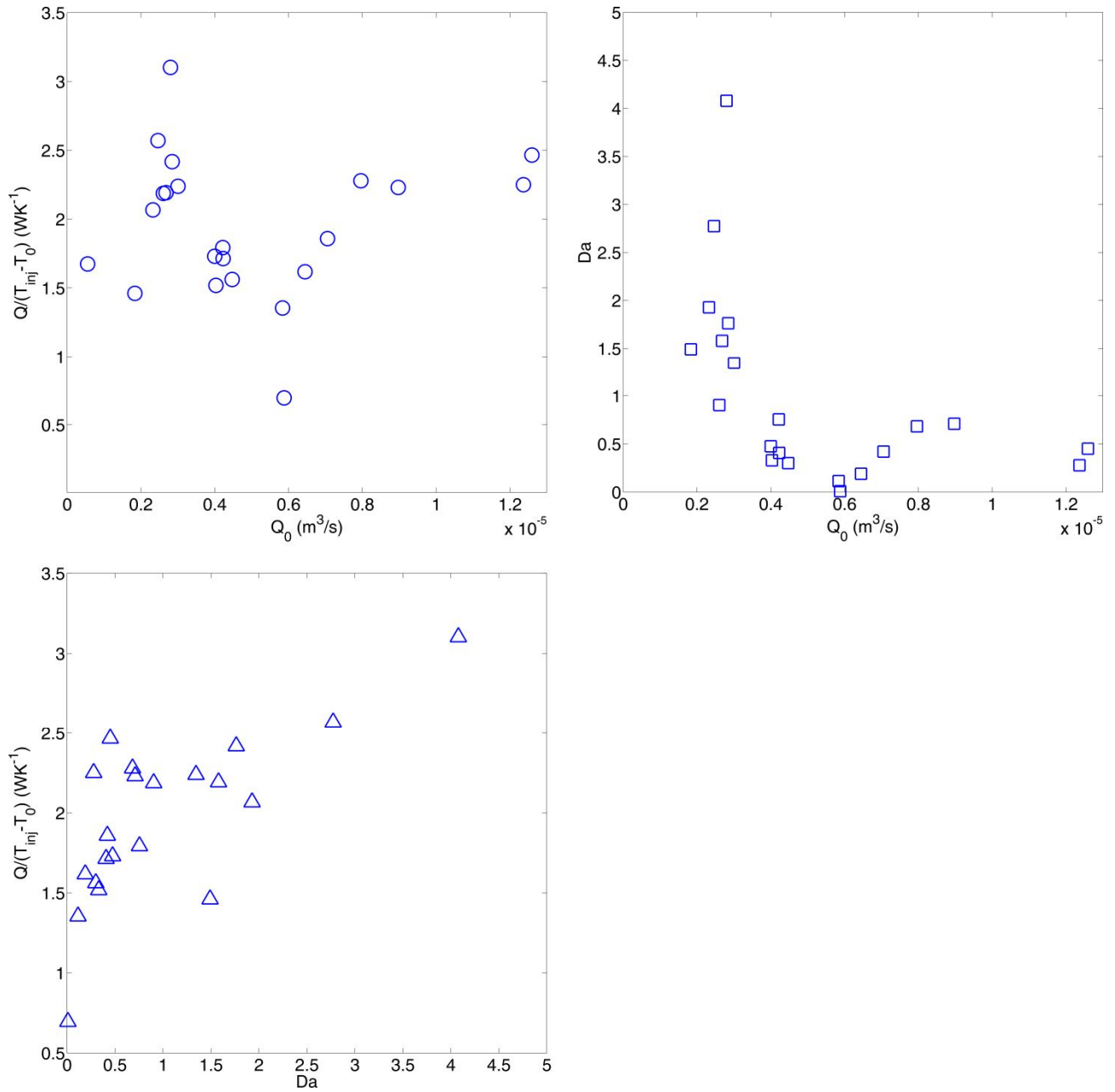


Figure 15. Heat power exchanged per difference temperature unit $\dot{Q}/(T_{inj}-T_0)$ as function of injection flow rate Q_0 (m³s⁻¹) (a), Damköhler number Da as function of injection flow rate (b), power exchanged per difference temperature unit as function of Damköhler number (c).

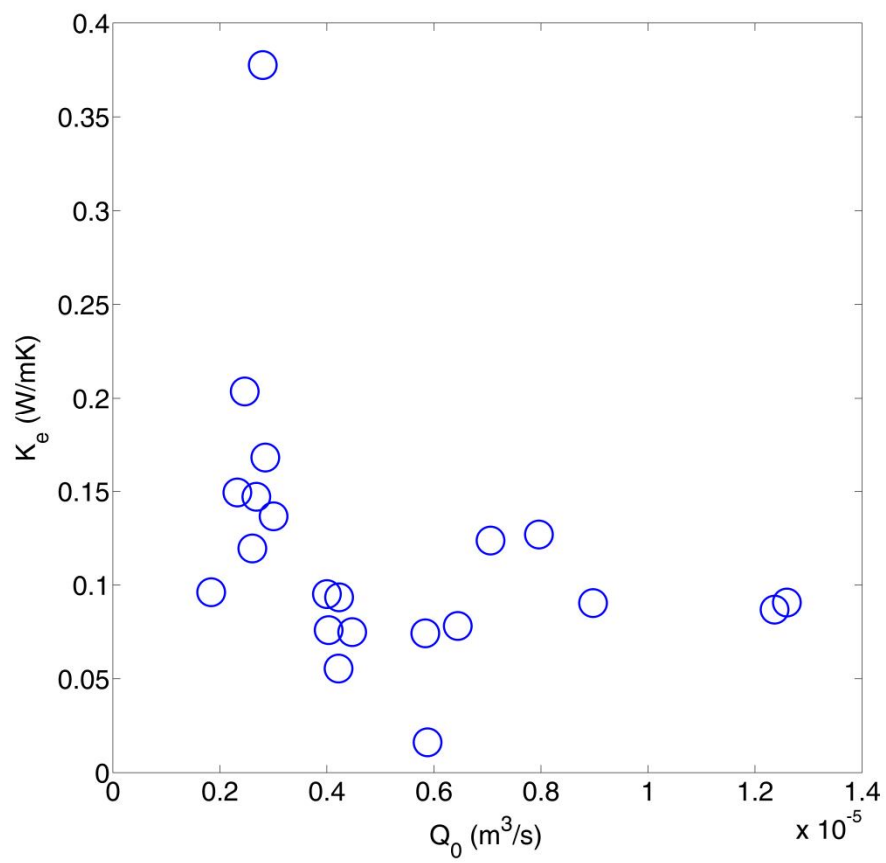


Figure 16. Effective thermal conductivity k_e ($Wm^{-1}K^{-1}$) as function of injection flow rate Q_0 (m^3s^{-1}).