

**The double layers in the separatrix region during magnetic reconnection**

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1   **Abstract** We studied the evolution of double layer which appears during the magnetic  
2   reconnection through two dimensional particle-in-cell simulation. The simulation  
3   results show that the double layer in the wake of electron hole is formed in the  
4   separatrix after magnetic reconnection. At first, a localized electron beam forms. Then  
5   the speed of electron beam increases as the magnetic reconnection goes on. When the  
6   speed is large enough, the electron beam excites the ion-acoustic instabilities, which  
7   results in the formation of double layers. The estimated spatial size of the double layer  
8   found in our work is about ten Debye lengths, and these structures propagate along  
9   the magnetic field with a velocity comparable to the ion acoustic speed, which  
10  accords with the observation results.

11   Keywords: the double layer, magnetic reconnection, particle-in-cell simulation

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## 1    **1. Introduction**

2        Magnetic reconnection is a very important progress in the space plasma, which  
3    change the magnetic field energy into kinetic energy of electrons and ions. (Pritchett,  
4    2001; Lu et al. 2010) In the previous works, more attentions are paid on the whistler  
5    waves (Fujimoto and Sydora, 2008; Deng and Matsumoto, 2001; Guo, 2011; Xiao et  
6    al. 2007,2008,2010) and electron acceleration. (Fu et al. 2006; Huang et al. 2010;  
7    Pritchett, 2006) Recently, the electrostatic waves have been found in the simulation  
8    and observation. Through the simulation, Drake et al. (2003) reported that the  
9    electrostatic waves and electron holes(EHs) are produced by the Buneman instability.  
10   In their simulation, the initial electron drift speed is above the threshold to trigger the  
11   Buneman instability except for a strong guide field. However, Fujimoto and Machida  
12   (2006) suggested that the electrostatic waves are excited by the electron two-stream  
13   instability which has a relationship with magnetic reconnection. Particularly, no guide  
14   field is used in their initial condition. The observation (Li et al. 2009) proved that the  
15   guide field has no direct effect on the generation of the electrostatic wave in or around  
16   the reconnection diffusion region. These reported electrostatic waves appear with  
17   bipolar electric field and electron holes, while the signature of the double layers (DLs)  
18   is a unipolar electric field. The electrons and ions will be accelerated, decelerated, or  
19   reflected by the electric field when they enter the double layer. The current-driven  
20   double layers have been carefully studied by using a series of one-dimensional Vlasov  
21   simulations.(Singh, 1980,1982, 2000) It is found that electron holes are a common  
22   feature of a strong double layer. The evolution of the electron beam accelerated by a  
23   double layer would contribute to continuously creating moving electron holes.  
24   Besides that, the double layer accelerate the ion beam to generate fluctuations above  
25   the ion cyclotron frequency in the 2.5dimensional particle-in-cell simulations. (Singh  
26   and Khazanov, 2003)

27        Electron holes are frequently observed by the spacecraft measurement during  
28   reconnection. Double layers are frequently observed in the auroral ionosphere.  
29   (Boström, 1992; Ergun et al., 2001) Only recently, Ergun et al. (2009) reported the  
30   double layers in the plasma sheet in the magnetotail. But, they could not confirm the  
31   relation between the double layers and reconnection in their work. Wang et al. (Wang  
32   et al., 2014) presented the first evidence of double layers during magnetic  
33   reconnection, and found that the double layers are moving away from X line at a  
34   velocity of about ion acoustic speed along the separatrix region. On the contrary, a

1 series of electron holes moving toward the  $x$  line are observed in the wake of the  
2 double layer. In addition, the multiple DLs are also observed, which could be created  
3 in the simulation.(Singh et al.,2011)

4 The electrostatic waves have a closely relationship with electron beams. Previous  
5 simulation results by Hosino et al. (2001) show that electron beams form mainly close  
6 to the separatrix. Using three-dimensional simulation in the presence of a guide field,  
7 Prichett and Coroniti (2004) found the enhanced parallel electric field and electron  
8 velocity are confined to one pair of separatrix. In this case strong DLs can be  
9 generated at the reconnection site. The purpose of our study is to investigate the  
10 generation mechanism of the double layer during the magnetic reconnection without a  
11 guide field. Our results suggest that both the double layer and electron hole are found  
12 in our simulation. These polarized structure should be excited by the ion-acoustic  
13 instabilities.

