

This discussion paper is/has been under review for the journal Nonlinear Processes in Geophysics (NPG). Please refer to the corresponding final paper in NPG if available.

Complexity signatures in the geomagnetic H component recorded by the Tromsø magnetometer (70° N, 19° E) over the last ¼ century

C. M. Hall

Tromsø Geophysical Observatory, UiT – The Arctic University of Norway, Tromsø, Norway

Received: 24 April 2014 - Accepted: 2 May 2014 - Published: 13 May 2014

Correspondence to: C. M. Hall (chris.hall@uit.no)

Published by Copernicus Publications on behalf of the European Geosciences Union & American Geophysical Union.

ssion Pape

Discussion Pa

Discussion Paper

Discussion Pape

NPGD

1, 895-915, 2014

Complexity in the geomagnetic H component at 70° N, 19° E

C. M. Hall

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I4 ►I

Back Close

Full Screen / Esc

Printer-friendly Version



Solar disturbances, depending on the orientation of the interplanetary magnetic field, typically result in perturbations of the geomagnetic field as observed by magnetometers on the ground. Here, the geomagnetic field's horizontal component, as measured by the ground-based observatory-standard magnetometer at Tromsø (70° N, 19° E) is examined for signatures of complexity. 25 year-long 10 s resolution datasets are analysed, but for fluctuations with timescales less than 1 day. Quantile-quantile (Q-Q) plots are employed first, revealing the fluctuations are better represented by Cauchy rather than Gaussian distributions. Thereafter, both spectral density and detrended fluctuation analysis methods are used to estimate values of the generalized Hurst exponent, α . The results are then compared with independent findings. Inspection and comparison of the spectral and detrended fluctuation analyses reveals that timescales between 1 h and 1 d are characterized by fractional Brownian motion with a generalized Hurst exponent of ~ 1.4 whereas including timescales as short as 1 min suggests fractional Brownian motion with a generalized Hurst exponent of ~ 1.6. This is consistent with changes in the position of the auroral electrojet that can be considered rapid during the course of an evening, whereas from minute-to-minute the electrojet moves more persistently in geomagnetic latitude.

1 Introduction and methodology

Understanding the coupling mechanisms between various processes and phenomena in the solar-terrestrial system remains a considerable challenge. An approach that has gained popularity in recent years involves examining the noise in a signal (or time-series), i.e. the stochastic rather than the deterministic component. The underlying idea is that a signature in the noise occurring in a driving mechanism may reappear in the noise of another observable, thus linking the two. Known as complexity matching, this approach is akin to fingerprinting a crime scene. Examination of time

ussion Paper

Discussion Paper

Discussion Paper

Discussion Pape

NPGD

1, 895–915, 2014

Complexity in the geomagnetic H component at 70° N, 19° E

C. M. Hall

Title Page

Abstract Introduction

Conclusions References

Tables Figures

Close

Full Screen / Esc

Back

Printer-friendly Version



Pape

NPGD

1, 895–915, 2014

Complexity in the geomagnetic H component at 70° N. 19° E

C. M. Hall

Introductio **Abstract** Conclusions Reference

Title Page

Figures Tables

Close

Full Screen / Esc

Back

Printer-friendly Version

Interactive Discussion

series for such fingerprints was pioneered by, inter alios, Hurst (1951), Mandelbrot (1983), Grassberger and Procaccia (1983), and Koscielny-Bunde et al. (1998). Work by Eichner et al. (2003), Lennartz and Bunde (2009), and Kantelhardt et al. (2006), for example have refined the approach. Much attention has been given to oceanographic and meteorological observables including the recent study by Hall (2014), and more recently solar-related observables, e.g. Scafetta and West (2003) and Rypdal and Rypdal (2011). On the other hand, there has been relatively little focus on observables related to the terrestrial ionosphere and measured locally in order to examine the mapping of solar forcing to the Earth's surface. Hall et al. (2011) examined complexity in the ionospheric E region in the auroral zone: the altitude, strength and persistence of the E region are of particular interest for radio communications and for studying the possible overall shrinking of the middle atmosphere due to climatic cooling (Roble and Dickinson, 1989; Rishbeth and Clilverd, 1999). In this particular study, the geomagnetic field characteristics represented by a local time series measured, on average, beneath the auroral oval at 70° N 19° E (geographic), will be examined. Stochastic variations appear as fluctuations driven by ionospheric currents and thus associated magnetic fields perturbing the background geomagnetic field. The time series employed will be described in more detail forthwith.

The approach to analysing the geomagnetic field data here is the same as that used by Hall (2014): first the data are filtered using a boxcar to remove all periodicities less than one day and the result is then subtracted from the original time series, thus producing a residual excluding all pre-conceived (deterministic) periodicities. This is equivalent to "deseasonalization" commonly applied to neutral atmosphere data, for example. The reasoning for removing all fluctuations of period 1 day or larger will become apparent when the data are described in more detail.

The majority of studies to obtain complexity signatures from time series aim at evaluating the Hurst exponent, H, as invented by Hurst, (1951) as a quantification of the scaling nature, or self-affinity of the stochastic component of the data. H, however lies in the interval 0,1 and alone cannot identify the process as fractional Gaussian

Discussion Pape

noise (fGn) or fractional Brownian motion (fBm) as invented by Mandelbrot and van Ness (1968). In the concept of fBm successive increments are correlated: the time series is non-stationary and with temporally varying variance fGn, on the other hand, is stationary and time-invariant in expectation value and variance. In these processes, positive correlation between successive increments indicates that preceding motion is likely to continue and negative correlation indicates that preceding motion is likely to be followed by a reversal, likelihoods commonly referred to as persistent and antipersistent, respectively. Rather than derive H, therefore, the approach of Kantelhardt et al. (2006) is adopted here and the generalized Hurst exponent, α , is derived. The two exponents are related: for fGn, $H = \alpha$ and for fBm, $H = \alpha - 1$. Thus, α unambiguously characterizes as process as fBm ($\alpha > 1$), persistent fGn (0.5 < $\alpha <$ 1) and anti-persistent fGn (0 < α < 0.5), with α = 1.5 indicating the special case of Brownian motion. Furthermore, one can define the scaling exponent of the power spectrum of the signal (the negative of the spectral slope in log-log space) by β :

$$_{15} \quad S(f) \propto |f|^{-\beta} \,. \tag{1}$$

White noise is thus characterized by a flat spectrum and therefore $\beta = 0$. "Pink noise" is when $\beta = 1$, and the case where $\beta = 2$ is referred to as "red noise" and corresponds to Brownian motion, e.g. Vasseur and Yodzis (2004). Importantly, the generalized Hurst exponent, α and the power spectrum scaling exponent, β are related by

$$\alpha = (\beta + 1)/2 \tag{2}$$

as explained by, e.g., Hartmann et al. (2013), Delignieres et al. (2006), and references therein. The relationship is conveniently summarized in Fig. 1 of Hall (2014). Moreover, the fractal or Hausdorff-Besicovich dimension, D = 2 - H, but assuming fBm. One can see, therefore, calculating D by, for example, the method of Grassberger and Procaccia (1983), can potentially yield H but not unambiguously provide the same information as α.

NPGD

1, 895–915, 2014

Complexity in the geomagnetic H component at 70° N. 19° E

C. M. Hall

Title Page

Abstract

Introductio

Conclusions

Reference

Tables

Figures

Back

Close

Full Screen / Esc

Abstract

Reference

Tables

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Following the sequence used by Hall (2014), rather than blindly launch into a determination of α which will almost inevitably yield some result, the data are examined first for indications of non-linearity by inspections of the probability density function (PDF) and quantile-quantile (Q-Q) analyses (Wilk and Gnanadesikan, 1968). 5 A PDF can indicate qualitatively if the distribution is non-Gaussian. In Q-Q plots, quantiles of the distribution of the noise in the signal are plotted against those derived from a semi-empirical Gaussian distribution having the same mean and standard deviation; a straight line will result if the signal exhibits a Gaussian distribution. With a preconception of the nature of the PDF a number of approaches may be employed to obtain α . Some of the most used methods are described and compared by Delignieres et al. (2006), Hartmann et al. (2013), and Heneghan and McDarby (2000) (note, however, that these last authors use " α " as the spectral scaling exponent rather than β). Using experience gained from Hall (2014) α is obtained using both spectral analysis (SA) and detrended fluctuation analysis (DFA); while most physicists will feel comfortable with the more intuitive SA, DFA (Peng et al., 1993) is arguably the preferred method in contemporary research when searching for long-term memory in data. For the purposes of SA, since experimental data are under consideration, the time series should be treated as irregularly sampled; data gaps are few, but even so must be assumed to exist. Lomb-Scargle periodogram analysis (Press and Rybicki, 1989) is more appropriate than a Fourier transform. Additionally, Fougère (1985) and Eke et al. (2000) have proposed preconditioning of the time series by applying a parabolic window, bridge detrending using the first and last points in the series, and finally frequency selection prior to attempting to obtain a spectral exponent. Applying frequency selection to the Lomb-Scargle periodogram is somewhat unpredictable as discovered by Hall (2014), so the entire spectrum is retained. Finally, the spectrum S is plotted vs. f in log-log space to hopefully identify a regime exhibiting a scaling exponent β according to Eq. (1). In DFA, the stochastic component of the original time series is first cumulatively summed (each new point is the sum of the preceding points in the original). This cumulative summation is then divided into sub-series of equal

899

Discussion Paper

1, 895-915, 2014

Complexity in the geomagnetic H component at 70° N. 19° E

NPGD

C. M. Hall

Title Page

Introductio

Conclusions

Figures

NPGD

1, 895–915, 2014

Complexity in the geomagnetic H component at 70° N, 19° E

C. M. Hall

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I ■ ▶I

■ Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

© Û

length (n). Each of these sub-series is then detrended either by subtracting the straight line between end-points (bridge detrending) or linear or polynomial fits (referred to as DFA(1), DFA(2), etc.). Variances are calculated for each sub-series and the then averaged to obtain a mean F(n). After repeating for a range of sub-series lengths (usually all possible n), the function F(n) is plotted vs. n in log-log space (as was done in the spectral analysis case) to hopefully identify a regime exhibiting a scaling exponent α :

$$F(n) \propto n^{\alpha}$$
 (3)

wherein α is the generalized Hurst exponent. Here, a simple linear detrending will be used and DFA will be used to refer to DFA(1).