## 14 2. Simulation Model

15 The initial magnetic field distribution is set to be  $B_x(y) = B_0 \tanh[(y - L_y/2)/\delta_0]$ ,  
16 where  $\delta_0$  is the half width of the initial current sheet. The particle densities read  $n(y)$   
17  $= n_p \text{sech}^2[(y - L_y/2)/\delta_0] + n_b$ , where  $n_p$  and  $n_b$  represent the current sheet and background  
18 densities.  $\delta_0$  is equal to  $0.5\lambda_i$ , where  $\lambda_i$  is the ion inertial length given by  $n_p$ . All of the  
19 particles have the initial Maxwellian velocity distributions. In the present simulation,  
20 the simulation size is  $L_x \times L_y = 25.6\lambda_i \times 12.8\lambda_i$ . The other parameters are  $T_i/T_e = 5$ ,  $n_b =$   
21  $0.1n_p$ ,  $m_i/m_e = 256$ ,  $c/V_A = 30$ , where  $V_A$  is the Alfvén speed based on  $B_0$  and  $n_p$ . Then  
22 the ratio of ion gyro-frequency to plasma frequency is  $\omega_{pi}/\Omega_i = c/V_A = 30$ . The spatial  
23 resolution is  $\Delta x = \Delta y = 0.05\lambda_i$ . The time step is  $\Delta t\Omega_i = 0.001$ , where  $\Omega_i$  is the proton  
24 cyclotron frequency. Along the  $x$  axis, the periodic boundary conditions are used, and  
25 the ideal conducting boundary conditions are used in the  $y$  direction. The particles will  
26 be reflected when they reach the boundary in the  $y$  direction. The magnetic and  
27 electric fields are calculated with a full explicit algorithm. About  $6 \times 10^6$  particles per  
28 species are employed in the simulation. A small initial magnetic perturbation is  
29 superposed in the form which is the same as the references (Lu, et al. 2013; Guo,  
30 2014).

## 31 3. Simulation Results

32 Figure 1a shows the electric field parallel to the local magnetic field  $E_{||}$  and  
33 magnetic field lines at  $t\Omega_i = 15.3$ . Figure 1b shows the magnification of  $E_{||}$  in  
34 left-hand plane. We plot figure 1b as function of the electron Debye length instead of

the ion inertial length. At this time, the electron thermal speed  $v_{the} \sim v_{th0} = (2T_e/m_e)^{1/2} \sim 6.5V_A$ . It is obvious that the electric fields with polarized structures are mainly located in the separatrix region. These structures are almost along the magnetic field lines. As the magnetic reconnection proceeds, the polarized electric fields will also appear in the diffusion region, which have been discussed in our previous work. (Guo, 2014)

Shown in figure 2 are the  $v_{||} - x$  phase space distributions of electron (a) and ion (b), and the electric field  $E_{||}$  at  $y/\lambda_i=6.75$ (c). Figure 1(a) and (c) show clearly that there is an electron phase-space hole at  $x/\lambda_i \sim 4.1$ . Besides that, a double layer with a width about  $10\lambda_{De}$  lies at  $x/\lambda_i \sim 3.5$ , which is in the wake of a electron hole,  $\lambda_{De}=v_{the}/\omega_{pe}$  is the initial electron Debye length. Figure 2(d) is the parallel velocity distribution of electron  $f(v_{||})$  at about  $x/\lambda_i=4.1$  and  $y/\lambda_i=6.75$ , which is corresponding to the electron hole shown in figure 2(a). This distribution appears an electron beam with  $v_{||}/V_A \sim -12.0$  and a broad peak centered around  $v_{||}/V_A \sim 10.0$ (flat-top distribution). On the other hand, the low velocity portion of the distribution is also dominated by an plateau formation. Figure 2(e) is the density distribution of electron along  $y$  axis at  $y/\lambda_i=3.5$  where the double layer appear. Figure 2 (f) is the density distribution of electron along  $x$  axis at  $y/\lambda_i=6.75$ . Couple the (e) and (f), it is found that the density of electron where the double layer appears is lower than the surrounding along both  $x$  and  $y$  axis. Based on the observations, (Wang et al., 2013; 2014) the DL and electron hole are observed together. Then, our simulation results are basically consistent with the observations at least in the structure.