2 Underlying data and analysis

Analyses of geomagnetic time-series are few relative to for other observables such as surface air temperature (SAT) and, at the other end of the solar-terrestrial system, sunspot number (SSN). Downloadable datasets such as the auroral electrojet index (AE) have been examined, e.g. Rypdal and Rypdal (2011), but the AE index is really a synthesis of individual magnetometer measurements at a selection of observatories under or near the auroral oval and therefore with implicit averaging. Wanliss and Reynolds (2003) have determined β for a number of low latitude records although references therein accentuate the preceding focus on global indices. Hamid et al. (2009) similarly examine data from specific sites. The nature of the data used in this study is somewhat different to those used by Wanliss and Reynolds (2003) and Hamid et al. (2009), however. The geomagnetic field is usually (but not exclusively) defined by three components: declination, D (°), horizontal, H (nT), and vertical, Z (nT). When constructing geomagnetic indices as indicators of activity, for example the k index (Bartels et al., 1939), the horizontal component is preferred because an approximately zonally aligned current system induces a maximum perturbation in the horizontal

Paper

Discussion

Printer-friendly Version

Interactive Discussion



component of the background field immediately below it. The vertical component, on the other hand induces a zero crossing in the perturbation. The magnetometer at Tromsø (70° N, 19° E) is operated as an observatory-standard instrument and as such calibrated accurately at regular intervals (the details of which are superfluous here); this means, however that the time series is long and reliable. This study uses values of H with 10 s time resolution in the interval of 1988–2013 inclusive. In contrast to the studies by Wanliss and Reynolds (2003) and Hamid et al. (2009), here entire years are analysed. Another important difference is the geographical location: at high latitude, most geomagnetic disturbances occur in the evening sector and the fluctuations in H reflect the rotation of the Earth underneath the auroral oval's typically zonally-aligned current systems which move meridionally backwards and forwards in a sporadic fashion over the magnetometer site. Activity can be expected to repeat at timescales of 1 day, and of course over solar rotation (Carrington rotation) (e.g. Bartels, 1934) and longer periods such as the 11-year solar cycle. In order to eliminate these deterministic features from the dataset to be studied a boxcar filter is applied to remove fluctuations less than 24 h; the smoothed time-series is then subtracted from the original to arrive at a set of residuals representing the stochastic component. A corresponding method was employed by Hall (2014) and discussed and tested by Hall et al. (2011). As will be shown, an advantage of spectral analysis is that individual periodicities remaining in the (supposedly) stochastic residual show up as narrow spikes and in practice have an insignificant influence on determination of the slope of the spectrum. On the contrary, in DFA such periodicities are in general *not* distinguishable.

An example of the input data, in this case for 2001 – in the middle of the overall time interval - is shown in Fig. 1. The top panel shows the original data in black and with a 1-day smoothing superimposed. The bottom panel shows the result of subtracting the smoothed time series from the original to obtain a residual representing the stochastic component. Other years are similar. In Fig. 2, the top panels show the distribution of the stochastic component with linear (left) and logarithmic (right) ordinates, again from 2001. In a somewhat unsophisticated approach, although adequate to the purpose, the

NPGD

1, 895–915, 2014

Complexity in the geomagnetic H component at 70° N. 19° E

C. M. Hall

Title Page

Introductio **Abstract**

Conclusions Reference

> **Figures Tables**

Close

Back

Full Screen / Esc

Discussion Paper

Figures

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



maximum of the distribution and its width at half-maximum are determined. The mean is assumed to be zero as a result of the subtraction of the deterministic component as illustrated in Fig. 1. Corresponding Gaussian and Cauchy distributions are determined and these are also shown in the figure. A characteristic of the distributions (for all years) 5 is that they are skewed; this is because the current in the overlying ionosphere tends to have a preferred orientation and perturbations of the horizontal geomagnetic field tend to be negative on average. Qualitatively the Cauchy distribution is a better description of that of the data than the Gaussian. Again all years are similar, although for less skewed distributions the suitability of the Cauchy model is even more evident. Furthermore, in contrast to the Gaussian model the data exhibit heavy tails. The bottom panels of Fig. 2. show the quantile-quantile (Q-Q) portrayals – left: vs. Gaussian and right: vs. Cauchy. The departures from linearity (i.e. in the central regions of the respective plots) are indicative of long tails at both ends of the distribution relative to the model. See Chambers et al. (1963) for diagnostics of Q-Q plots. The Cauchy distribution reproduces the tails in the data distribution rather better than the Gaussian. Recall, however that in this simple approach, the half-maximum full-width values have been matched and comparisons might have been improved by choosing 1/e or another arbitrary value. Nonetheless, a Cauchy distribution would always represent the tails in the data distribution better than a Gaussian. It is important to note at this point that a Cauchy process can be defined as a Brownian motion subordinated to a process associated with a Lévy distribution (Sato, 1999). Again, it should be noted that analyses for all 25 years exhibit similar characteristics, and thus that the results hitherto justify the further investigation that follows.

The next step is to determine the power spectral density and its scaling with respect to frequency. A stated earlier it is incorrect to presuppose there are no data breaks and therefore a Lomb-Scargle periodogram is derived, rather than the more traditional Fourier transform, but having first preconditioned the time series by applying a parabolic window and bridge detrending using the first and last points. The result (again for 2001) is shown in the left panel of Fig. 3. At periods greater than one

NPGD

1, 895–915, 2014

Complexity in the geomagnetic H component at 70° N. 19° E

C. M. Hall

Title Page

Abstract

Introductio

Conclusions

Reference

Tables

Back

Full Screen / Esc

Printer-friendly Version



day fluctuations have been effectively removed by the subtraction of the deterministic component, and, as predicted, discrete peaks at 1 day and (approximately) 12 h remain demonstrating the method not to be perfect. Vertical dotted and dashed lines indicate familiar timescales. Convincing scaling is evident from 1 day down to approximately 5 min; there is a suggestion of a subrange between 5 and 1-min scales and then a tendency to flattening. The scaling exponent β has therefore been obtained over two subranges, day-minute and 12-1 h indicated on the plot by red ($\beta = 2.014 \pm 0.001$) and cyan ($\beta = 1.811 \pm 0.012$) lines respectively. The annotation gives the result of the overall day-minute scaling (the red line) expressed as the generalized Hurst exponent α (1.51), whereas the 12–1 h scaling yields α = 1.41. The DFA(1) analysis of the same data is shown in the right hand panel of Fig. 3. Again familiar timescales are indicated in the plot, and linearity over approximately 2 orders of magnitude yields $\beta = 1.474 \pm 0.002$. Departure from the fitted line is easy to identify at longer timescales. but not at shorter timescales, as opposed to as seen in the SA approach. On the other hand, DFA results in a much "cleaner" plot. Had timescales > 1 h been excluded from the fit in the DFA, α from the overall SA and α from the DFA would have been similar. It can be argued that SA is easier to interpret because a physicist would normally have some preconception of the processes characterized by different timescales, hidden to some degree when using only DFA. At this point the method used here departs somewhat from that used by Hall (2014), in which surrogate data were generated and then compared with the original (Theiler et al., 1992). For the purposes of this study, at least, generation of, for example 100 surrogate data sets corresponding to 1 year long 10 s resolution (i.e. over 3 million points) followed by DFA analyses is not practicable for computational reasons. Inspection of the probability distribution functions combined with visual comparison with known distributions and subsequently Q-Q analyses is deemed to confirm the complex nature of the stochastic process in the data. Again, only one year's results are shown here; all 25 years exhibit similar values of α when for each of DFA and the two SA subranges.

NPGD

1, 895-915, 2014

Complexity in the geomagnetic H component at 70° N. 19° E

C. M. Hall

Title Page

Abstract

Conclusions Reference

Figures

Introductio

Tables

Close

Back

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



The results of analysing all 25 years from 1988 to 2013 inclusive as described and illustrated for 2001 above are shown in Fig. 4. From top to bottom the panels show: DFA(1), SA (1 d-1 min) and SA (12-1 h). The final panel shows yearly mean sunspot numbers from the Solar Influence Data Analysis Center (SIDC) (Clette, 2011). For each year (small) vertical bars indicate the 1- σ uncertainty in the individual linear fits. It is evident (by comparing axes) that by taking all scales between 1 d and 1 min in the SA, α is always > 1.5. DFA and SA (12–1 h) the α s are similar and always < 1.5. There are considerable year-to-year variations irrespective of method, but no obvious periodicity that could be attributable to the two solar cycles the data set spans. On the other hand, linear regressions reveal trends, which are also indicated in the figure together with 95% confidence limits according to the method of Working and Hotelling (1929). The trends are small but worth mentioning here to give the possibility for comparison with other studies in future. For DFA the trend is $0.04 \pm 0.05 \, \text{century}^{-1}$; for SA (1 d-1 min), 0.2 ± 0.2 century⁻¹; for SA (12–1 h), 0.01 ± 0.1 century⁻¹. Since in all 3 cases, the uncertainties are approximately equal to the trends themselves, none of the values can be considered to be significant. The mean values of α over the 25 years are: DFA, 1.46 ± 0.02 ; SA (12–1 h), 1.54 ± 0.07 ; SA (1 d–1 min), 1.39 ± 0.04 .