The magnetic field line passes through  $y/\lambda_i=6.75$ , where the magnetic field is nearly parallel to the  $x$  axis in the region  $x/\lambda_i < 7$ . The plateau function means that the Buneman or ion-acoustic modes probably appear. Figure 3 is the wave spectrum of parallel electric field. The sampling region is  $0 < x/\lambda_i < 6.4$  and the time interval is  $15.0 < t\Omega_i < 15.5$ . It is found that the normalized wave number associated with the highest wave energy density is  $k\lambda_{De} \sim \pm 0.8$ . These forward and backward modes are corresponding to the distribution shown in figure 2(d). During this period, the frequency of the dominant mode is far below the ion plasma frequency. All of the above suggests that the DL located in the separatrix region shown in figure 2(c) should be produced by the ion-acoustic instabilities.

Numerical simulations and observations have been performed during the past decade showing that DLs are highly variable structures moving with time. (Singh et

al., 2005; Wang et al., 2014) Figure 4(a) is the time evolution of the polarized electric field shown in figure 1(b) at  $y/\lambda_i=6.75$ . The double layer in our simulation seems to only propagate outward along the magnetic field for a short distance. The propagation velocity can be estimated to be  $0.2V_A$ . While the double layer found in the separatrix near the X line shown in figure 4(b) can propagate for a long time and distance. The propagation velocity can be estimated to be  $0.4V_A$ . In fact, these two velocities are of the same order of the ion acoustic speed, although the former is a little small. The observation (Wang et al., 2014) also suggests that the DL propagates away from the X line at a velocity of about ion acoustic speed. That is, the results shown in figure 4 are very consistent with those observations. However, the DL found in the separatrix at a distance of several ion inertial length away from the X line shown in figure 1(b) cannot propagate for a long distance. A reasonable explanation for the figure 4(a) is due to the periodic boundary condition.

Previous simulation results about magnetic reconnection (Hosino et al., 2001; Prichett and Coroniti, 2004) show that electron beams form mainly close to the separatrix. In this condition, strong DLs can be generated at the reconnection site. These simulation results have been confirmed by the Cluster observations published by Vaivads et al. (2004). Figure 5 shows the time evolution of the electron flow velocity parallel to the magnetic field at  $y/\lambda_i=6.75$ . The localized electron beam with negative drift velocity propagates along the magnetic field toward left. At time  $t\Omega_i \sim 12$ , this electron beam lies at  $x/\lambda_i \sim 4.8$ , while the propagation stops at  $x/\lambda_i \sim 4.1$  due to the periodic boundary condition at time  $t\Omega_i \sim 15.5$ . This evolution is consistent with that of parallel electric field shown in figure 4(a). Of course, the DL appears after the electron beam formed for a period of time. On the other hand, as the time goes on, the width of electron flow becomes smaller, while the beam velocity becomes larger. The figure shows that only when the velocity of electron beam reaches a certain value will excite the electrostatic waves. Compared with the figure 2, the electron beam just locates in the region where the electron hole appears. Our previous simulation results (Guo and Li, 2013) suggest that the ion-acoustic waves are always accompanied by electron beams. Considering the figure 2(d), thus it can be concluded that the localized electron beam excites the ion-acoustic instabilities, which results in the formation of DLs. However, the electron beam cannot drift for a long time due the periodic boundary, which lead the DL to cannot propagate long distance.