Discussion and conclusions

To summarize the above findings, all analyses, irrespective of scale, indicate fBm. Both SA used in the regime 12–1 h and DFA (in which determination of the scaling exponent is weighted towards the longest scales), indicate $\alpha \approx 1.42$. For day-minute scales SA yields $\alpha = 1.54$ but the uncertainty dictates that the result cannot be regarded as significantly different from, for example that of the DFA. The results weighted towards longer timescale fluctuations, however, exhibit small enough uncertainties that taken collectively one can conclude that α is slightly less than 1.5, the significance of which will be discussed forthwith. Other studies of complexity in geomagnetic, or geomagnetically related time series have either used isolated periods of, for example,

NPGD

1, 895–915, 2014

Complexity in the geomagnetic H component at 70° N. 19° E

C. M. Hall

Title Page

Introductio **Abstract**

Conclusions Reference

Figures Tables

Close

Paper

NPGD

Complexity in the geomagnetic H component at 70° N, 19° E

1, 895-915, 2014

C. M. Hall

Title Page

Introductio **Abstract**

Conclusions Reference

Figures Tables

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



months (Wanliss and Reynolds, 2003; Hamid et al., 2009) albeit with time resolution comparable to that used here, or much longer derived datasets of, for example AE index with different time resolution. Rypdal and Rypdal (2010) studied AE index at timescales similar to those addressed here. Averaging, even over several relatively local time-5 series (as is done when determining the AE index, but especially globally - e.g. for the KP index) will tend to even out variances over intra-diurnal timescales, e.g. occurrence of local ionospheric current systems. Any non-stationarities may be masked out such that local determinations of α and identification of processes as fGn or fBm may well differ. Wanliss and Reynolds (2003) and Hamid et al. (2009) employed geomagnetic data from specific stations, but for low latitude. In contrast to the analyses here, Wanliss and Reynolds (2003) examined only a short time interval of 5 days, but for 6 different Southern Hemisphere sites determining α to increase approximately with increasing latitude (southward) from $\alpha = 1.55$ to $\alpha = 1.69$ i.e. fBm but with consistently slightly higher exponents than determined here. Hamid et al. (2009) employed a longer dataset (1 month) than Wanliss and Reynolds (2003) but for 2 sites. However Hamid et al. (2009) categorized days as active or quiet and finding active days exhibited $\alpha = 1.64$ and 1.55 for the two sites, and, for quiet days, $\alpha = 1.45$ and 1.33. In this study, no attempt has been made to pick out quiet and disturbed days. Over the course of an entire year, however, it could be expected that quiet days predominate considering that the rapid perturbations extracted from the observation and deemed to be a stochastic component rely on current systems being approximately over the magnetometer. The findings in this study, viz. that α lies slightly under 1.5, can be considered in good agreement with those of Wanliss and Reynolds (2003) and Hamid et al. (2009). In order to attempt to discriminate between active and quiet years (e.g. Vaquero et al., 2014), however annual mean sunspot numbers have been plotted in the bottom panel of Fig. 4. There is no conclusive correlation between solar activity and the values of α from the 2 methods (and 2 scaling ranges). If the trends could be considered significant (which they are not) they might be seen to anticorrelate with overall solar activity over

Paper

9)

the 25 years (quieter sun) which would contradict the suggestion by Hamid et al. (2009) that active days are characterized by $\alpha > 1.5$.

Wanliss and Reynolds (2003) point to several publications employing high latitude geomagnetic data, but these use the AE index. Takalo et al. (1994) find that AE scales with $\alpha \approx 1$ for low frequencies (timescales > 100 min) and $\alpha \approx 1.5$ for high frequencies (1–100 min, and therefore shorter than typical substorm durations). Note that Takalo et al. (1994) use " α " for power-law dependence whereas this study uses " β ", and thereafter Rypdal and Rypdal (2010) convert the value of Takalo et al. (1994) value to "H" – the Hurst exponent. In terms of the classification used here and also by Kantelhardt et al. (2006), AE appears as a non-stationary process for intra-sub-storm timescales with $\alpha \approx 1.5$ but becoming stationary (i.e. fGn) when only >sub-storm timescales are considered. This is compatible with the findings here because at any given instant, it is unlikely that the same geomagnetic fluctuations will be registered by more than a few geographically grouped observations: AE and the stochastic component of H should be expected to exhibit similar signatures at short timescales, and this is the case here.

Other studies of geomagnetic signatures include analysis of the Disturbance storm time (Dst) index, e.g. by Balasis et al. (2006), who calculate, explicitly, β for periods during 2001 and for the entire year. Scaling was examined in the range of 5 d–2 h and indicated α between \sim 1.4 and \sim 1.6. However inspection of the spectra, and particularly for the whole year (as used here too) there is a suggestion of a change of slope at \sim 10 h, such the higher frequency subrange would yield a slightly higher (presumably > 1.5) result for α . This is not the same as the spectral breakpoint mentioned in this study, but together they illustrate that bicoloured noise (Takalo et al., 1994) may well be present. Recent exploits into complexity matching are worthy of note: Scafetta and West (2003), proposed terrestrial temperature anomalies to be linked to solar flare intermittency via a Lévy process. Rypdal and Rypdal (2011) find identical multifractal noise signatures in both the AE index and the z component of the interplanetary magnetic field suggestive of the existence of mechanisms linking

NPGD

1, 895–915, 2014

Complexity in the geomagnetic H component at 70° N, 19° E

C. M. Hall

Title Page

Abstract Introductio

Conclusions References

Tables Figures

I₫

•

Back

Close

Full Screen / Esc

Printer-friendly Version



Tables

Back

Printer-friendly Version

Interactive Discussion

intermittency in the two. These studies utilised very long datasets, typically of 1-month time resolution aimed at facilitating better trend analyses and prediction of future climate, Here, similar techniques are employed on shorter (~years) datasets with higher time resolution (~seconds) but to help identify differences between geographically local complexity. Kantelhardt et al. (2006), using different hydrological data types, explain how results from shorter-term data could be modelled by an autoregressive movingaverage (ARMA) (Wittle, 1951), but given the time series lengths and similarities with other work, fBm seems a good candidate to model the stochastic nature of the geomagnetic field.

To conclude: 25 years of 10 s local measurements of the horizontal component of the geomagnetic field are examined, one year at a time. All variability with timescales 1d or longer thus including anticipated and/or known periodicities are removed. This is analogous to deseasonalization of, for example, monthly temperature data - a common practice for meteorological time-series, but apparently not necessarily the case for studies of the AE index. Thereafter, Q-Q followed by SA and DFA analyses are performed revealing, as a characteristic common to all years, distributions better described as Cauchy rather than Gaussian. The SA, performed here by a Lomb-Scargle periodogram analysis, rather than the more usual Fourier analysis, in order to allow for data-gaps, suggests bicoloured spectra, more difficult to discern if using DFA alone. The resulting generalized Hurst exponents, α , all lie in the region of 1.5 (mostly ≈ 1.42), although there is a possibility that for shorter timescales (down to 1 min) $\alpha \approx 1.55$. The former is indicative of fBm but with a degree of likelihood for fast switching of direction in the motion (antipersistence), while the latter is indicative of a higher persistence. This difference could be explained thus: during the course of an evening, changes in the position of the auroral electrojet can be considered rapid, whereas from minute-to-minute the electrojet moves more persistently in geomagnetic latitude. The results are in excellent agreement with independent findings both derived from local data, as used here, and with zonally averaged data as comprises the AE index, for example. This would, in turn, support a hypothesis that geomagnetic

NPGD

1, 895–915, 2014

Complexity in the geomagnetic H component at 70° N. 19° E

C. M. Hall

Title Page Introductio **Abstract** Conclusions Reference

Close

Figures

Full Screen / Esc

Discussion Pape

field variations can be universally described by fractional Brownian motion. Matching this signature with those identified in space weather parameterizations add to a growing arsenal of tools available for understanding and forecasting the impact of solar activity on the terrestrial environment. This study also points the way to further, although computationally demanding, analyses including use of geomagnetic data from other locations, hypothesis-testing using surrogates and more refined data selection according to disturbed conditions.

Acknowledgements. The author acknowledges the staff of Tromsø Geophysical Observatory for ensuring consistency in the dataset chosen for this study and in particular Børre Heitmann Holmeslet for assistance in assembling the time series. Data from the Tromsø station can be obtained via World Data Centres for Geomagnetism.

References

- Balasis, G., Daglis, I. A., Kapiris, P., Mandea, M., Vassiliadis, D., and Eftaxias, K.: From prestorm activity to magnetic storms: a transition described in terms of fractal dynamics, Ann. Geophys., 24, 3557-3567, doi:10.5194/angeo-24-3557-2006, 2006.
- Bartels, J.: Twenty-Seven Day Recurrences in Terrestrial-Magnetic and Solar Activity, 1923-1933, Terrestrial Magnetism and Atmospheric Electricity, 39, 201–202, 1934.
- Bartels, J., Heck, N. H., and Johnston, H. F.: The three-hour range index measuring geomagnetic activity, Terrestrial Magnetism and Atmospheric Electricity, 44, 411-454, doi:10.1029/TE044i004p00411, 1939.
- Chambers, J. M., Cleveland, W. S., Kleiner, B., and Tukey, P. A.: Graphical Methods for Data Analysis, 395 pp., Duxbury Press, Boston, Massachusetts, 1963.
- Clette, F.: Past and future sunspot indices: new goals for SoTerIA, J. Atmos. Sol.-Terr. Phys., 73. 182-186. 2011.
- Delignieres, D., Ramdani, S., Lemoine, L., Torre, K., Fortes M., and Ninot, G.: Fractal analyses for "short" time series: A re-assessment of classical methods, J. Math. Psychol., 50, 525-544, 2006.