#### 4. Conclusion

1 In this paper, the evolutions of double layers during magnetic reconnection are  
2 studied by two-dimensional electromagnetic particle-in-cell simulation. The  
3 simulation results show that, the DLs appear in the separatrix, which are produced by  
4 the ion-acoustic instabilities. The DL found in our simulation is about ten Debye  
5 lengths and propagate out of the diffusion region with a velocity comparable to the  
6 ion acoustic speed. These results accord with the observation results. (Wang et al.,  
7 2014) The physical evolution process can be inferred from the following process. At  
8 first, the electrons are accelerated near the X line and then flow out of the diffusion  
9 region along the magnetic field. When the velocity of the electron beam is large  
10 enough, then the localized electron beam excites the ion-acoustic instabilities, which  
11 produced the DL. But the double layers at a few ion inertial length away from the X  
12 line can only propagate for a short distance, because the propagation of electron beam  
13 tends to stable due to periodic boundary condition. However, even though we get  
14 some interesting results, there are still many questions that remain to be addressed.  
15 For instance, a sufficiently long system will be used to study the propagation of DL in  
16 the future work.

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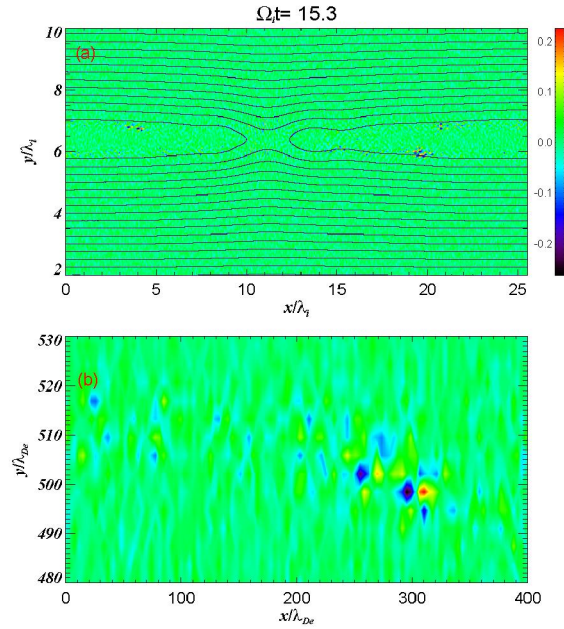


FIG. 1. The electric field parallel to the local magnetic field  $E_{\parallel}$  and magnetic field lines at  $t\Omega_i = 15.3$ (a); the magnification of the left-hand plane (b).

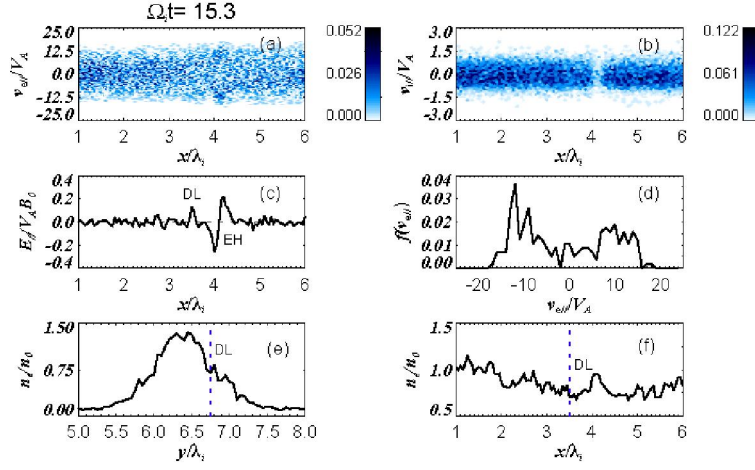


FIG. 2. The  $v_{||}$  -  $x$  phase space distributions of electron (a) and ion (b), and the electric field  $E_{||}$  at  $y/\lambda_i=6.75$ (c), the parallel velocity distribution of electron  $f(v_{e||})$  at about  $x/\lambda_i=4.1$  and  $y/\lambda_i=6.75$ (d), the density distribution of electron along  $y$  axis at  $y/\lambda_i=3.5$  where the double layer appear (e) and the density distribution of electron along  $x$  axis at  $y/\lambda_i=6.75$ (f).