NPGD

1, 895–915, 2014

Complexity in the geomagnetic H component at 70° N. 19° E

C. M. Hall

Title Page

Introductio **Abstract**

Conclusions Reference

> **Tables Figures**

Back

Full Screen / Esc

Close



NPGD

1, 895-915, 2014

Complexity in the geomagnetic H component at 70° N, 19° E

C. M. Hall

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I◀ ▶I

Full Screen / Esc

Back

Close

Printer-friendly Version

Interactive Discussion

© BY

- Eichner, J. F., Koscielny-Bunde, E., Bunde, A., Havlin, S., and Schnellnhuber, H.-J.: Power-law persistence and trends in the atmosphere: A detailed study of long temperature records, Phys. Rev. E, 68, 046133, doi:10.1103/PhysRevE.68.046133, 2003.
- Eke, A. H., Hermán, P., Bassingthwaighte, J. B., Raymond, G. M., Percival, D. B., Cannon, M., Balla, I., and Ikrényi, C.: Physiological time series: Distinguishing fractal noises from motions, Pflug. Arch. Eur. J. Phy., 439, 403–415, 2000.
- Fougère, P.F.: On the accuracy of spectrum analysis of red noise processes using maximum entropy and periodograms methods: Simulation studies and application to geographical data, Geogr. Res., 90, 4355–4366, 1985.
- Grassberger, P. and Procaccia, I.: Measuring the strangeness of strange attractors, Physica D, 9, 189–208, 1983.
 - Hall, C. M., Rypdal, K., and Rypdal, M.: The E-region at 69° N 19° E: trends, significances and detectability, J. Geophys Res., 116, A05309, doi:10.1029/2011JA016431, 2011.
 - Hall, C. M.: Complexity signatures for short time scales in the atmosphere above Adventdalen, Svalbard, J. Geophys. Res., 119, doi:10.1002/2013JD020988, 2014.
 - Hamid, N. S. A., Gopir, G., Ismail, M., Misran, N., Hasbi, A. M., Usang, M. D., and Yumoto, K.: The Hurst exponents of the geomagnetic horizontal component during quiet and active periods, in: International Conference on Space Science and Communication, 2009. IconSpace 2009, 186–189, IEEE publishing, US and Canada, 2009.
- Hartmann, A., Mukli, P., Nagy, Z., Kocsis, L., and Hermán, P.: Real-time fractal signal processing in the time domain, Physica A, 392, 89–102, 2013.
 - Heneghan, C. and McDarby, G.: Establishing the relation between detrended fluctuation analysis and power spectral density analysis for stochastic processes, Phys. Rev. E, 62, 6103–6110, 2000.
- 25 Hurst, H. E.: Long-term storage of reservoirs: an experimental study, T. Am. Soc. Civ. Eng., 116, 770–799, 1951.
 - Kantelhardt, J. W., Koscielny-Bunde, E., Rybski, D., Braun, P., Bunde, A., and Havlin S.: Long-term persistence and multifractality of precipitation and river runoff records, J. Geophys. Res., 111, D01106, doi:10.1029/2005JD005881, 2006.
- Koscielny-Bunde, E., Bunde, A., Havlin, S., Roman, H. E., Goldreich, Y., and Schnellnhuber, H.-J.: Analysis of daily temperature fluctuations, Phys. Rev. Lett., 81, 729–732, 1998.
 - Lennartz, S. and Bunde, A.: Trend evaluation in records with long-term memory: application to global warming, Geophys. Res. Lett., 36, L16706, doi:10.1029/2009GL039516, 2009.
 - 909

Paper

Discussion Pape

Printer-friendly Version

Mandelbrot, B. B.: The fractal geometry of nature, Macmillan, ISBN 978-0-7167-1186-5, 486 pp., 1983.

Mandelbrot, B. B. and van Ness, J. W.: Fractional Brownian motions, fractional noises and applications, SIAM Rev., 10, 422-437, 1968.

5 Peng, C. K., Mictus, J., Hausdorff, J., Havlin, S., Stanley, H. E., and Goldberger, A.L.: Longrange anticorrelations and non-Gaussian behavior of the heartbeat, Phys. Rev. Lett., 70, 1343–1346, 1993.

Press, W. H. and Rybicki, G. B.: Fast algorithm for spectral analysis of unevenly sampled data, Astron. J., 338, 277–280, 1989.

Rishbeth, H., and Clilverd, M.: Long-term change in the upper atmosphere, Astron. Geophys., 40. 3.26-3.28. 1999.

Roble, R. G. and Dickinson, R. E.: How will changes in carbon-dioxide and methane modify the mean structure of the mesosphere and thermosphere?, Geophys, Res. Lett., 16, 1441–1444. 1989.

Rypdal, M. and Rypdal, K.: Stochastic modeling of the AE index and its relation to fluctuations in B_z of the IMF on time scales shorter than substorm duration, J. Geophys. Res., 115, A11216, doi:10.1029/2010JA015463, 2010.

Rypdal, M. and Rypdal, K.: Discerning a linkage between solar wind turbulence and ionospheric dissipation by a method of confined multifractal motions, J. Geophys. Res., 116, A02202. doi:10.1029/2010JA015907, 2011.

Sato, K.: Lévy processes and infinitely divisible distributions, Cambridge Studies in Advanced Mathematics, 468 pp., Cambridge University Press, Cambridge, 1999.

Scafetta, N. and West, B. J.: Solar flare intermittency and the Earth's temperature anomalies, Phys. Rev. Lett., 90, 248701, doi:10.1103/PhysRevLett.90.248701, 2003.

Takalo, J., Timonen, J., and Koskinen, H.: Properties of AE data and bicolored noise, J. Geophys. Res., 99, 13239-13249, 1994.

Theiler, J., Eubank, S., Longtin, A., Galdrikian B., and Farmer, J. D.: Testing for nonlinearity in time series: the method of surrogate data, Physica D, 58, 77–94, 1992.

Vaquero, J. M., Gutiérrez-López, S., and Szelecka, A.: A note on the relationship between sunspot numbers and active days, Adv. Space Res., 53, 1180-1183, 2014.

Vasseur, D. A., and Yodzis, P.: The color of environmental noise, Ecology, 84, 1146-1152, 2004.

1, 895–915, 2014

Complexity in the geomagnetic H component at 70° N. 19° E

NPGD

C. M. Hall

Title Page

Abstract Introduction

Conclusions References

Tables Figures

 \triangleright

Close

Full Screen / Esc

Wanliss, J. A. and Reynolds, M. A.: Measurement of the stochasticity of low-latitude geomagnetic temporal variations, Ann. Geophys., 21, 2025-2030, doi:10.5194/angeo-21-

Wilk, M. B. and Gnanadesikan, R.: Probability plotting methods for the analysis of data, Biometrika, 55, 1-17, 1968.

2025-2003, 2003.

Whittle, P.: Hypothesis Testing in Time Series Analysis, 120 pp., Hafner Publishing Co., New York, 1951.

Working, H. and Hotelling, H.: Application of the theory of error to the interpretation of trends, Journal of the American Statistical Assocation, 24, 73-85, 1929.

NPGD

1, 895-915, 2014

Complexity in the geomagnetic H component at 70° N. 19° E

C. M. Hall

Title Page **Abstract** Introduction References Conclusions **Figures Tables**

14

 \triangleright

Close Back

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



911



1, 895-915, 2014

Complexity in the geomagnetic H component at 70° N, 19° E

NPGD

C. M. Hall



Full Screen / Esc

Printer-friendly Version



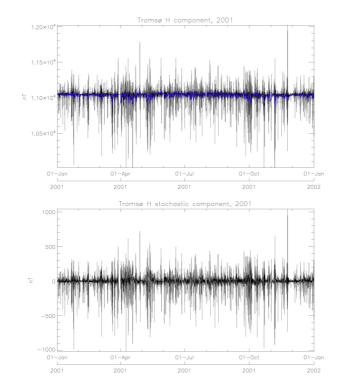


Fig. 1. H-component of geomagnetic field from Tromsø, 70° N, 19° E for the year 2001. Data are at 10s time resolution. The top panel shows the original data in black and with a 1day smoothing superimposed in blue. The bottom panel shows the residual - the result of subtracting the smoothed time series from the original.







Discussion Paper

Back Full Screen / Esc

Abstract

Conclusions

Tables

Printer-friendly Version

NPGD

1, 895-915, 2014

Complexity in the

geomagnetic

H component at

70° N, 19° E

C. M. Hall

Title Page

Introduction

References

Figures

M

Close



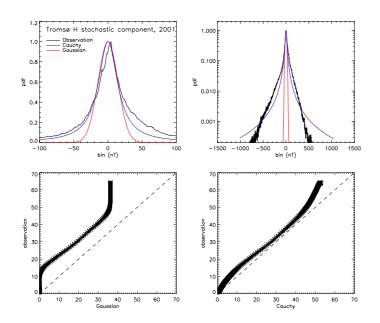


Fig. 2. Portrayals of the distribution of the stochastic component of the H-component of the geomagnetic field from 2001 as shown in Fig. 1. Top-left: linear ordinate axis; top right: logarithmic ordinate axis. In the top panels Gaussian (red) and Cauchy (blue) distributions are fitted (explained and discussed in the text). Bottom left: Q-Q plot of the observed data versus Gaussian; bottom right: Q-Q plot of the observed data versus Cauchy.

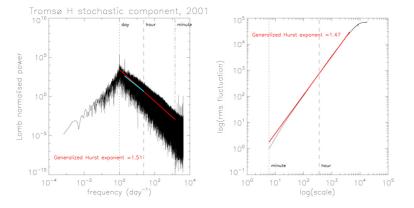


Fig. 3. Spectral (left) and detrended fluctuation (right) analyses for data shown in previous figures. Familiar timescales are indicated by vertical dotted/dashed lines. Fitted scaling exponents are shown by coloured lines together with corresponding values.

NPGD

1, 895-915, 2014

Complexity in the geomagnetic H component at 70° N, 19° E

C. M. Hall

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

I◀

►I

•

•

Back

Close

Full Screen / Esc

Printer-friendly Version



Discussion Paper

Interactive Discussion



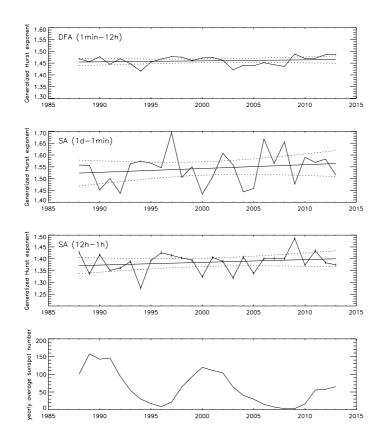


Fig. 4. Generalized Hurst exponents (β) from all years 1988–2013 (with uncertainties). Top: DFA method; second panel: SA method using range 1 day-1 min; third panel: SA using only 12-1 h. Tentative linear trends are shown together with 95% confidence limits indicated by dotted hyperbolae. Bottom panel: yearly average sunspot numbers.

NPGD

1, 895-915, 2014

Complexity in the geomagnetic H component at 70° N. 19° E

C. M. Hall

Title Page

Abstract Introduction

Conclusions References

> **Figures Tables**

 \triangleright

Close Back

Printer-friendly Version