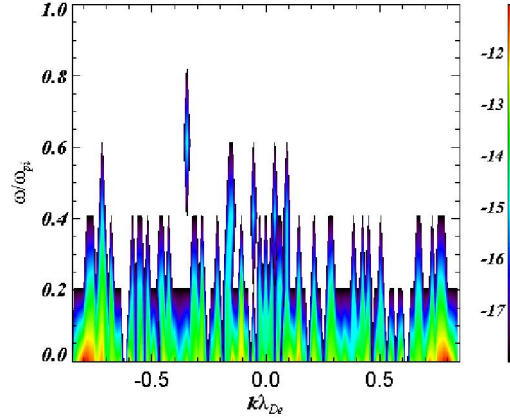


FIG. 3. The wave spectrum of parallel electric field. The sampling region is  $0 < x/\lambda_i < 6.4$  and the time interval is  $15.0 < t\Omega_i < 15.5$ .

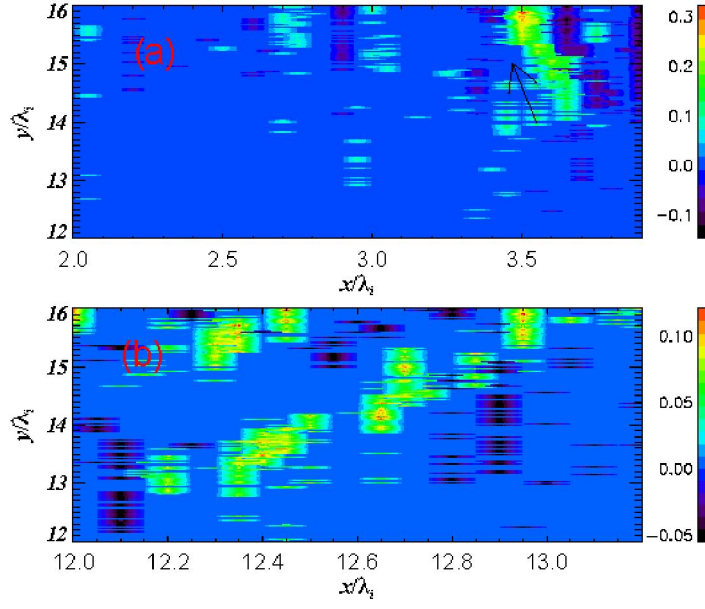


FIG. 4. The time evolution of the polarized electric field shown in figure 1(b) at  $y/\lambda_i=6.75$  (a) and the double layer found in the separatrix near the X line (b).

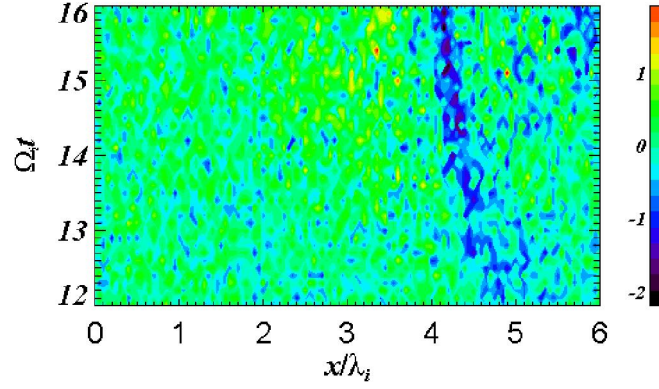


FIG. 5. The time evolution of the electron flow velocity parallel to the magnetic field at  $y/\lambda_i=6.75$ .